



Alexander Zaytsev

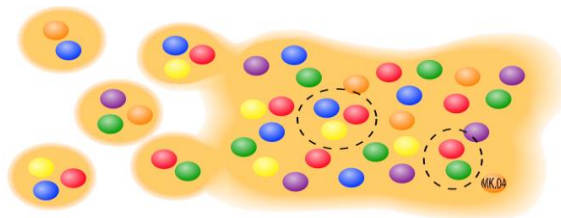
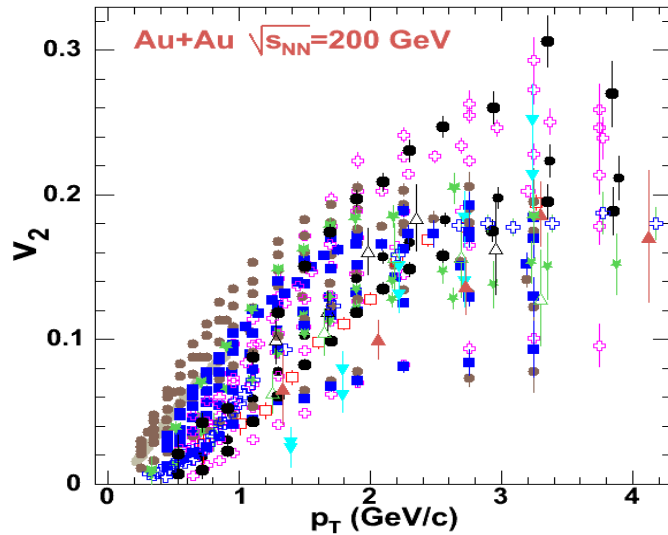
National Research Nuclear University MEPhI

# Scaling properties of collective effects at RHIC

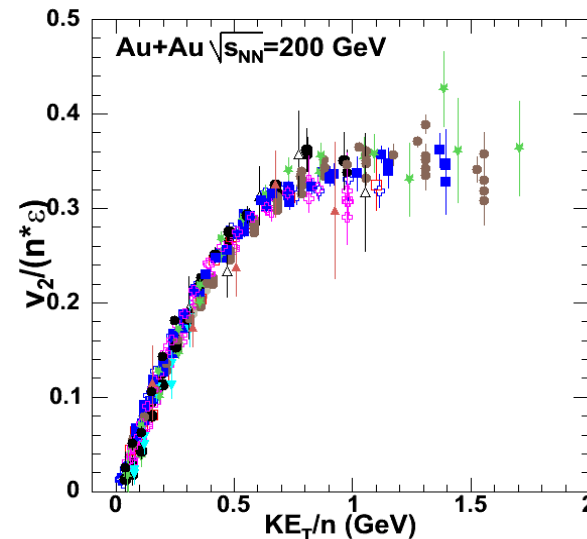
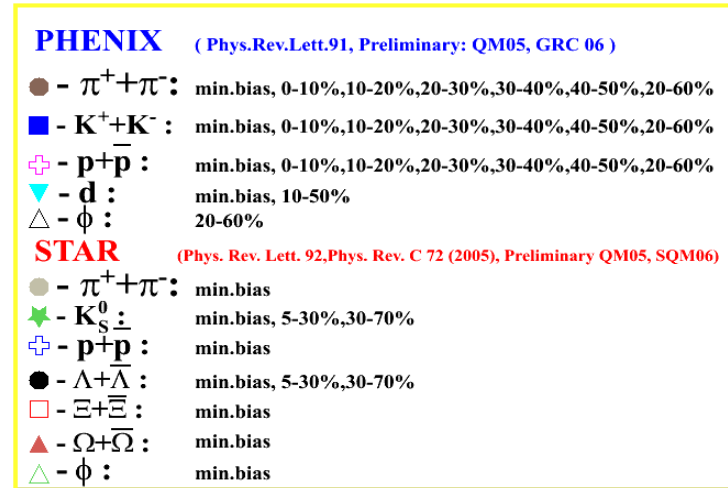
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# Collective flow at RHIC: 2005



$n=3$  for baryons and  $n=2$  for mesons

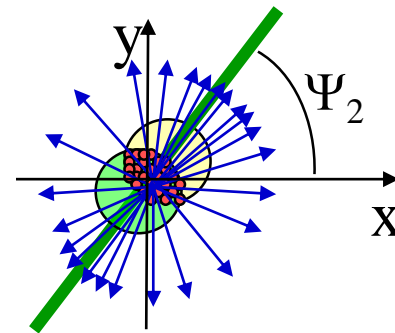
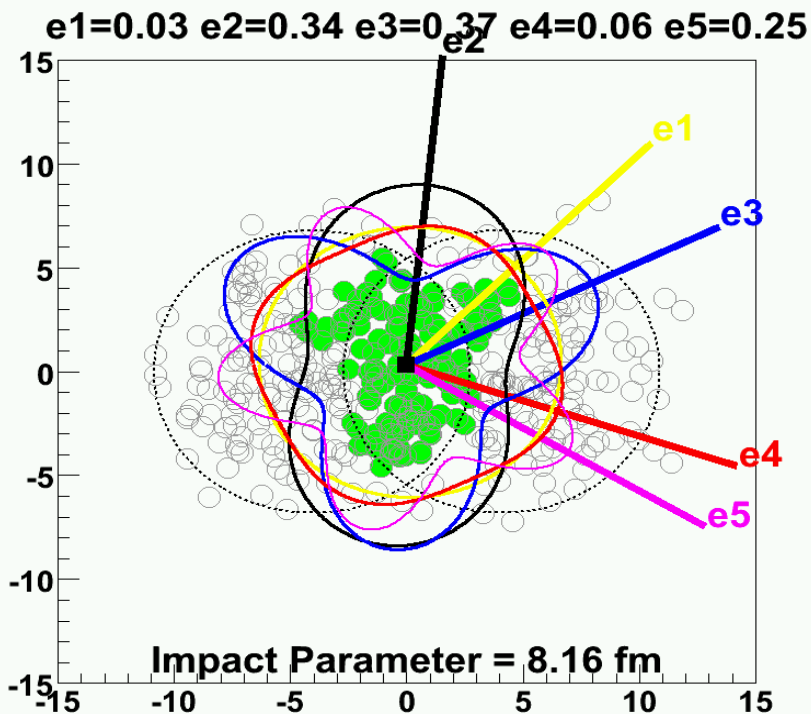
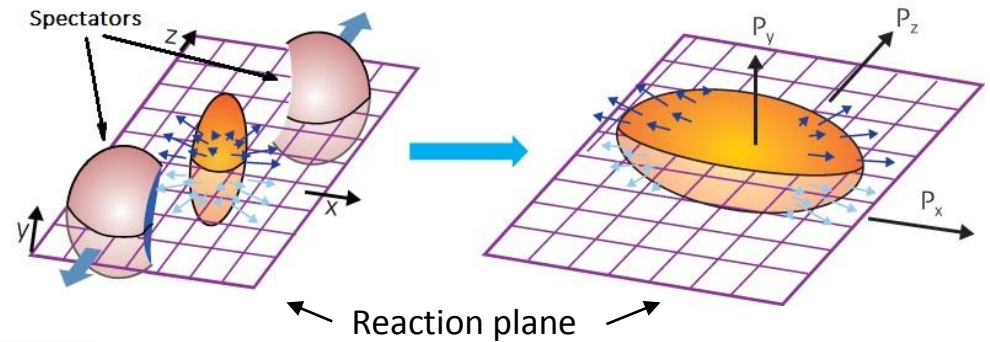


# Collective flow

Fourier coefficients:

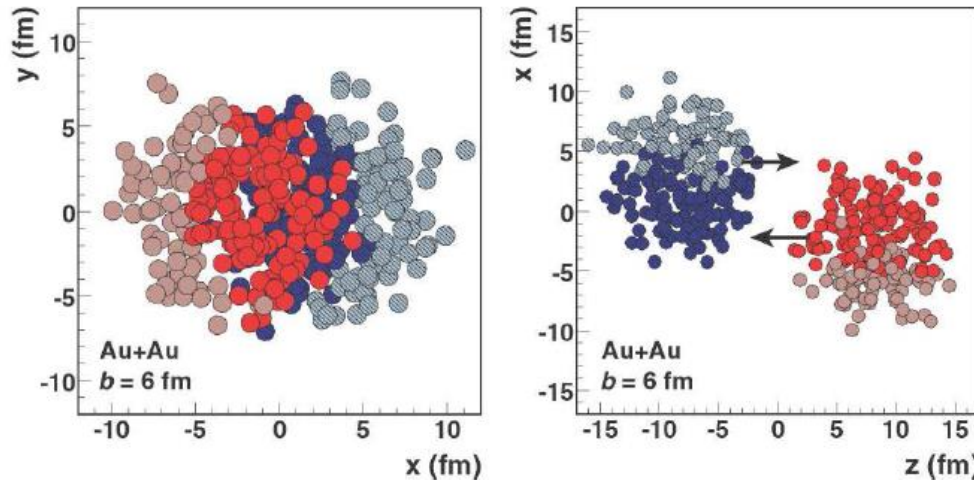
$$\frac{dN}{d\phi} \propto \left( 1 + \sum_{n=1} v_n \cos(n\phi - n\Psi_n) \right)$$

$$v_n = \langle \cos n(\phi - \Psi_n) \rangle$$



Event plane – an estimate of the reaction plane

# Glauber model



Glauber Monte Carlo event  
Au+Au at  $\sqrt{s_{NN}} = 200$  GeV

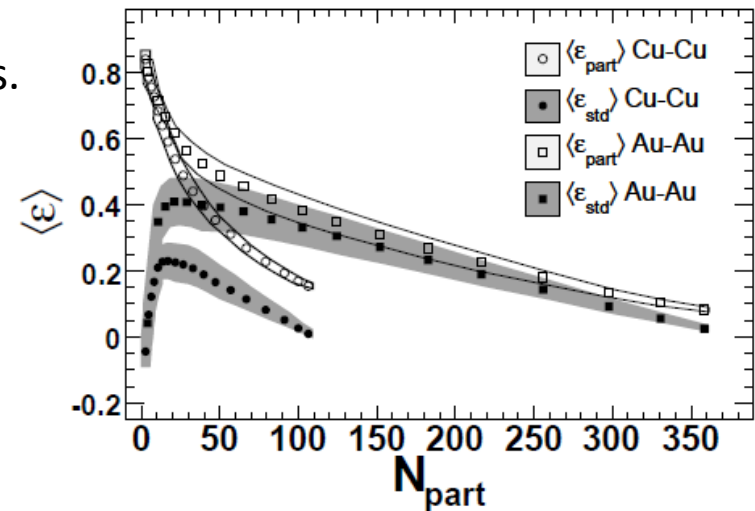
$$\frac{1}{R} = \sqrt{\frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2}}$$

$$\epsilon_n = \sqrt{\frac{\langle r^n \cos n\phi \rangle + \langle r^n \sin n\phi \rangle}{\langle r^n \rangle}}$$

$$\epsilon = \frac{\langle Y^2 - X^2 \rangle}{\langle Y^2 + X^2 \rangle}$$

$$\epsilon_{\text{part}} = \frac{\sqrt{(\sigma_x^2 - \sigma_y^2)^2 + 4(\sigma_{xy}^2)^2}}{\sigma_x^2 - \sigma_y^2}$$

Eccentricity vs.  
number of  
participants



Miller M L et al. 2007 *Ann. Rev. Nucl. Part. Sci.* **57** 205-243

# Is QGP a perfect fluid?

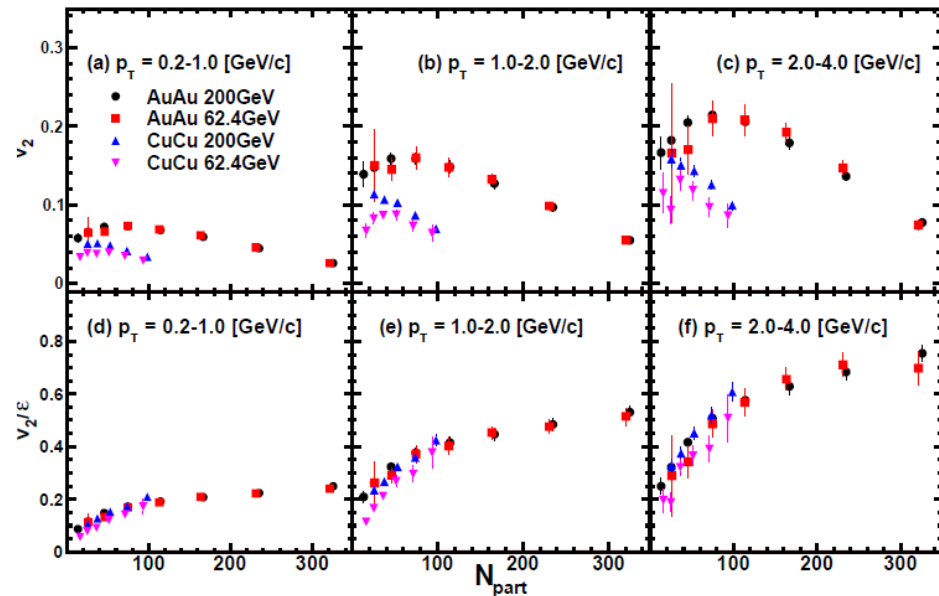
## Not quite

For perfect fluids  $v_2/\varepsilon$  should be independent on  $N_{\text{part}}$ , but for nonperfect fluids it also should depends on the Knudsen number:

$$K = \lambda / \bar{R}$$

( $\lambda$  is the mean free path)

PHENIX data



Adare A *et al.* (PHENIX collaboration) 2014 [arXiv:1412.1043](https://arxiv.org/abs/1412.1043)

# Applying viscous hydrodynamics

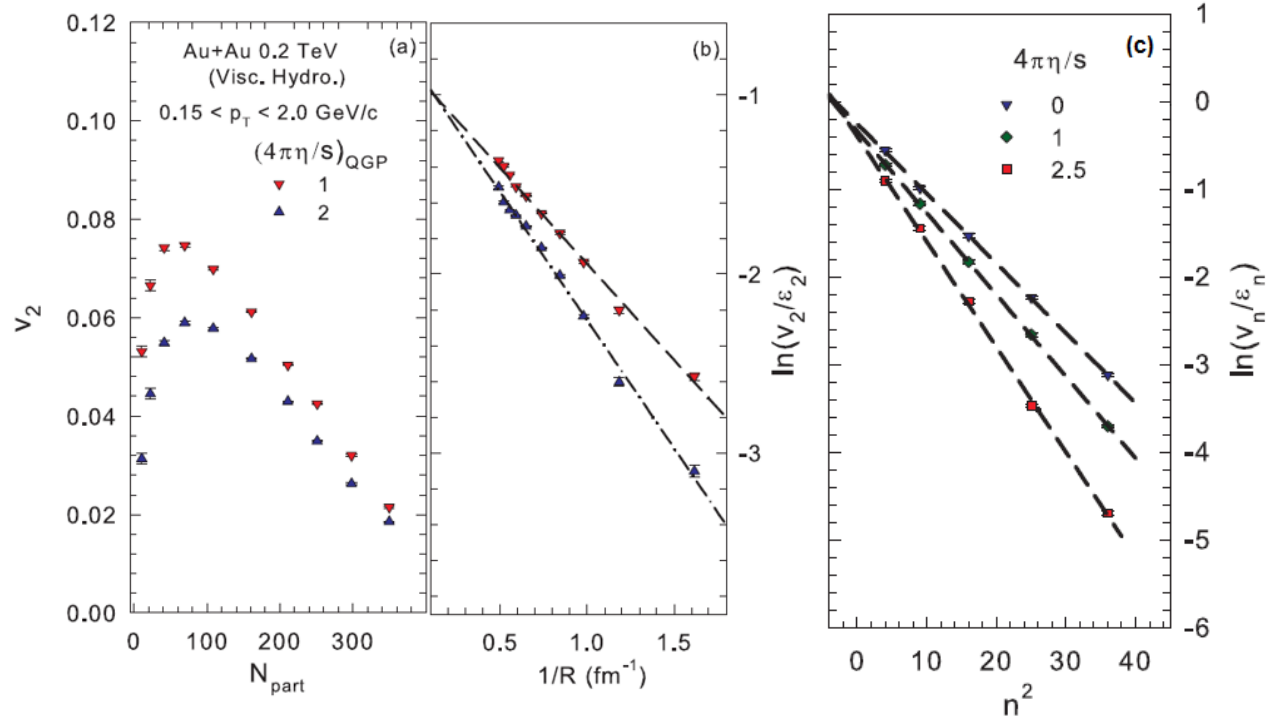
One effects of viscosity on sounds is damping of their amplitude. Assumption of the acoustic nature of collective flow leads to following dependencies:

$$\frac{A(t)}{A(0)} = \exp\left(-\frac{2}{3} \frac{\eta}{s} \frac{k^2 t}{T}\right)$$

$$\frac{v_n}{\varepsilon_n} \sim \exp\left[-C n^2 \frac{\eta}{s} \frac{1}{T R}\right]$$



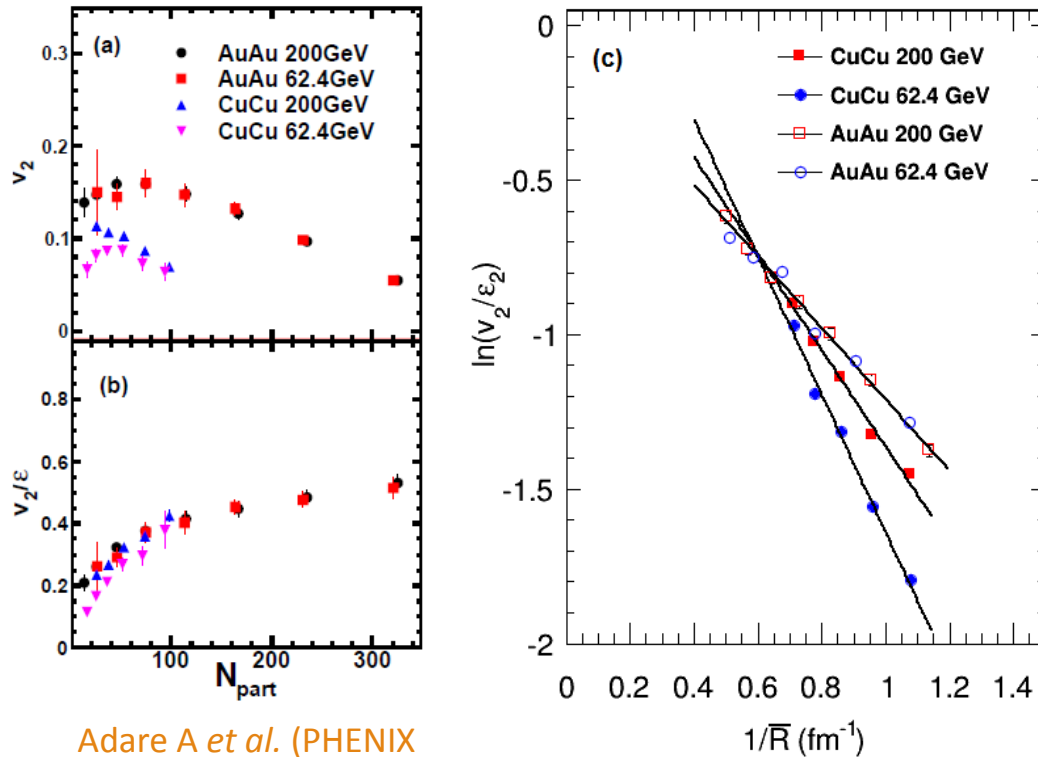
where  $\bar{R}$  is the transverse size of the collision zone



Shuryak E 2014 *arXiv:1412.8393*

Song H *et al.* 2011 *Phys.Rev. C* **83** 054910  
Lacey R A *et al.* 2014 *Phys. Rev. Lett.* **112** 082302

# Acoustic scaling for the PHENIX data



Adare A *et al.* (PHENIX collaboration) 2014  
arXiv:1412.1043

- The slopes are the same for Au+Au collisions at  $\sqrt{s_{NN}} = 62.4$  and 200 GeV.
- The slopes are different for Au+Au and Cu+Cu at  $\sqrt{s_{NN}} = 200$  GeV
- The slope is larger for Cu+Cu at 62.4 GeV than for 200 GeV.

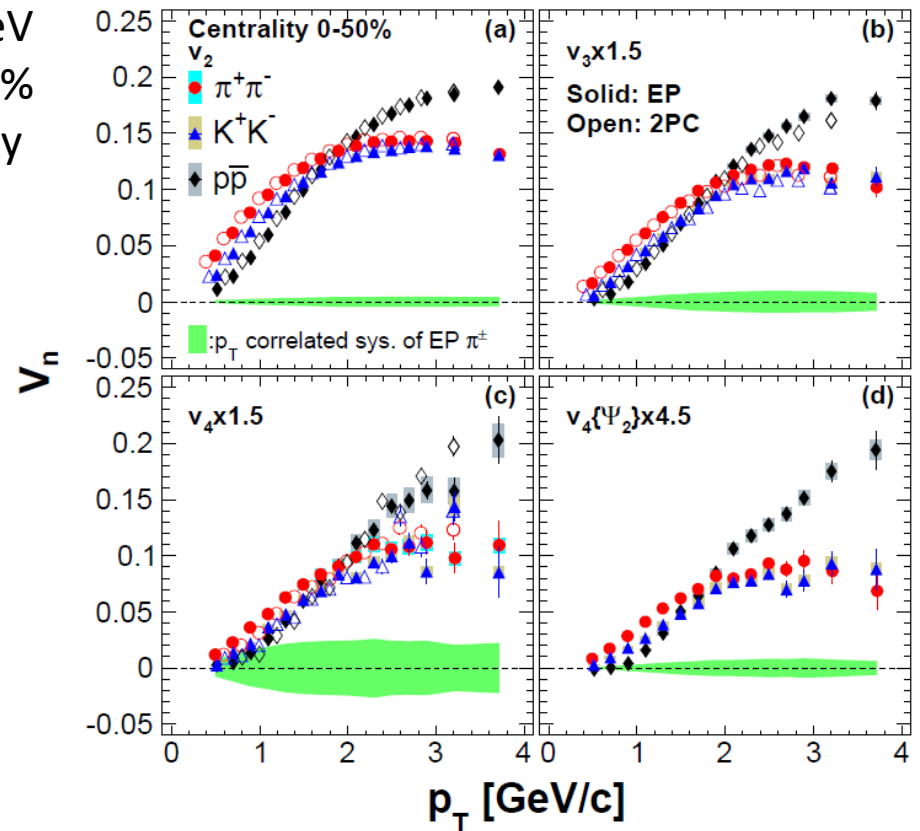
# Collective flow for identified hadrons

Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV  
 Centrality 0 – 50 %  
 Midrapidity

- At low  $p_T$ : the anisotropy is the highest for the lightest hadrons
- At high  $p_T$ : anisotropy is greater for the (anti-)baryons than for the mesons



quark scaling?



Adare A *et al.* (PHENIX collaboration) 2014 [arXiv:1412.1038](https://arxiv.org/abs/1412.1038)



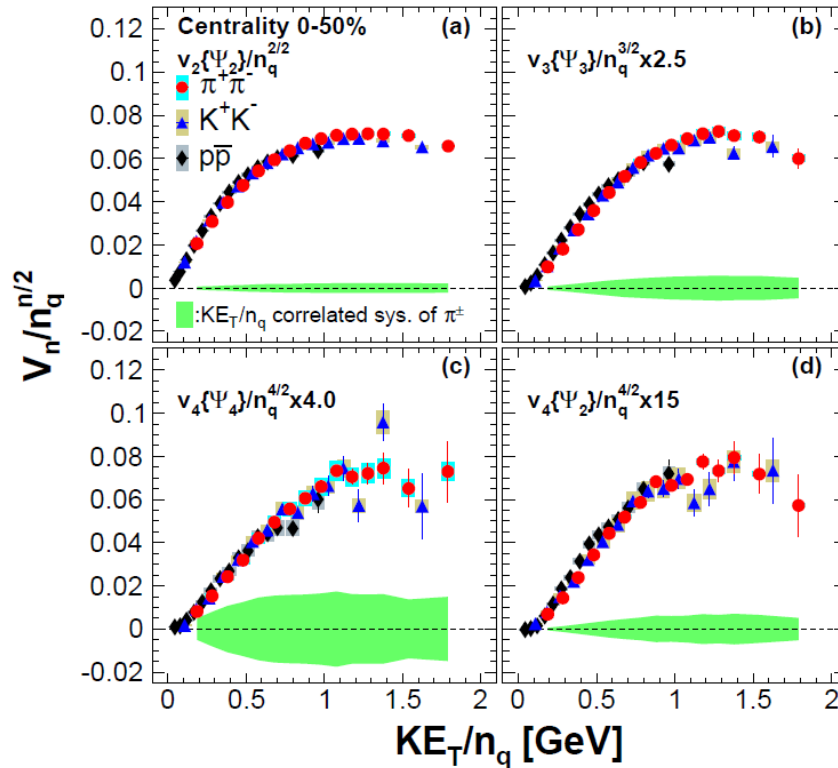
# Constituent quark scaling

Previously observed:

- 1)  $v_n(p_T) \propto (v_2)^{n/2}$
- 2) Quark scaling in the dependence  $v_2/n_q$  vs.  $KE_T/n_q$ , where  $KE_T$  is transverse kinetic energy:

$$KE_T = \sqrt{p_T^2 + m^2} - m$$

Combination of these properties leads to scaling of  $v_n / n_q^{n/2}$  vs.  $KE_T/n_q$



Adare A *et al.* (PHENIX collaboration) 2014 *arXiv:1412.1038*