

# On generalized Melvin solutions for Lie algebras of rank 3

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Generalized Melvin solutions for rank-3 Lie algebras  $A_3$ ,  $B_3$  and  $C_3$  are considered. Any solution contains metric, three Abelian 2-forms and three scalar fields. It is governed by three moduli functions  $H_1(z)$ ,  $H_2(z)$ ,  $H_3(z)$  ( $z = \rho^2$  and  $\rho$  is a radial variable), obeying three differential equations with certain boundary conditions imposed. These functions are polynomials with powers  $(n_1, n_2, n_3) = (3, 4, 3), (6, 10, 6), (5, 8, 9)$  for Lie algebras  $A_3$ ,  $B_3$ ,  $C_3$ , respectively. The solutions depend upon integration constants  $q_1, q_2, q_3 \neq 0$ . The power-law asymptotic relations for polynomials at large  $z$  are governed by integer-valued  $3 \times 3$  matrix  $\nu$ , which coincides with twice the inverse Cartan matrix  $2A^{-1}$  for Lie algebras  $B_3$  and  $C_3$ , while in the  $A_3$  case  $\nu = A^{-1}(I + P)$ , where  $I$  is the identity matrix and  $P$  is a permutation matrix, corresponding to a generator of the  $\mathbb{Z}_2$ -group of symmetry of the Dynkin diagram. The duality identities for polynomials and asymptotic relations for solutions at large distances are obtained. 2-form flux integrals over a 2-dimensional disc of radius  $R$  and corresponding Wilson loop factors over a circle of radius  $R$  are presented.

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