



Study of P-wave B_s^0 states at the CMS experiment

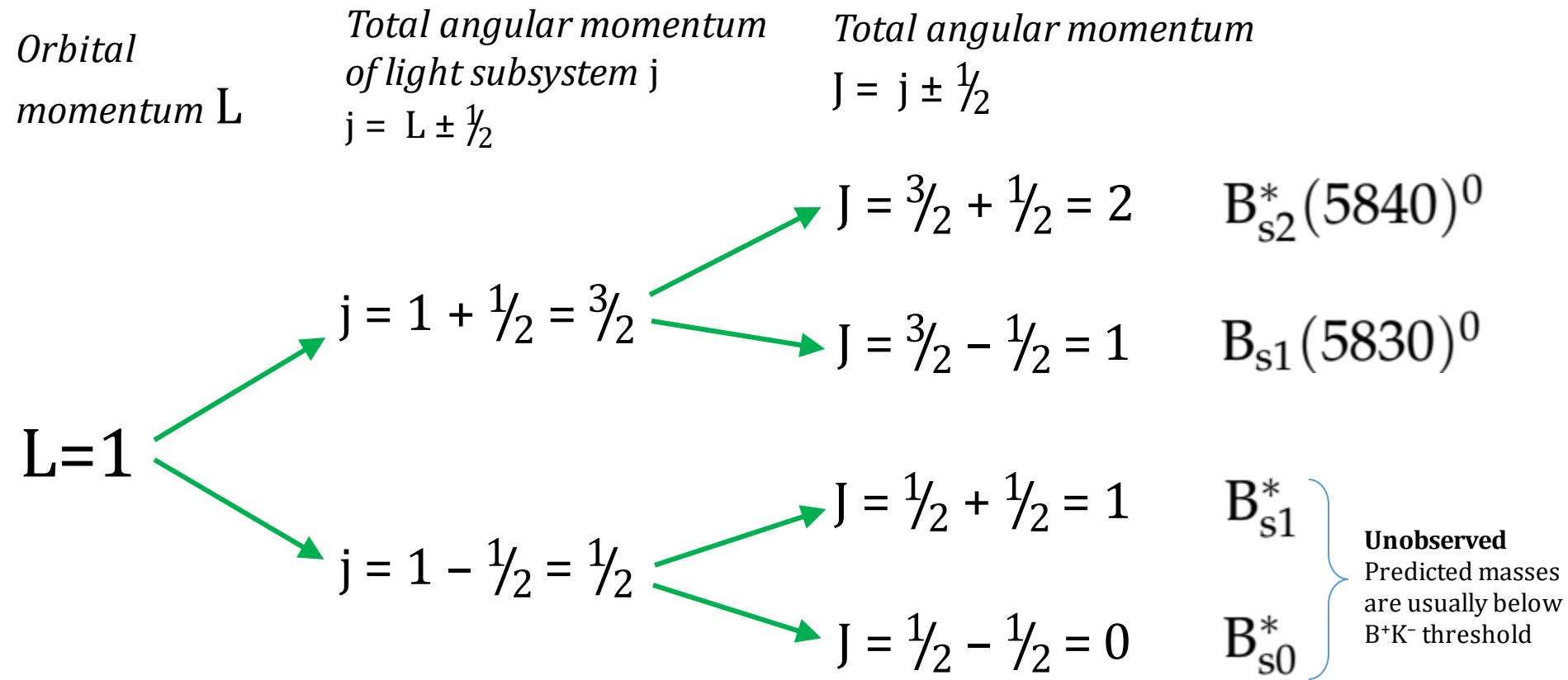
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[CMS-BPH-16-003](#), [arXiv:1809.03578](#)

Submitted to EPJC

Introduction (P-wave B_s^0 states)



The decay $B_{s1} \rightarrow B^+K^-$ corresponds to (in J^P) $1^+ \rightarrow 0^-0^-$ and is forbidden (need $L=1$ to conserve J , but then P is not conserved)

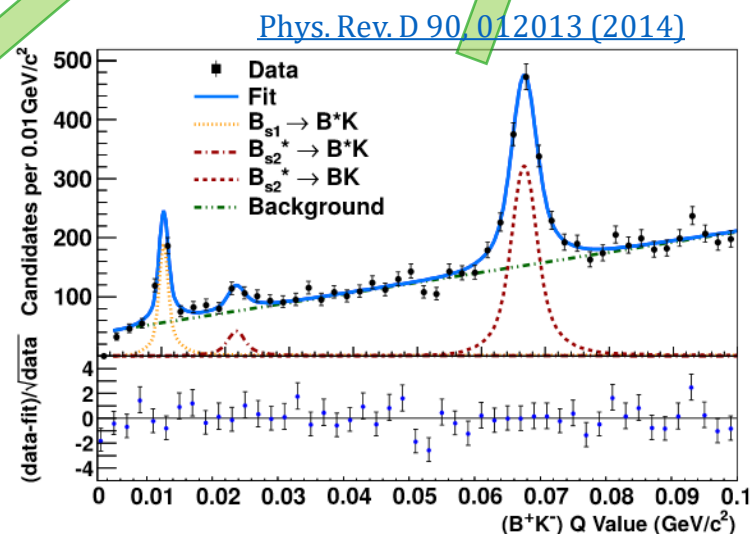
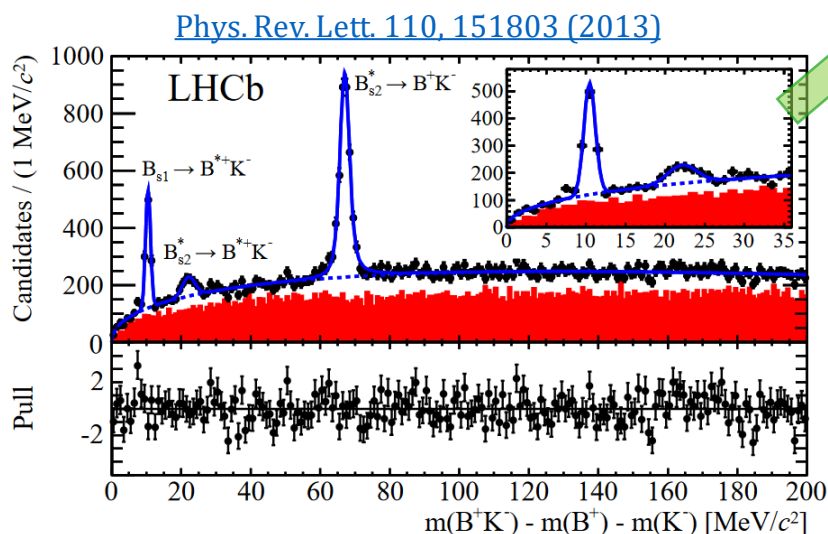
The decay $B_{s1} \rightarrow B^{*+}K^-$ corresponds to (in J^P) $1^+ \rightarrow 1^-0^-$ and $\frac{3}{2}^- \rightarrow \frac{1}{2}^+0^-$ in j^P
 In HQET j^P is also conserved \Rightarrow it cannot proceed in S-wave; but can proceed in D-wave.

Similarly, $B_{s2}^* \rightarrow B^+K^-$ and $B_{s2}^* \rightarrow B^{*+}K^-$ decays are expected to proceed in D-wave.

Introduction (previous results)

P-wave B_s^0 states were observed and studied only by CDF, D0, and LHCb in B^+K^- channel

Result	CDF 2008 [2]	D0 2008 [3]	LHCb 2013 [4]	CDF 2014 [5]
$N(B_{s2}^* \rightarrow B^+K^-)$	95 ± 23	125 ± 25	3140 ± 100	1110 ± 60
$N(B_{s2}^* \rightarrow B^{*+}K^-)$	—	—	307 ± 46	$?? \sim 100$
$N(B_{s1} \rightarrow B^{*+}K^-)$	39 ± 9	25 ± 10	750 ± 36	280 ± 40
$M(B_{s2}^*), \text{ MeV}$	5839.6 ± 0.7	5839.6 ± 1.3	5839.99 ± 0.21	5839.7 ± 0.2
$M(B_{s1}), \text{ MeV}$	5829.4 ± 0.7	—	5828.40 ± 0.41	5828.3 ± 0.5
$M(B_{s2}^*) - M(B^+) - M(K^-), \text{ MeV}$	66.96 ± 0.41	66.7 ± 1.1	67.06 ± 0.12	66.73 ± 0.19
$M(B_{s1}) - M(B^{*+}) - M(K^-), \text{ MeV}$	10.73 ± 0.25	11.5 ± 1.4	10.46 ± 0.06	10.35 ± 0.19
$\Gamma(B_{s2}^*), \text{ MeV}$	—	—	1.56 ± 0.49	1.4 ± 0.4
$\Gamma(B_{s1}), \text{ MeV}$	—	—	—	0.5 ± 0.4



Data and event selection

2012 dataset (19.6 fb^{-1}), trigger optimized to select $B \rightarrow J/\psi \dots$ decays, where $J/\psi \rightarrow \mu^+ \mu^-$

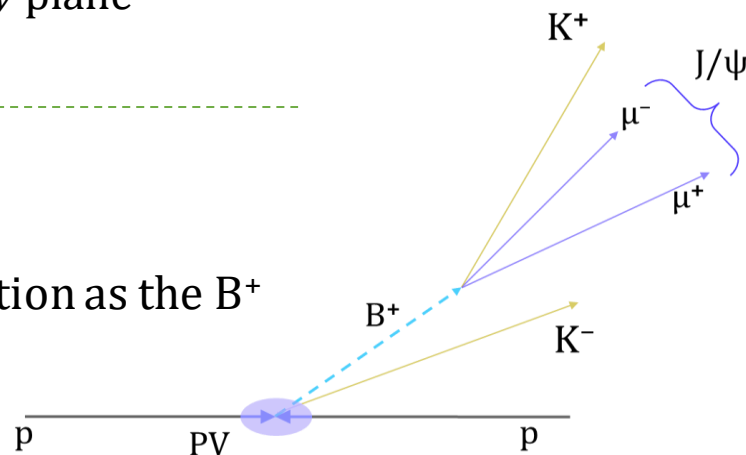
B^+ (B^0) candidates obtained combining J/ψ with 1(2) tracks: $B^+ \rightarrow J/\psi K^+$ and $B^0 \rightarrow J/\psi K^+ \pi^-$

B meson vertex required to be displaced from the PV in the transverse (xy) plane

B meson momentum required to point to the PV in the xy plane

$B^+ K^-$ channel:

Prompt K^- selected to come from the same pp interaction as the B^+



$B^0 K_s^0$ channel:

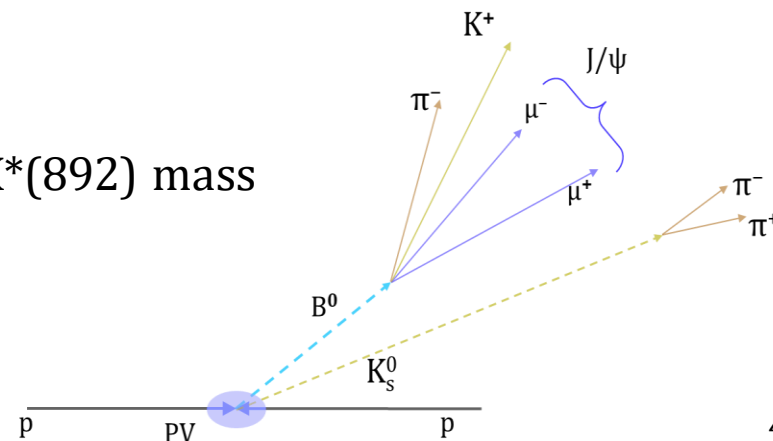
$M(K^+ \pi^-)$ in $\pm 90 \text{ MeV}$ from $K^*(892)$ mass,

$M(K^+ K^-) > 1.035 \text{ GeV}$ to cut out $B_s^0 \rightarrow J/\psi \phi$

K/π mass assignment: chose the candidate closer to $K^*(892)$ mass

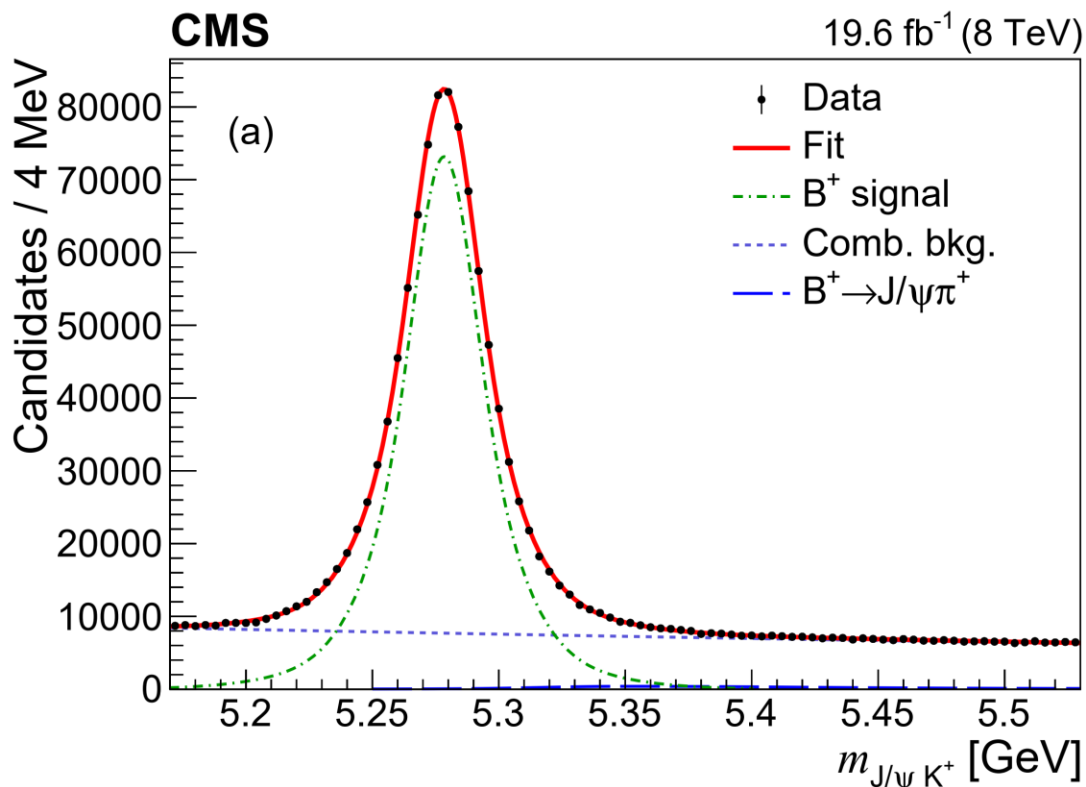
K_s^0 is build from displaced 2-prong vertexes

K_s^0 momentum required to point to PV in the xy plane



more details: see backup

B⁺ invariant mass distribution



Modelled with triple Gaussian function with common mean for signal, exponential for bkg
additional small contribution to account for Cabibbo suppressed B⁺ → J/ψ π⁺ decay

The B⁺ invariant mass resolution is consistent between data and MC

Effective resolution* is about 24 MeV

$$* \sigma_{eff} = \sqrt{f_1 \sigma_1^2 + f_2 \sigma_2^2 + (1 - f_1 - f_2) \sigma_3^2}$$

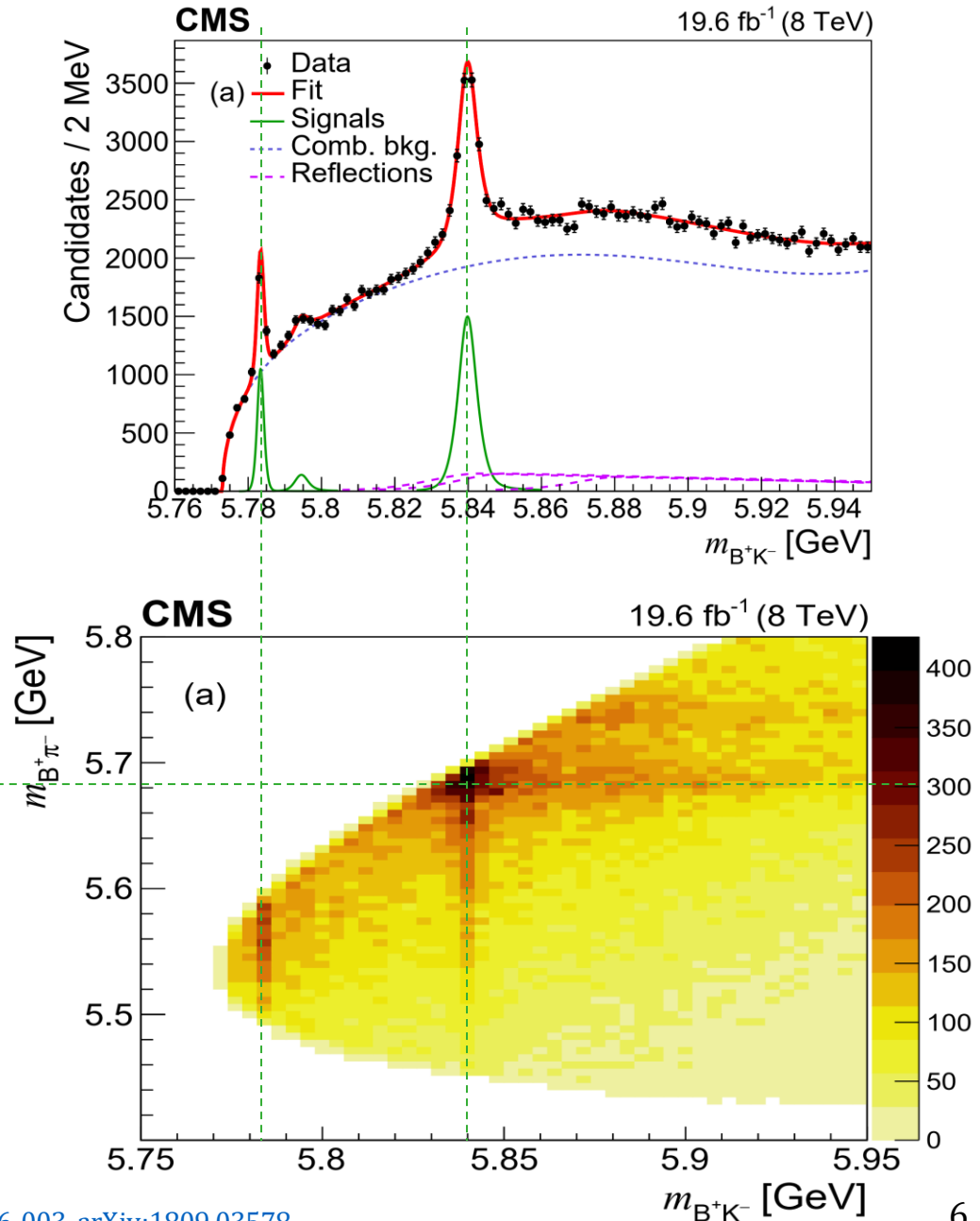
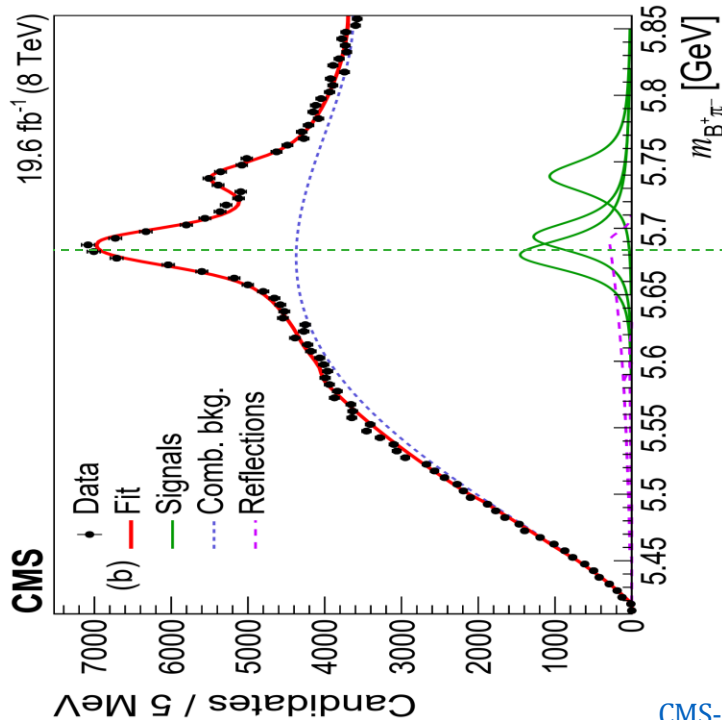
A small difference of ~3% is used in the estimation of the systematic uncertainties

Now combine B⁺ with a track from the same PV →

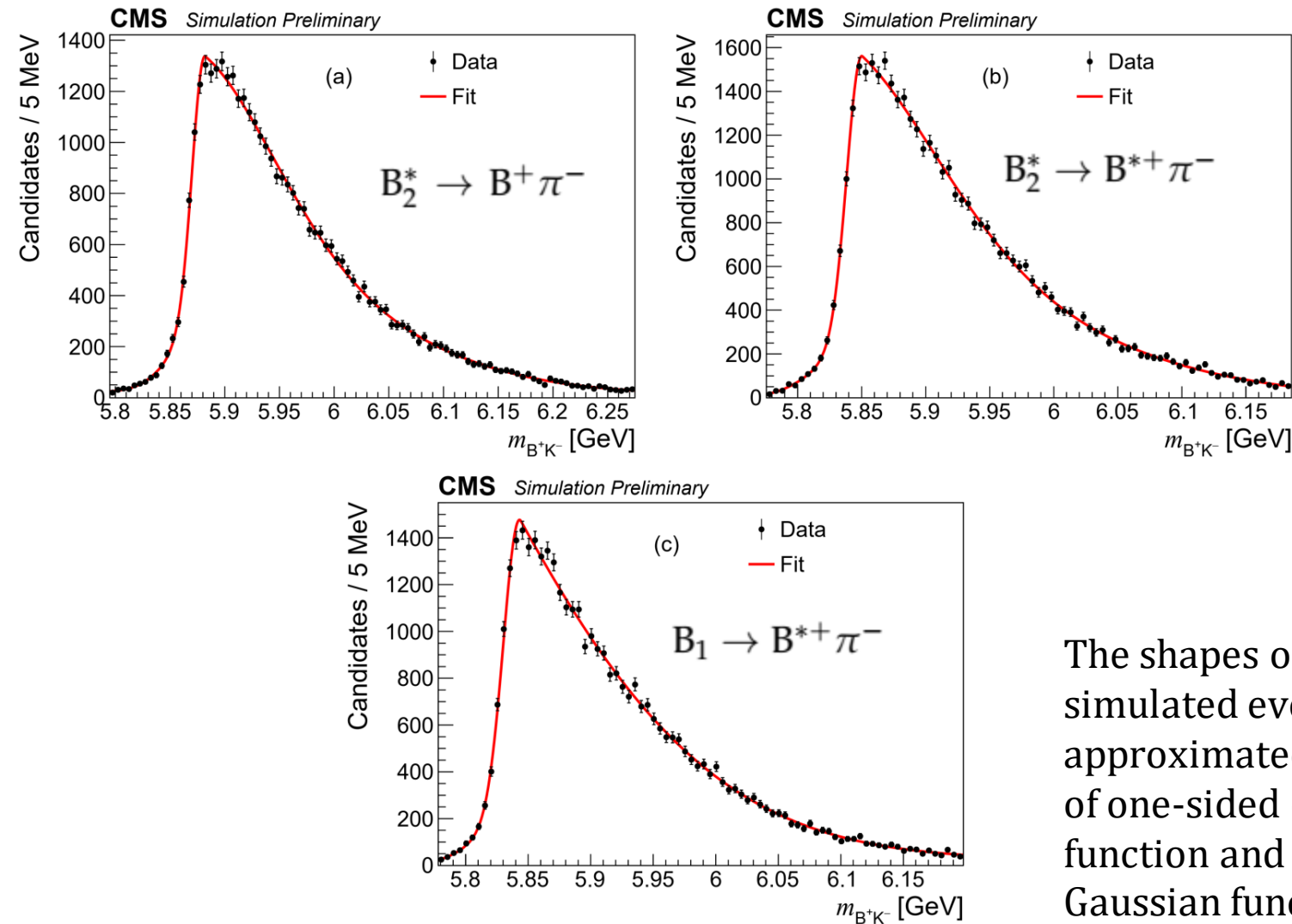
B^+h^- invariant mass distributions

To describe the signal B^+K^- invariant mass distribution, we obtain the yields of reflections from excited B^0 decays using data (fit to $B^+\pi^-$ invariant mass distribution) and their shapes using MC

(see [slide](#) in backup for details)



Shape of reflections from $B^{*0} \rightarrow B^{(*)+} \pi^-$ decays in $B^+ K^-$ invariant mass distribution



The shapes obtained using simulated events are approximated with a product of one-sided double-Gaussian function and sum of two Gaussian functions

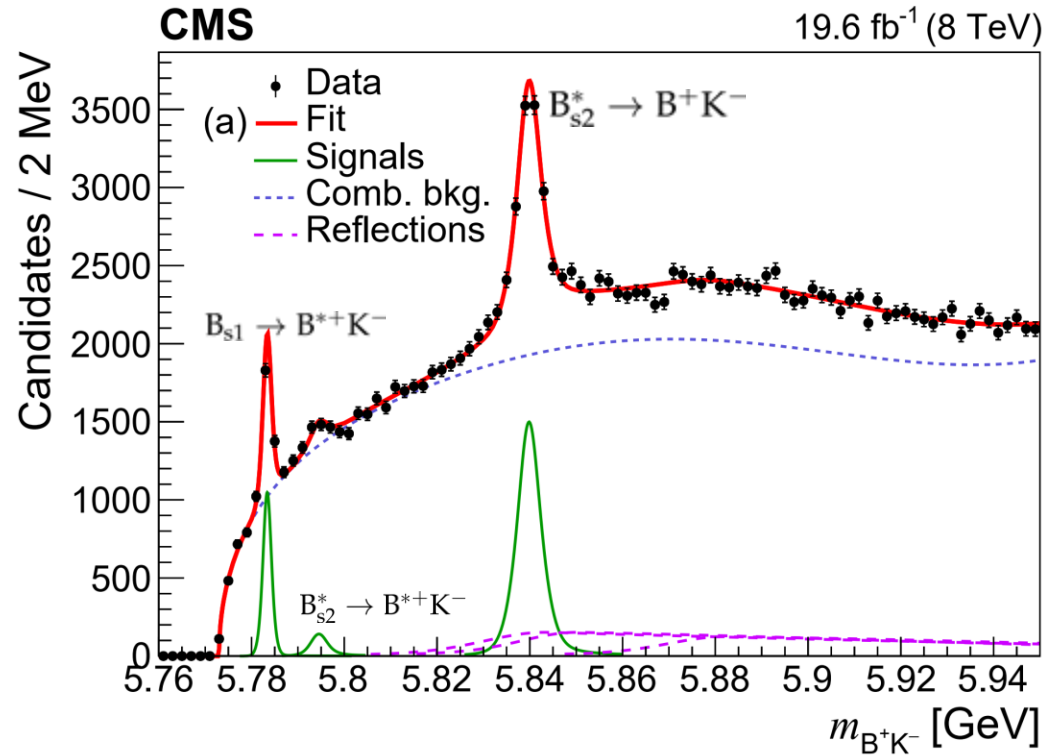
B⁺K⁻ invariant mass distribution

Now we fit B⁺K⁻ invariant mass distribution:

3 D-wave RBW functions convolved with resolutions

+ $(x-x_0)^a \cdot \text{Pol}_6(x)$ for background, x_0 is threshold value

+ contributions from excited B⁰ (shapes fixed to MC, yields fixed to the fit results to the B⁺π⁻ invariant mass distribution)

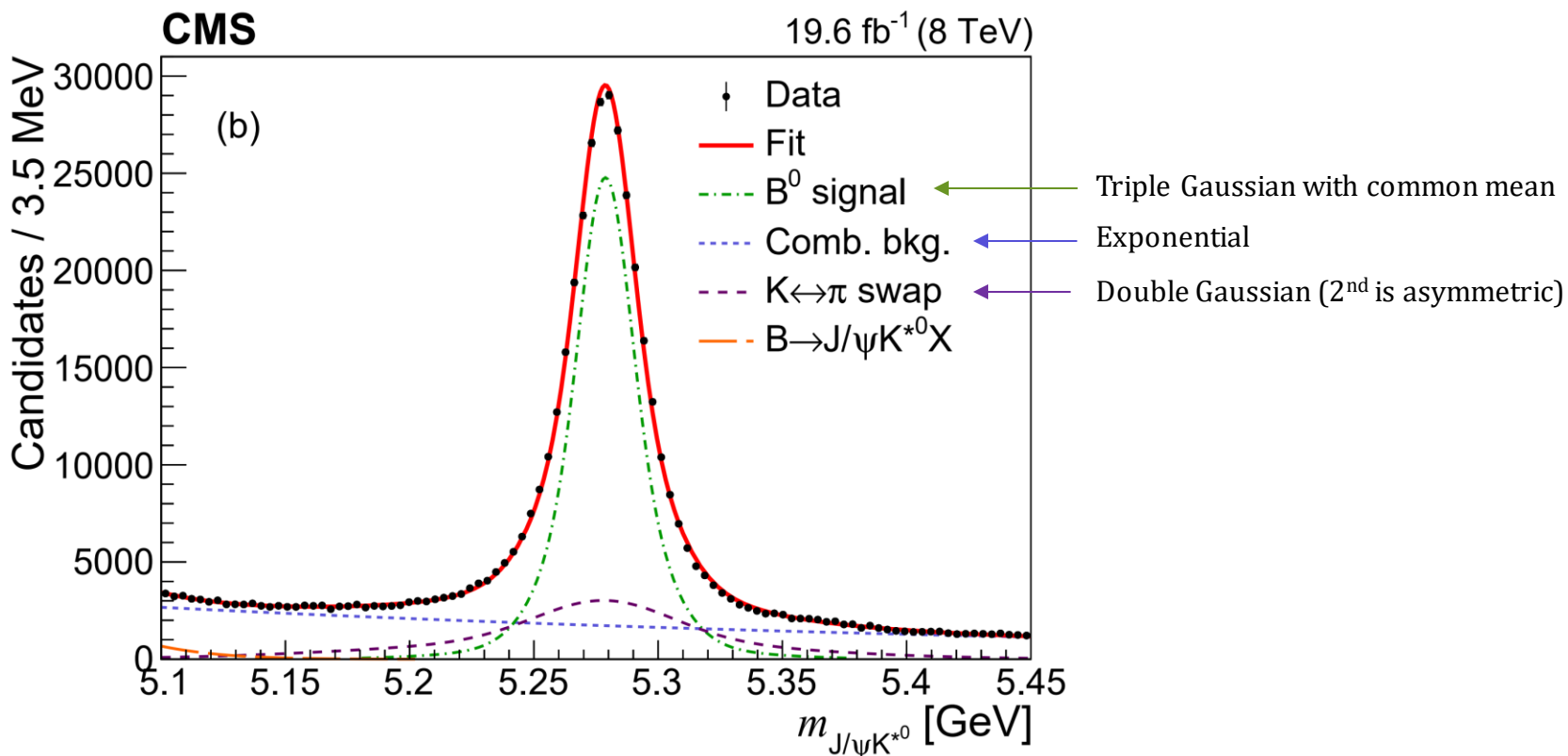


$N(B_{s2}^* \rightarrow BK)$	$N(B_{s2}^* \rightarrow B^*K)$	$N(B_{s1} \rightarrow B^*K)$	$\Gamma(B_{s2}^*), \text{ MeV}$	$\Gamma(B_{s1}), \text{ MeV}$
5424 ± 269	455 ± 119	1329 ± 83	1.52 ± 0.34	0.10 ± 0.15

$M(B_{s2}^*) - M(B) - M(K), \text{ MeV}$	$M(B_{s1}) - M(B^*) - M(K), \text{ MeV}$
66.926 ± 0.093	10.495 ± 0.089

$B^0 K_S^0$ final state

$B^0 \rightarrow J/\psi K^+ \pi^-$ invariant mass distribution



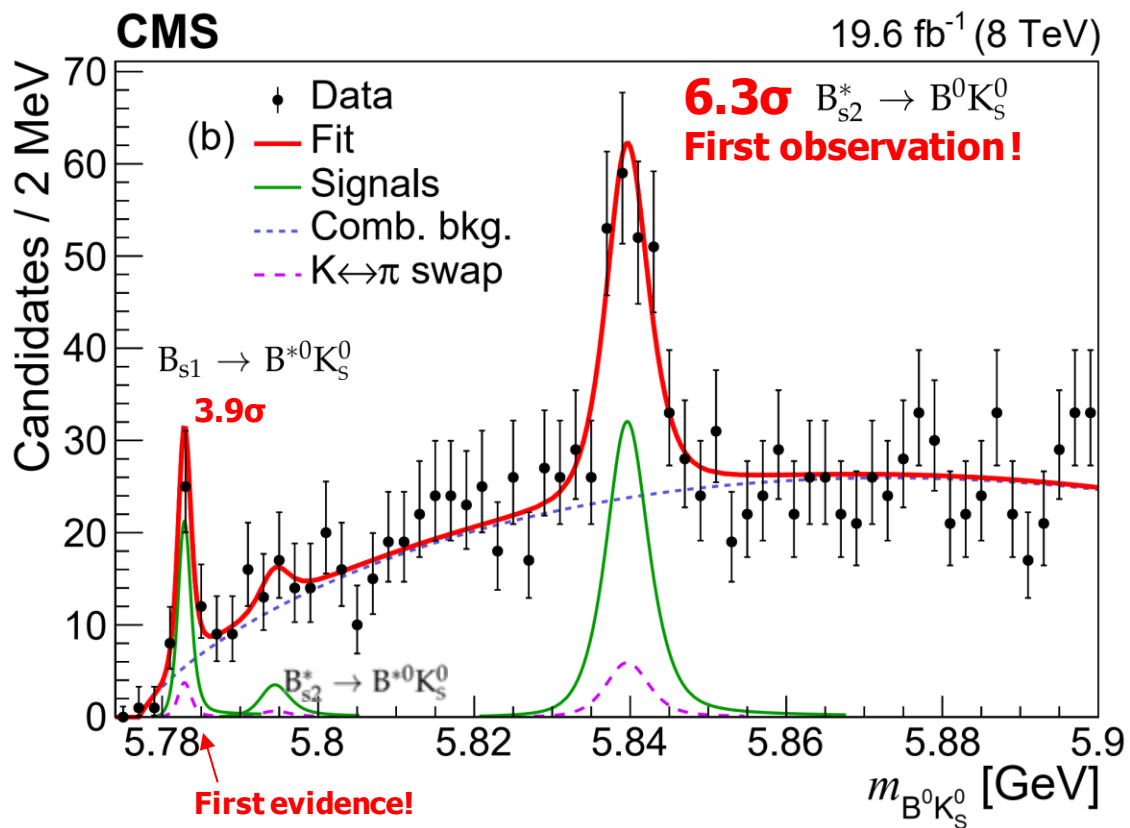
The resolution parameters and the shape of $K \leftrightarrow \pi$ swapped component are fixed from simulation (see backup)

Fraction of swapped component with respect to signal = $(18.9 \pm 3.0)\%$
in the B^0 signal region of $\pm 2\sigma$

$B^0 K_S^0$ invariant mass distribution

Fit:

- 3 D-wave RBW functions convolved with resolutions
- $(x-x_0)^a \cdot \text{Pol}_1(x)$ for bkg, x_0 is threshold value
- 3 contributions from $K \leftrightarrow \pi$ swap (yields fixed relative to signal: $S \cdot 0.189$)



$N(B_{s2}^* \rightarrow BK)$	$N(B_{s2}^* \rightarrow B^* K)$	$N(B_{s1} \rightarrow B^* K)$	$\Gamma(B_{s2}^*), \text{ MeV}$	$\Gamma(B_{s1}), \text{ MeV}$
128 ± 22	12 ± 11	34.5 ± 8.3	2.1 ± 1.3	0.4 ± 0.4
$M(B_{s2}^*) - M(B) - M(K), \text{ MeV}$		$M(B_{s1}) - M(B^*) - M(K), \text{ MeV}$		
62.42 ± 0.48		5.65 ± 0.23		

Measuring BF ratios

Ratio of the signal
yields in data

Ratio of total
efficiencies ~ 16
from MC

$$R_2^{0\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_s^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = \frac{N(B_{s2}^* \rightarrow B^0 K_s^0)}{N(B_{s2}^* \rightarrow B^+ K^-)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s2}^* \rightarrow B^0 K_s^0)} \times$$

$$\times \frac{\mathcal{B}(B^+ \rightarrow J/\psi K^+)}{\mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) \mathcal{B}(K^{*0} \rightarrow K^+ \pi^-) \mathcal{B}(K_s^0 \rightarrow \pi^+ \pi^-)}$$

Known branching fractions from PDG

$$\mathcal{B}(B^+ \rightarrow J/\psi K^+) = (1.026 \pm 0.031) \times 10^{-3}, \mathcal{B}(K_s^0 \rightarrow \pi^+ \pi^-) = (0.6920 \pm 0.0005)$$

$$\mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) = (1.28 \pm 0.05) \times 10^{-3}, \mathcal{B}(K^{*0} \rightarrow K^+ \pi^-) = (0.99754 \pm 0.00021)$$

Formulae and efficiencies ratios for all 6 measured ratios are in backup

Sources of systematic uncertainty

Systematic uncertainties on the branching fraction ratios are related to:

➤ Choice of the fit model

separate uncertainties related to the fits of $B^+\pi^-$, B^+K^- and $B^0K_S^0$ invariant mass distributions;
largest deviation of the results under changes of the fit model is used as systematic uncertainty

➤ Track reconstruction efficiency (3.9% per extra track)

7.8% since 2 more tracks to reconstruct in $B^0K_S^0$ final state

➤ Mass resolution

largest change of the resulting ratios under simultaneous variations of resolution by $\pm 3\%$

➤ Fraction of $K \leftrightarrow \pi$ swapped component

largest change of the resulting ratios under variations of this fraction by $\pm 3\%$

➤ Uncertainty on $m_{B^*} - m_B$

largest change of the resulting ratios under variations of $m_{B^*} - m_B$ by \pm PDG uncertainty

➤ Non- K^* contribution in $B^0 \rightarrow J/\psi K^+ \pi^-$ decay

estimated by fitting background-subtracted $K^+ \pi^-$ invariant mass distribution

➤ Finite size of the simulation samples

uncertainties from the previous slide

Next slide shows these uncertainties and the total systematic uncertainties for the 6 measured ratios

Results

Uncertainties here are, respectively, statistical, systematic, related to PDG uncertainties

Theory: 0.43
[arXiv:1202.1224](https://arxiv.org/abs/1202.1224),
[arXiv:1607.02812](https://arxiv.org/abs/1607.02812)

new $R_2^{0\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.432 \pm 0.077 \pm 0.075 \pm 0.021,$

new $R_1^{0\pm} = \frac{\mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)} = 0.49 \pm 0.12 \pm 0.07 \pm 0.02,$ **Theory: 0.23**
[arXiv:1202.1224](https://arxiv.org/abs/1202.1224), 2.5σ

$R_{2*}^{\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*+} K^-)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.081 \pm 0.021 \pm 0.015,$ **LHCb** $0.093 \pm 0.013 \pm 0.012$
CDF $0.10 \pm 0.03 \pm 0.02$

new $R_{2*}^0 = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)} = 0.093 \pm 0.086 \pm 0.014.$

$R_{\sigma}^{\pm} = \frac{\sigma(pp \rightarrow B_{s1} X) \mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}{\sigma(pp \rightarrow B_{s2}^* X) \mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.233 \pm 0.019 \pm 0.018,$ **LHCb** $0.232 \pm 0.014 \pm 0.013$

new $R_{\sigma}^0 = \frac{\sigma(pp \rightarrow B_{s1} X) \mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\sigma(pp \rightarrow B_{s2}^* X) \mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)} = 0.266 \pm 0.079 \pm 0.063.$

Results are in agreement with existing measurements of LHCb and CDF

CMS 2018: [CMS-BPH-16-003](https://arxiv.org/abs/1809.03578), [arXiv:1809.03578](https://arxiv.org/abs/1809.03578)

LHCb 2013: [doi:10.1103/PhysRevLett.110.151803](https://doi.org/10.1103/PhysRevLett.110.151803)

CDF 2014: [doi:10.1103/PhysRevD.90.012013](https://doi.org/10.1103/PhysRevD.90.012013)

Results

$$\Delta M_{B_{s2}^*}^{\pm} = M(B_{s2}^*) - M_{B^+}^{\text{PDG}} - M_{K^-}^{\text{PDG}} = 66.87 \pm 0.09 \pm 0.07 \text{ MeV},$$



$$\Delta M_{B_{s2}^*}^0 = M(B_{s2}^*) - M_{B^0}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}} = 62.37 \pm 0.48 \pm 0.07 \text{ MeV},$$

$$\Delta M_{B_{s1}}^{\pm} = M(B_{s1}) - M_{B^{*+}}^{\text{PDG}} - M_{K^-}^{\text{PDG}} = 10.45 \pm 0.09 \pm 0.06 \text{ MeV},$$



$$\Delta M_{B_{s1}}^0 = M(B_{s1}) - M_{B^{*0}}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}} = 5.61 \pm 0.23 \pm 0.06 \text{ MeV}.$$

$$\Gamma_{B_{s2}^*} = 1.52 \pm 0.34 \pm 0.30 \text{ MeV}$$

Comparison to previous measurements

	$M(B_{s2}^*) - M(B^+) - M(K^-)$	$M(B_{s1}) - M(B^{*+}) - M(K^-)$	$\Gamma(B_{s2}^*)$
LHCb	67.06 ± 0.12	10.46 ± 0.06	1.56 ± 0.49
CDF	67.73 ± 0.19	10.35 ± 0.19	1.4 ± 0.44
CMS	66.87 ± 0.12	10.45 ± 0.11	1.52 ± 0.43

2nd and 3rd column are consistent with existing measurements of LHCb and CDF

Measurement of $M(B_{s2}^*) - M(B^+) - M(K^-)$ agrees with LHCb, not with CDF

CMS 2018: [CMS-BPH-16-003](#), [arXiv:1809.03578](#)


LHCb 2013: [doi:10.1103/PhysRevLett.110.151803](#)

CDF 2014: [doi:10.1103/PhysRevD.90.012013](#)

Results

We also measure the mass differences between neutral and charged $B^{(*)}$ mesons:

$$M_{B^0} - M_{B^+} = 0.57 \pm 0.49 \pm 0.10 \pm 0.02 \text{ MeV}$$


$$M_{B^{*0}} - M_{B^{*+}} = 0.91 \pm 0.24 \pm 0.09 \pm 0.02 \text{ MeV}$$

The first mass difference is known with much better precision: $(0.31 \pm 0.06) \text{ MeV}$ [PDG] while there are no measurements for the second one.

We present a new method to measure these mass differences!
It may become very precise with more data

Summary

First observation (6.3σ) of the $B_{s2}^* \rightarrow B^0 K_S^0$ decay

First evidence (3.9σ) for the $B_{s1} \rightarrow B^{*0} K_S^0$ decay

Measure 4 BF ratios $\frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)}, \frac{\mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}, \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*+} K^-)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)}, \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}$

Measure 2 BF x σ ratios $\frac{\sigma(pp \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}{\sigma(pp \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)}, \frac{\sigma(pp \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\sigma(pp \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}$

Measure 6 mass differences and the B_{s2}^* natural width

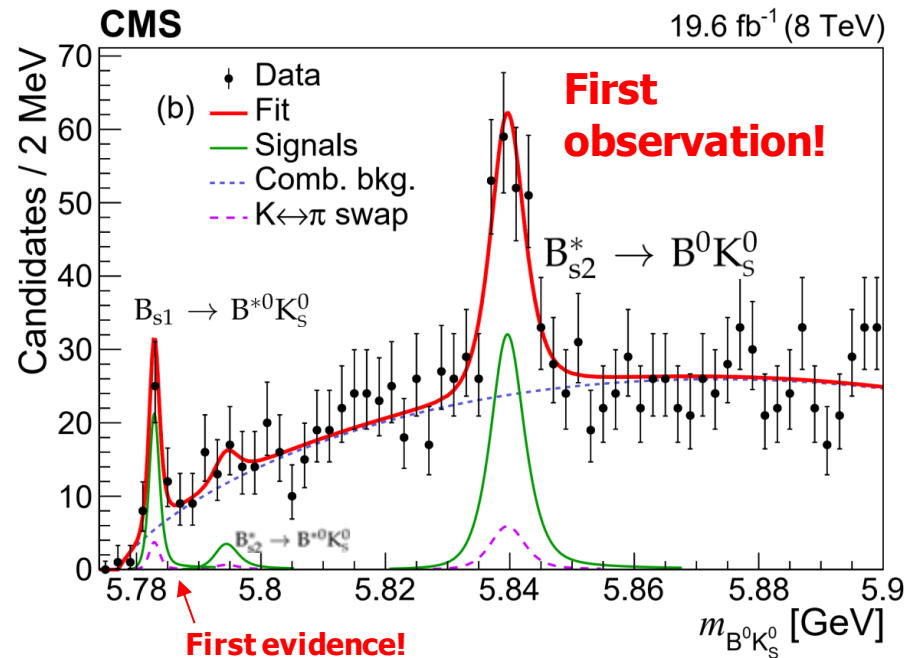
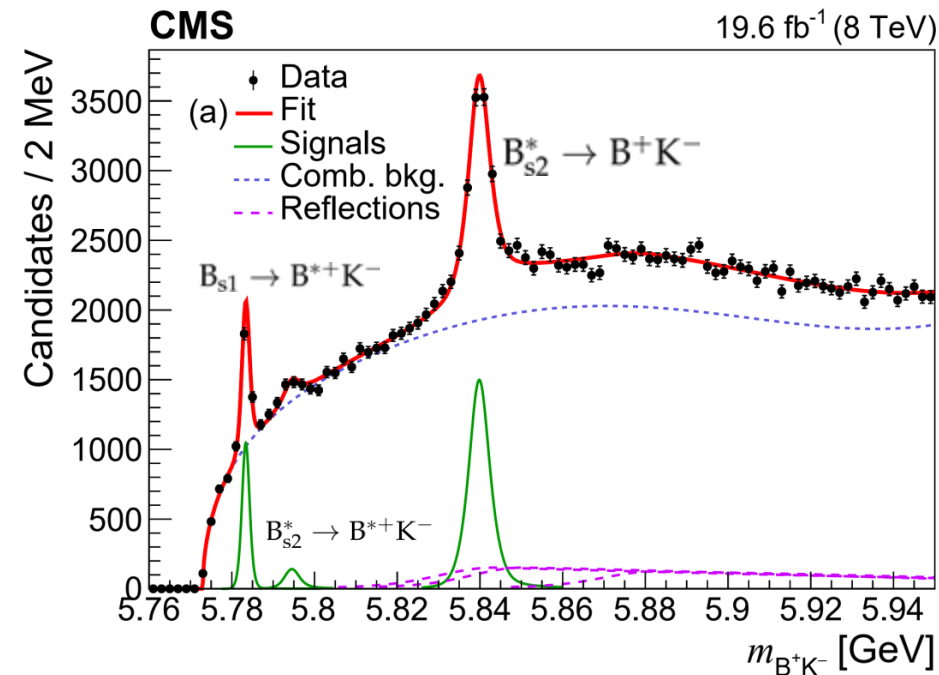
- $M(B_{s2}^*) - M(B^+) - M(K^-)$
- $M(B_{s1}) - M(B^{*+}) - M(K^-)$
- $M(B_{s2}^*) - M(B^0) - M(K_S^0)$ (*first measurement*)
- $M(B_{s1}) - M(B^{*0}) - M(K_S^0)$ (*first measurement*)
- $M(B^{*+}) - M(B^+)$
- $M(B^{*0}) - M(B^0)$ (*first measurement*)
- $\Gamma(B_{s2}^*)$

We also report the mass measurements $M(B_{s2}^*)$ and $M(B_{s1})$ (*in backup*)

The results are in agreement with previous measurements, if they exist

Thank you !

Overview



Final state	$N(B_{s2}^* \rightarrow BK)$	$N(B_{s2}^* \rightarrow B^*K)$	$N(B_{s1} \rightarrow B^*K)$
B^+K^-	5424 ± 269	455 ± 119	1329 ± 83
$B^0K_s^0$	128 ± 22	12 ± 11	34.5 ± 8.3

B^+ is reconstructed in $J/\psi K^+$ channel

B^0 is reconstructed in $J/\psi K^+\pi^-$ channel

“Reflections”:

From $B^{**} \rightarrow B^{(*)+}\pi^-$ in B^+K^- channel, yields fixed from the fit to $B^+\pi^-$ invariant mass;

From $K \leftrightarrow \pi$ swap in $B^0K_s^0$ channel, yields fixed relative to the signal yields

We also measure masses, mass differences and $\Gamma(B_{s2}^*)$ in these decays

Summary of all reported measurements

$$R_2^{0\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_s^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.432 \pm 0.077 \text{ (stat)} \pm 0.075 \text{ (syst)} \pm 0.021 \text{ (PDG)}$$

$$R_1^{0\pm} = \frac{\mathcal{B}(B_{s1} \rightarrow B^{*0} K_s^0)}{\mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)} = 0.492 \pm 0.122 \text{ (stat)} \pm 0.068 \text{ (syst)} \pm 0.024 \text{ (PDG)}$$

$$R_{2*}^{\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*+} K^-)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.081 \pm 0.021 \text{ (stat)} \pm 0.015 \text{ (syst)},$$

$$R_{2*}^0 = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*0} K_s^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_s^0)} = 0.093 \pm 0.086 \text{ (stat)} \pm 0.014 \text{ (syst)},$$

$$R_{\sigma}^{\pm} = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = 0.233 \pm 0.019 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

$$R_{\sigma}^0 = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*0} K_s^0)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^0 K_s^0)} = 0.266 \pm 0.079 \text{ (stat)} \pm 0.063 \text{ (syst)}$$

$$\Delta M_{B_{s2}^*}^{\pm} = M(B_{s2}^*) - M(B^+) - M(K^-) = 66.870 \pm 0.093 \text{ (stat)} \pm 0.073 \text{ (syst)} \text{ MeV},$$

$$\Delta M_{B_{s2}^*}^0 = M(B_{s2}^*) - M(B^0) - M(K_s^0) = 62.37 \pm 0.48 \text{ (stat)} \pm 0.07 \text{ (syst)} \text{ MeV},$$

$$\Delta M_{B_{s1}}^{\pm} = M(B_{s1}) - M(B^{*+}) - M(K^-) = 10.452 \pm 0.089 \text{ (stat)} \pm 0.063 \text{ (syst)} \text{ MeV},$$

$$\Delta M_{B_{s1}}^0 = M(B_{s1}) - M(B^{*0}) - M(K_s^0) = 5.61 \pm 0.23 \text{ (stat)} \pm 0.06 \text{ (syst)} \text{ MeV},$$

$$M(B_{s2}^*) = 5839.86 \pm 0.09 \pm 0.07 \pm 0.15 \text{ MeV}$$

$$M(B_{s1}) = 5828.78 \pm 0.09 \pm 0.06 \pm 0.28 \text{ MeV}$$

$$m_{B^0} - m_{B^+} = 0.57 \pm 0.49 \text{ (stat)} \pm 0.10 \text{ (syst)} \pm 0.02 \text{ (PDG)} \text{ MeV}$$

$$m_{B^{*0}} - m_{B^{*+}} = 0.91 \pm 0.24 \text{ (stat)} \pm 0.09 \text{ (syst)} \pm 0.02 \text{ (PDG)} \text{ MeV}$$

$$\Gamma(B_{s2}^*) = 1.52 \pm 0.34 \text{ (stat)} \pm 0.30 \text{ (syst)} \text{ MeV}$$

Highlighted in
yellow are the first
measurements

BACKUP

$B^+\pi^-$ invariant mass distribution

To obtain yields of these reflections,
we fit $B^+\pi^-$ invariant mass distribution:

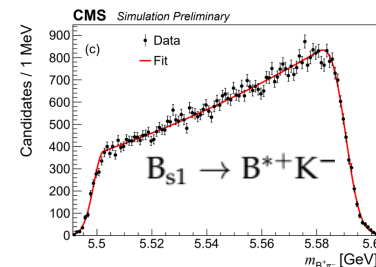
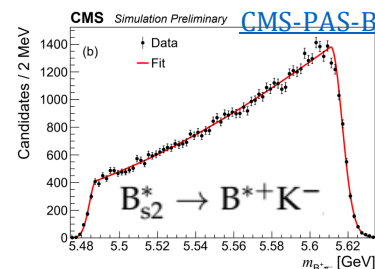
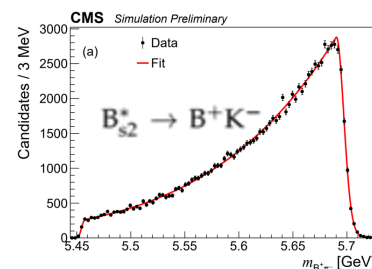
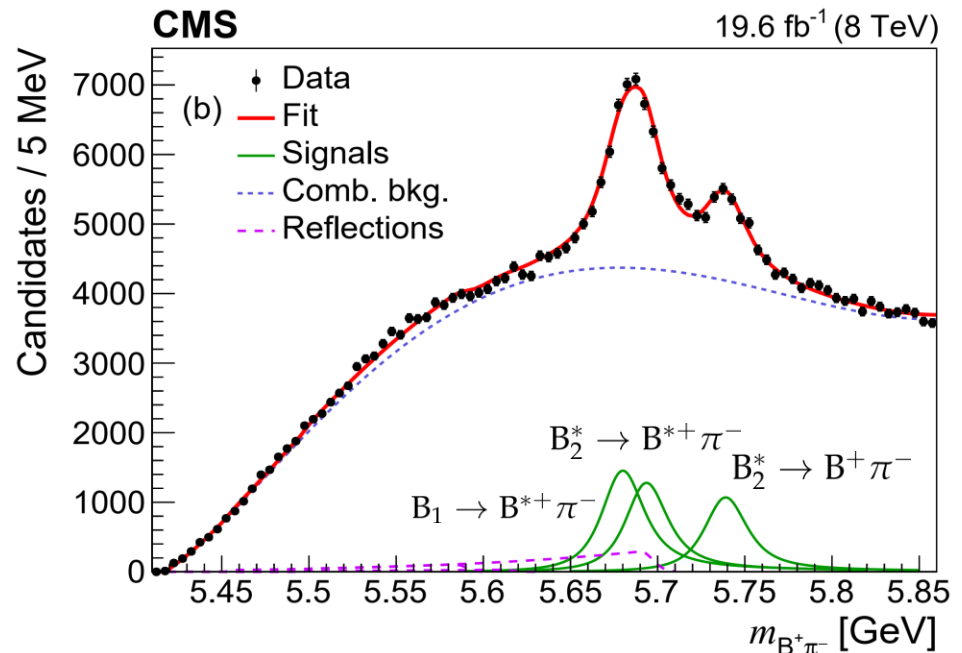
3 D-wave RBW functions convolved
with resolutions (*from MC*)

+ $(x-x_0)^a \bullet \text{Pol}_m(x)$ for background,
 x_0 is threshold value, $\text{Pol}_m(x)$ is polynomial of degree m

+ (small) contributions from $B_{s1,2}^{(*)}$

In the baseline fit, masses and natural
widths of excited B^0 states are fixed to PDG

The fit returns yields of about
8500, 10500 and 12000 events for the
 $B_2^{*+} \rightarrow B^+\pi^-$, $B_2^{*+} \rightarrow B^{*+}\pi^-$, and $B_1^{*+} \rightarrow B^+\pi^-$ decays,
respectively



*Shapes from
simulation*

Data and event selection

Common selection for B^+ and B^0

2012 dataset (19.6 fb^{-1}), trigger optimized to select $B \rightarrow J/\psi \dots$ decays

Muons matched to trigger; $p_T(\mu^\pm) > 3.5 \text{ GeV}/c$, $|\eta(\mu^\pm)| < 2.2$

Standard CMS “high purity” tracks, $p_T > 1 \text{ GeV}$

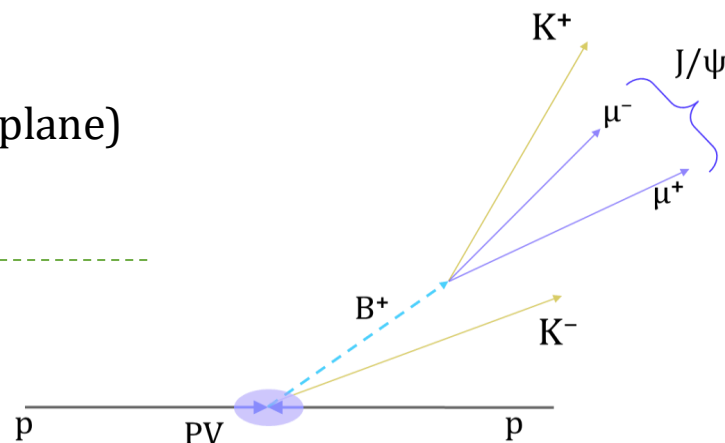
$P_{\text{vtx}}(B) > 1\%$

PV is chosen as the one with best pointing angle

$L_{xy}/\sigma_{Lxy}(B) > 5.0$

$\cos\alpha_{xy} > 0.99$ (B momentum points to PV in xy plane)

B mass in $\sim \pm 2\sigma_{\text{eff}}$ from PDG



B^+K^- channel: K^- is chosen from PV track collection

$B^0K_S^0$ channel:

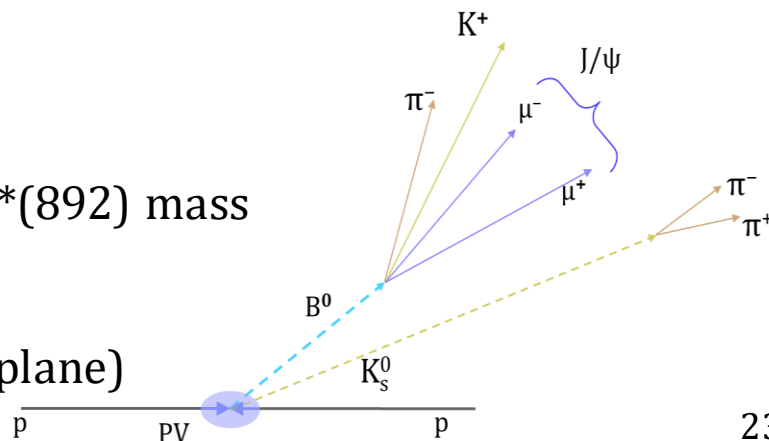
$M(K^+\pi^-)$ in $\pm 90 \text{ MeV}$ from $K^*(892)$ mass,

$M(K^+, K^-) > 1.035 \text{ GeV}$ to cut out $B_s^0 \rightarrow J/\psi \phi$

K/π mass assignment: chose the candidate closer to $K^*(892)$ mass

K_S^0 is build from displaced 2-prong vertices

$\cos\alpha_{xy} > 0.999$ (K_S^0 momentum points to PV in xy plane)



B^+K^- signal extraction logic

Fit to $B^{*0} \rightarrow B^+\pi^-$ MC samples to obtain signal resolutions

Fit to $B_{s1,2}^{(*)} \rightarrow B^+K^-$ MC samples to obtain reflection shapes (if reconstructed as $B^+\pi^-$)

Fit to $B^{*0} \rightarrow B^+\pi^-$ MC samples to obtain reflection shapes (if reconstructed as B^+K^-)

Fit to $B_{s1,2}^{(*)} \rightarrow B^+K^-$ MC samples to obtain signal resolutions

Fit to $B^+\pi^-$ invariant mass distribution in data, with signal resolutions from MC and fixed shapes of reflections from $B_{s1,2}^{(*)} \rightarrow B^+K^-$

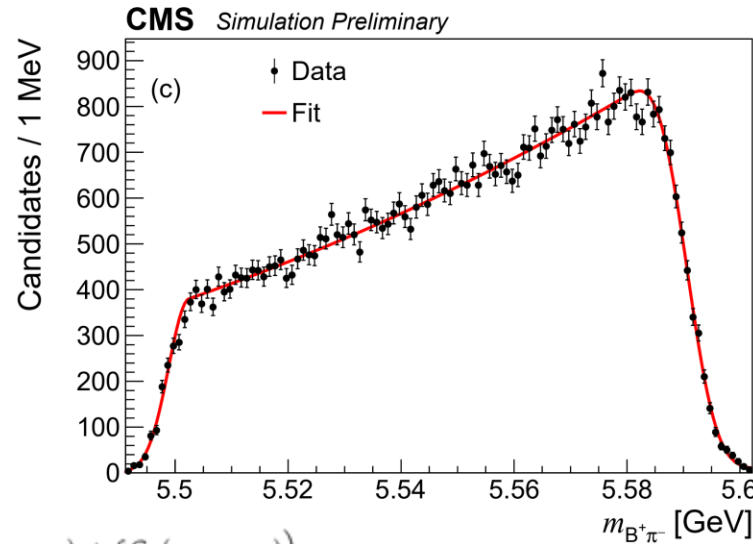
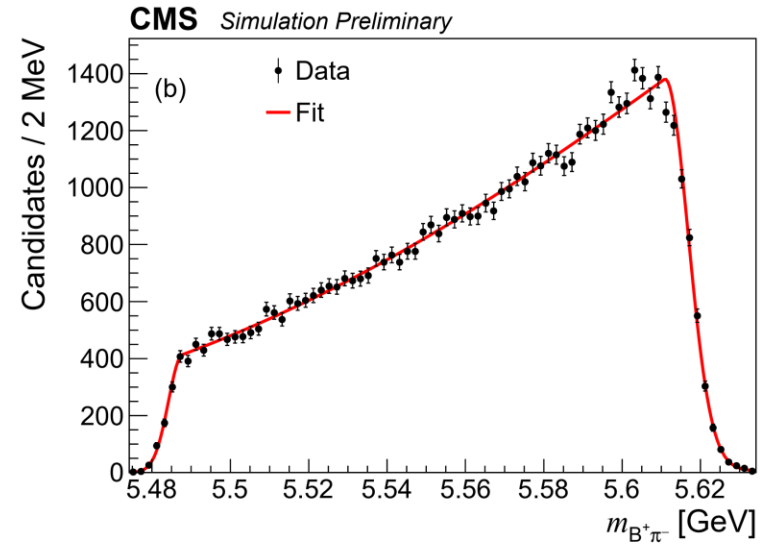
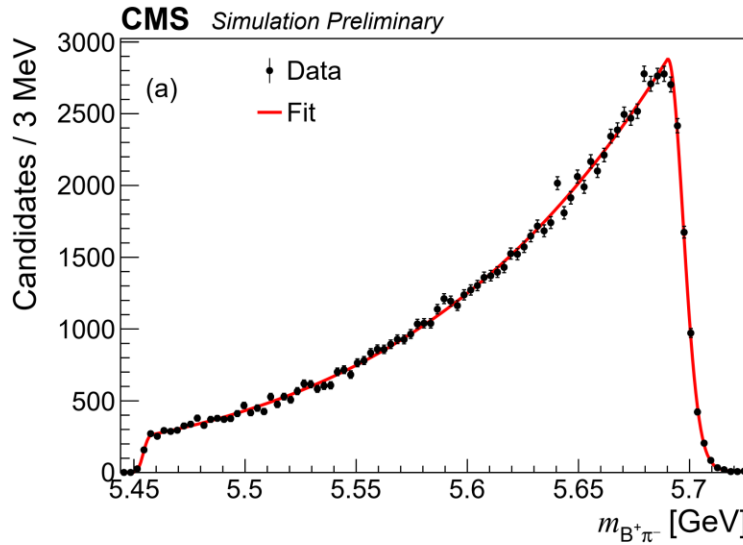
Yields of $B^{*0} \rightarrow B^+\pi^-$ contributions

Fit to B^+K^- distribution in data, with

- reflections from B^{*0} shapes and yields fixed
- Signal resolutions fixed to MC

Signal yields, mass differences, Γ

The shapes of reflections from $B_{s1,2}^0$ decays in $B^+\pi^-$ invariant mass



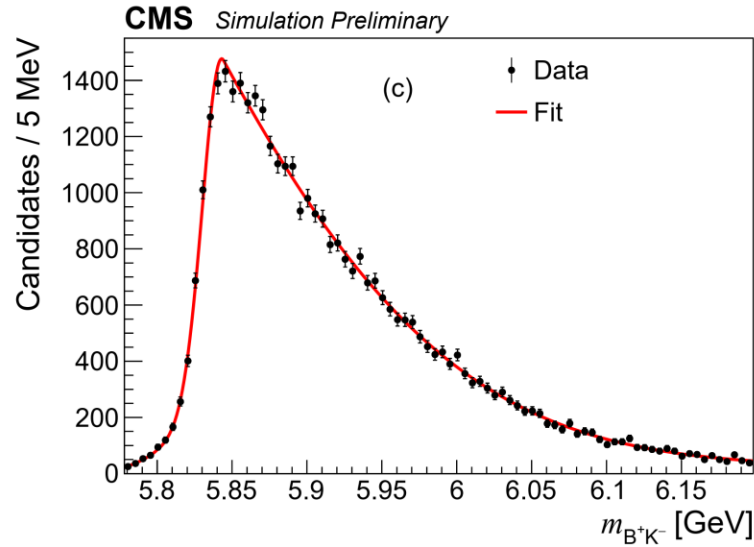
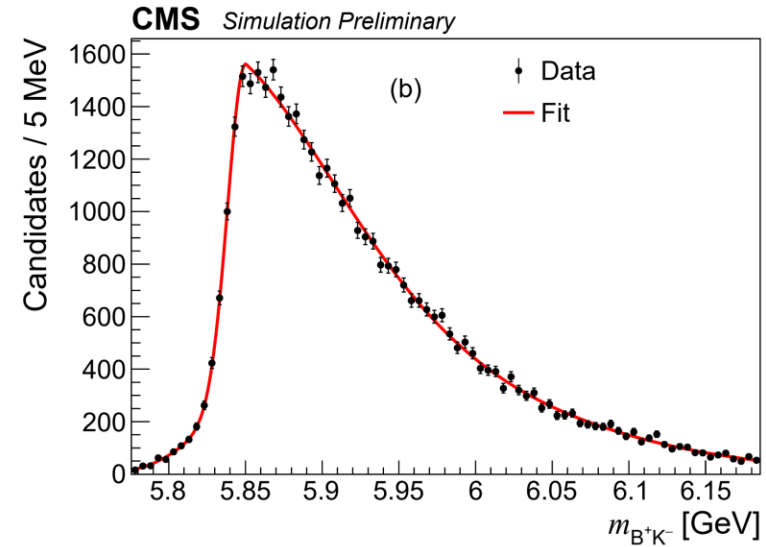
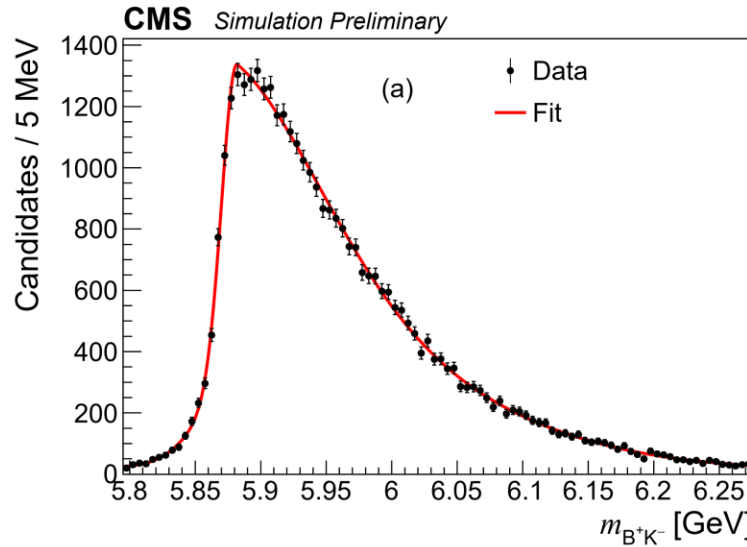
Product of a Gaussian function and 1-sided Gaussian function

$$F(x; \dots) = G_L(x; m_L, \sigma_L) * \exp\left(-\frac{(x - m_c)^2}{2\sigma_c^2}\right) * \left((1 - f) G_R(x; m_R, \sigma_{R1}) + f G_R(x; m_R, \sigma_{R2})\right)$$

$$\text{where } G_L(x; m, \sigma) = \begin{cases} \exp\left(-\frac{1}{2} \left(\frac{x-m}{\sigma}\right)^{\lambda_L}\right) & \text{if } x \leq m \\ 1 & \text{if } x \geq m \end{cases}$$

$$\text{and } G_R(x; m, \sigma) = \begin{cases} 1 & \text{if } x \leq m \\ \exp\left(-\frac{1}{2} \left(\frac{x-m}{\sigma}\right)^{\lambda_R}\right) & \text{if } x \geq m \end{cases}$$

The shapes of reflections from B^0 decays in B^+K^- invariant mass



Product of a double-Gaussian function and double 1-sided Gaussian function

$$F(x; \sigma_{01}, \sigma_{02}, m_0, \sigma_1, m_1, \sigma_2, m_2, f, \phi) = G(x; \dots) * \left(\exp\left(-\frac{(x - m_1)^2}{2\sigma_1^2}\right) + f * \exp\left(-\frac{(x - m_2)^2}{2\sigma_2^2}\right) \right)$$

$$\text{where } G(x; \sigma_{01}, \sigma_{02}, \phi, m_0) = \begin{cases} (1 - \phi) \exp\left(-\frac{(x - m_0)^2}{2\sigma_{01}^2}\right) + \phi \exp\left(-\frac{(x - m_0)^2}{2\sigma_{02}^2}\right) & \text{if } x < m_0 \\ 1 & \text{if } x > m_0 \end{cases}$$

B^0 invariant mass distribution (MC)

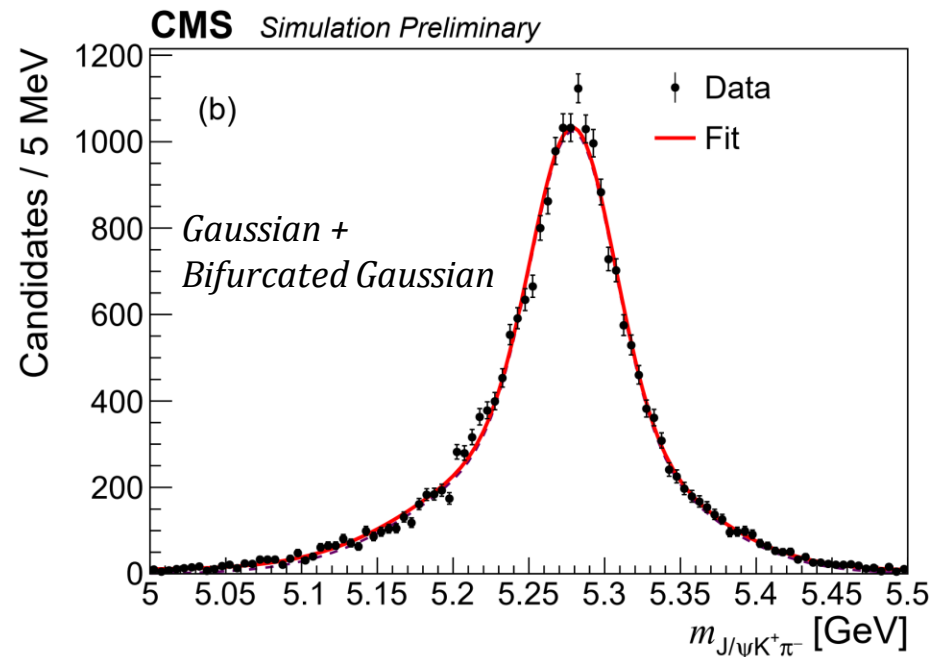
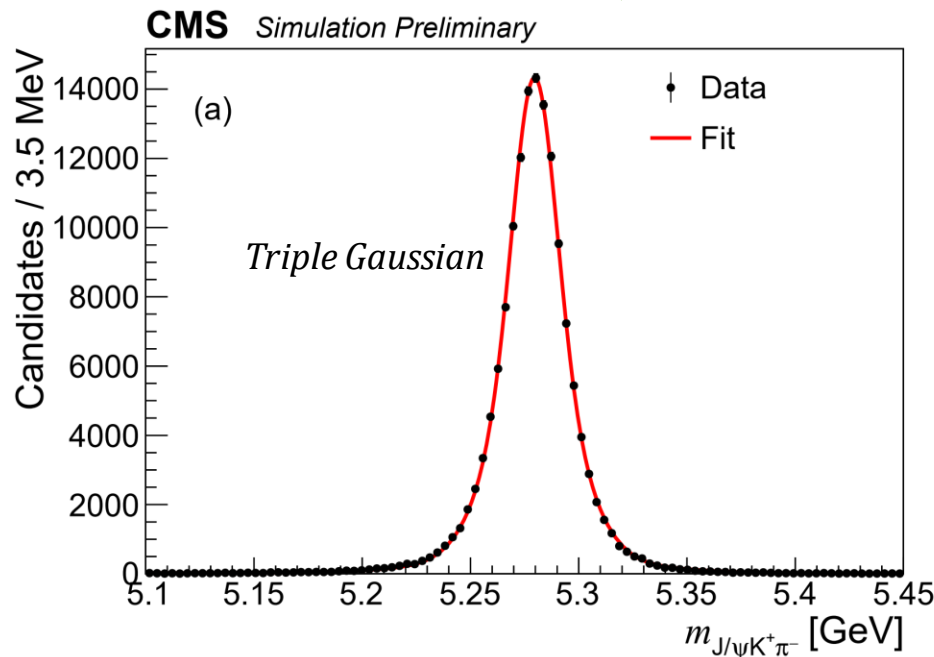
B^0 is reconstructed in the decay to $J/\psi K^+ \pi^-$, where kaon and pion can be misidentified (swapped) in the reconstruction. The selection requirements are

$M(K^+ \pi^-)$ in ± 90 MeV from $K^*(892)$ mass,

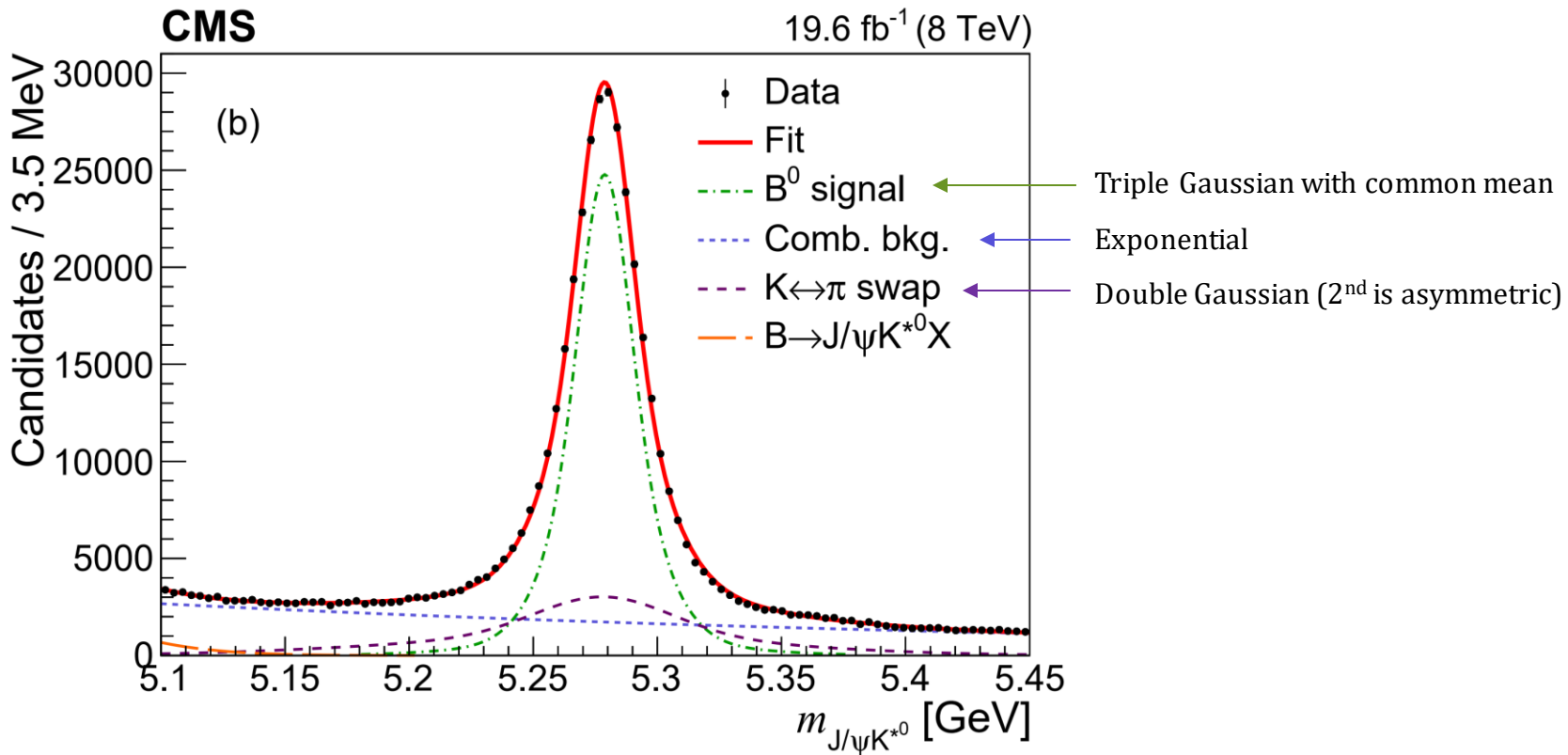
$M(K^+, K^-) > 1.035$ GeV to cut out $B_s^0 \rightarrow J/\psi \phi$, as in P5' analysis

K/π mass assignment: as in P5', chose the candidate closer to $K^*(892)$ mass

We use MC to obtain the signal resolution and shape of $K \leftrightarrow \pi$ swapped component:



B^0 invariant mass distribution



The resolution parameters and the shape of $K \leftrightarrow \pi$ swapped component are fixed from simulation (see backup)

The B^0 signal region [5245, 5313] MeV includes ~ 220000 signal candidates and ~ 41000 $K \leftrightarrow \pi$ swap candidates \Rightarrow “fraction of swapped component w.r.t. signal” = $(18.9 \pm 0.3)\%$

Vary the signal resolution by + and - 3% (see B^+ fit) \Rightarrow variation of this fraction is $(18.9 \pm 3.0)\%$ (uncertainty will be considered as systematics source)

Systematic uncertainties in the branching fraction ratios

$$R_2^{0\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)}$$

$$R_1^{0\pm} = \frac{\mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}$$

Source	Systematic uncertainty in %	
	$R_2^{0\pm}$	$R_1^{0\pm}$
Track reconstruction efficiency	7.8	7.8
$m_{B^+\pi^-}$ distribution model	2.5	2.0
$m_{B^+K^-}$ distribution model	2.4	4.6
$m_{B^0K_S^0}$ distribution model	14	8.1
Mass resolution	0.7	2.2
Fraction of KPS	2.6	2.6
Non- K^{*0} contribution	5.0	5.0
Finite size of simulated samples	1.2	1.2
Total	18	14

$$R_{2*}^{\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*+} K^-)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} \quad R_{2*}^0 = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}$$

$$R_{\sigma}^{\pm} = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)}$$

$$R_{\sigma}^0 = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}$$

Source	Systematic uncertainty in %			
	R_{2*}^{\pm}	R_{2*}^0	R_{σ}^{\pm}	R_{σ}^0
$m_{B^+\pi^-}$ distribution model	2.9	—	2.7	—
$m_{B^+K^-}$ distribution model	17	—	7.1	—
$m_{B^0K_S^0}$ distribution model	—	13	—	24
Mass resolution	1.2	3.0	1.5	1.1
Uncertainties in $M_{B^*}^{\text{PDG}} - M_B^{\text{PDG}}$	7.7	4.8	—	—
Finite size of simulated samples	1.1	1.3	1.1	1.3
Total	19	15	7.8	24

Systematic uncertainties

Four mass differences obtained from the fits

$$\begin{aligned}\Delta M_{B_{s2}^*}^{\pm} &= M(B_{s2}^*) - M_{B^+}^{\text{PDG}} - M_{K^-}^{\text{PDG}}, & \Delta M_{B_{s1}}^{\pm} &= M(B_{s1}) - M_{B^{*+}}^{\text{PDG}} - M_{K^-}^{\text{PDG}} \\ \Delta M_{B_{s2}^*}^0 &= M(B_{s2}^*) - M_{B^0}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}}, & \Delta M_{B_{s1}}^0 &= M(B_{s1}) - M_{B^{*0}}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}}\end{aligned}$$

allow to measure the mass differences between neutral and charged $B^{(*)}$ mesons:

$$\begin{aligned}M_{B^0} - M_{B^+} &= \Delta M_{B_{s2}^*}^{\pm} - \Delta M_{B_{s2}^*}^0 + M_{K^-}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}} \\ M_{B^{*0}} - M_{B^{*+}} &= \Delta M_{B_{s1}}^{\pm} - \Delta M_{B_{s1}}^0 + M_{K^-}^{\text{PDG}} - M_{K_S^0}^{\text{PDG}}\end{aligned}$$

Additional systematic uncertainties are related to

> **Shift from reconstruction:** values obtained from the reconstructed MC differ a bit from those in the generation configuration. Our measurements are corrected by these shifts, and value of each shift is used as systematic uncertainty.

> **Detector misalignment:** 18 additional MC samples for each measurement are produced with differently distorted detector geometry, and maximum deviation from the case of no misalignment is taken as systematic uncertainty.

Source	$\Delta M_{B_{s2}^*}^{\pm}$	$\Delta M_{B_{s1}}^{\pm}$	$\Delta M_{B_{s2}^*}^0$	$\Delta M_{B_{s1}}^0$	$M_{B^0} - M_{B^+}$	$M_{B^{*0}} - M_{B^{*+}}$	$\Gamma_{B_{s2}^*}$
$m_{B^+\pi^-}$ distribution model	0.024	0.008	—	—	0.024	0.008	0.11
$m_{B^+K^-}$ distribution model	0.011	0.043	—	—	0.011	0.043	0.11
$m_{B^0K_S^0}$ distribution model	—	—	0.039	0.038	0.039	0.038	—
Uncertainties in $M_{B^*}^{\text{PDG}} - M_B^{\text{PDG}}$	0.012	0.003	0.003	0.0001	0.012	0.003	0.03
Shift from reconstruction	0.056	0.044	0.050	0.042	0.075	0.061	—
Detector misalignment	0.036	0.005	0.031	0.006	0.038	0.008	0.15
Mass resolution	0.007	0.005	0.005	0.005	0.009	0.007	0.20
Total	0.073	0.063	0.071	0.057	0.098	0.085	0.30

$B^0 K_S^0$ signal significance

Estimated using likelihood ratio of fits with and without signal component

$$P = \text{TMath.Prob}(\text{Log } L_S - \text{Log } L_0, 1) \\ \text{Signif} = \sqrt{2} \cdot \text{Tmath.ErfcInverse}(P)$$

where

L_0 corresponds to fit with signal

L_S corresponds to fit without signal

For these fits, systematic uncertainties of resolution and fraction of swapped component are included as Gaussian constraints in likelihood; Mass and Γ uncertainties from PDG are as well Gaussian-constrained

Obtained significance is:

6.3 σ for the $B_{s2}^* \rightarrow B^0 K_S^0$ decay

3.9 σ for the $B_{s1} \rightarrow B^{*0} K_S^0$ decay

They vary in $[6.3, 7.0]\sigma$ and $[3.6, 3.9]\sigma$ with variations of fit range and bkg model

Measured BF ratios

[CMS-BPH-16-003](#), [arXiv:1809.03578](#)

$$R_2^{0\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = \frac{N(B_{s2}^* \rightarrow B^0 K_S^0)}{N(B_{s2}^* \rightarrow B^+ K^-)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)} \times \frac{\mathcal{B}(B^+ \rightarrow J/\psi K^+)}{\mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) \mathcal{B}(K^{*0} \rightarrow K^+ \pi^-) \mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)}$$

$$R_1^{0\pm} = \frac{\mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)} = \frac{N(B_{s1} \rightarrow B^{*0} K_S^0)}{N(B_{s1} \rightarrow B^{*+} K^-)} \times \frac{\epsilon(B_{s1} \rightarrow B^{*+} K^-)}{\epsilon(B_{s1} \rightarrow B^{*0} K_S^0)} \times \frac{\mathcal{B}(B^+ \rightarrow J/\psi K^+)}{\mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) \mathcal{B}(K^{*0} \rightarrow K^+ \pi^-) \mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)},$$

$$R_{2*}^{\pm} = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*+} K^-)}{\mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = \frac{N(B_{s2}^* \rightarrow B^{*+} K^-)}{N(B_{s2}^* \rightarrow B^+ K^-)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s2}^* \rightarrow B^{*+} K^-)},$$

$$R_{2*}^0 = \frac{\mathcal{B}(B_{s2}^* \rightarrow B^{*0} K_S^0)}{\mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)} = \frac{N(B_{s2}^* \rightarrow B^{*0} K_S^0)}{N(B_{s2}^* \rightarrow B^0 K_S^0)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)}{\epsilon(B_{s2}^* \rightarrow B^{*0} K_S^0)},$$

$$R_{\sigma}^{\pm} = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*+} K^-)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^+ K^-)} = \frac{N(B_{s1} \rightarrow B^{*+} K^-)}{N(B_{s2}^* \rightarrow B^+ K^-)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s1} \rightarrow B^{*+} K^-)},$$

$$R_{\sigma}^0 = \frac{\sigma(\text{pp} \rightarrow B_{s1} \dots) \times \mathcal{B}(B_{s1} \rightarrow B^{*0} K_S^0)}{\sigma(\text{pp} \rightarrow B_{s2}^* \dots) \times \mathcal{B}(B_{s2}^* \rightarrow B^0 K_S^0)} = \frac{N(B_{s1} \rightarrow B^{*0} K_S^0)}{N(B_{s2}^* \rightarrow B^0 K_S^0)} \times \frac{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)}{\epsilon(B_{s1} \rightarrow B^{*0} K_S^0)},$$

Relative efficiencies

$$\begin{aligned}\frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)} &= 15.77 \pm 0.18, & \frac{\epsilon(B_{s1} \rightarrow B^{*+} K^-)}{\epsilon(B_{s1} \rightarrow B^{*0} K_S^0)} &= 16.33 \pm 0.20, \\ \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s2}^* \rightarrow B^{*+} K^-)} &= 0.961 \pm 0.010, & \frac{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)}{\epsilon(B_{s2}^* \rightarrow B^{*0} K_S^0)} &= 0.970 \pm 0.012, \\ \frac{\epsilon(B_{s2}^* \rightarrow B^+ K^-)}{\epsilon(B_{s1} \rightarrow B^{*+} K^-)} &= 0.953 \pm 0.010, & \frac{\epsilon(B_{s2}^* \rightarrow B^0 K_S^0)}{\epsilon(B_{s1} \rightarrow B^{*0} K_S^0)} &= 0.987 \pm 0.012,\end{aligned}$$

Their uncertainties are used as systematic uncertainties