



# Measurement of the CKM phase $\varphi_1$ in $b \rightarrow c\bar{u}d$ transitions at Belle (and BaBar)

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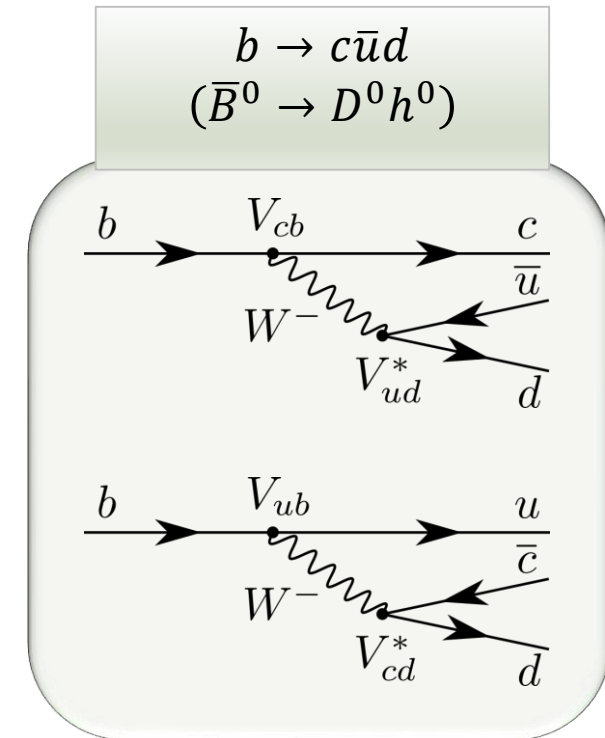
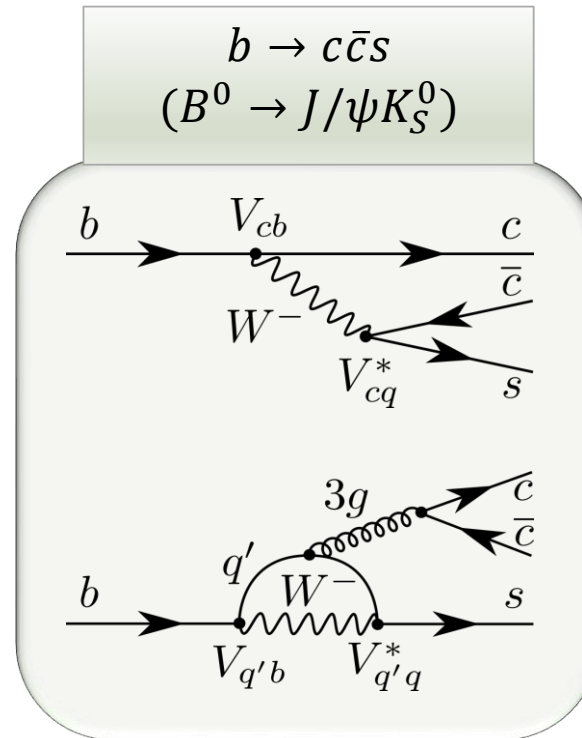
# Outline

- $CP$  violation study using the  $b \rightarrow c\bar{u}d$  transition
- Recent results:
  - Combined BaBar + Belle analysis of  $\bar{B}^0 \rightarrow D_{CP}^{(*)} h^0$  (2015)
  - Combined BaBar + Belle analysis of  $\bar{B}^0 \rightarrow D^{(*)} h^0, D^0 \rightarrow K_S^0 \pi^+ \pi^-$  (2017 preliminary)
  - *Model-independent* analysis of  $\bar{B}^0 \rightarrow D^{(*)} h^0, D^0 \rightarrow K_S^0 \pi^+ \pi^-$  with Belle data (2016)
- Prospects for measurement of the angle  $\varphi_1$  in  $b \rightarrow c\bar{u}d$  at LHCb and Belle II

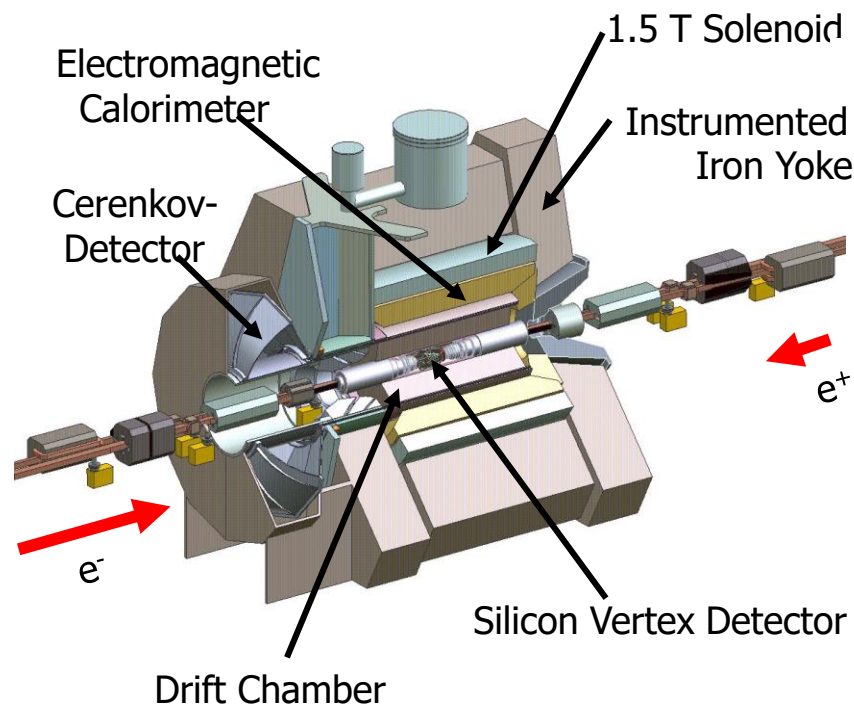
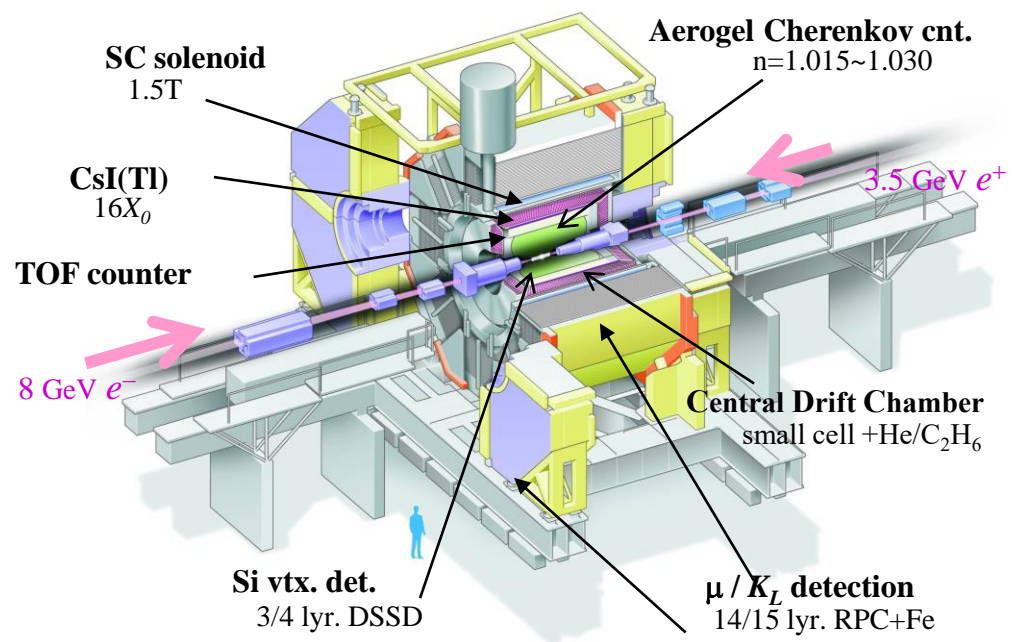


# Features of the $b \rightarrow c\bar{u}d$ transition

- A complementary and theoretically clean approach to access  $\varphi_1$
- The  $\bar{B}^0 \rightarrow D_{CP}^0 h^0$  ( $h^0 = \pi^0, \eta^{(\prime)}, \omega$ ) decays are **dominated by tree amplitudes** and are not sensitive to most of physics beyond standard model (BSM)
- A sizable deviation in the  $CP$  asymmetry of  $\bar{B}^0 \rightarrow D_{CP}^0 h^0$  decays from  $b \rightarrow c\bar{c}s$  would indicate BSM
- Time-dependent Dalitz analysis of the  $\bar{B}^0 \rightarrow D^0 h^0, D^0 \rightarrow K_S^0 \pi^+ \pi^-$  decays can be employed to measure  $\cos(2\varphi_1)$  and **to resolve the trigonometric ambiguity**.



# The Belle and BaBar experiments



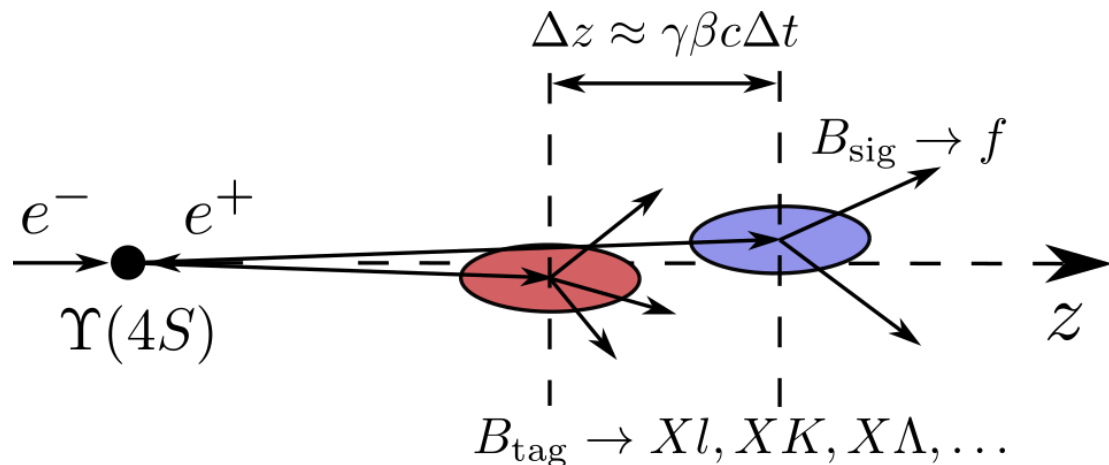
- The Belle experiment:

- Operation period: 1999 – 2010
- $1.04 \text{ ab}^{-1}$  integrated luminosity
- $772 \times 10^6 B\bar{B}$  pairs

- The BaBar experiment:

- Operation period: 1999 – 2008
- $541 \text{ fb}^{-1}$  integrated luminosity
- $471 \times 10^6 B\bar{B}$  pairs

# Time-dependent measurements at an asymmetric $B$ -factory

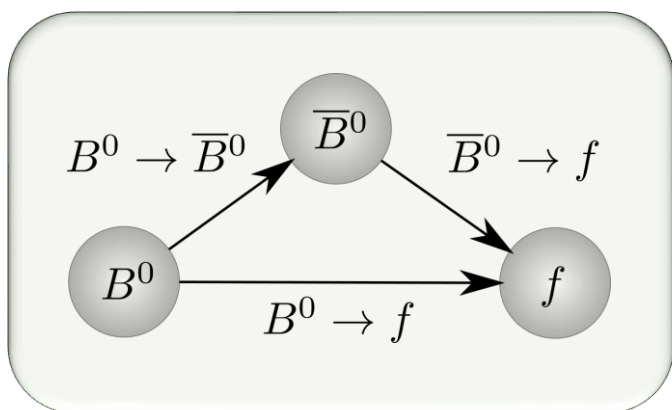


- Flight distance  $\Delta z \approx 200 \mu\text{m}$
- Vertex resolution  $\sigma(\Delta z) \approx 130 \mu\text{m}$
- Correct flavor tagging for  $\approx 80\%$  events
- Boost factor:
  - Belle  $\beta\gamma = 0.425$
  - BaBar  $\beta\gamma = 0.56$

## Time-dependent $B$ decay rate

$$g(\Delta t) = \frac{1}{4\tau_B} e^{-\frac{|\Delta t|}{\tau_B}} (1 + q[A \sin(\Delta m\Delta t) - B \cos(\Delta m\Delta t)])$$

- $q = \pm 1$  denotes the initial flavor of signal  $B$  meson
- Standard model predicts  $A = -\eta_f \sin(2\phi_1)$  and  $B = 0$  for a  $CP$ -specific final state with  $CP$  parity  $\eta_f$



# Combined BaBar + Belle analysis of

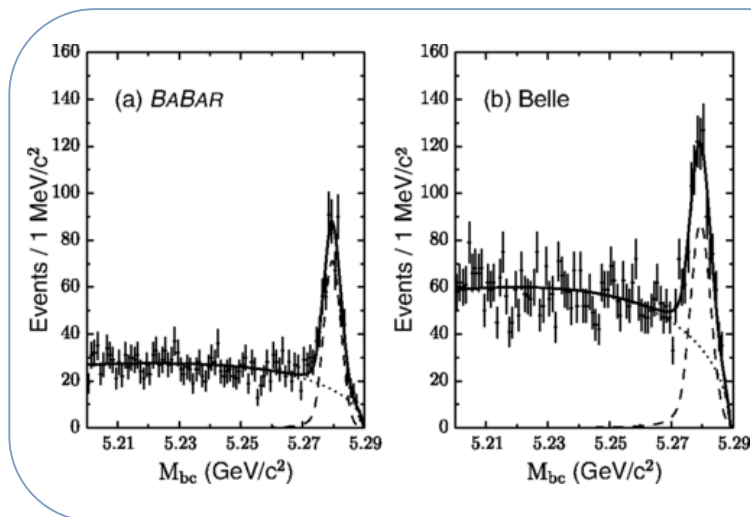
$$\bar{B}^0 \rightarrow D_{CP}^{(*)} h^0$$

**New approach: the first combined analysis of BaBar and Belle data**

PRL 115, 121604 (2015)

## Signal modes

- *CP*-even modes:
  - $D_{CP}\pi^0$  and  $D_{CP}\eta$  with  $D_{CP} \rightarrow K_S^0\pi^0, K_S^0\omega$
  - $D_{CP}\omega$  with  $D_{CP} \rightarrow K_S^0\pi^0$
  - $D_{CP}^*\pi^0$  and  $D_{CP}^*\eta$  with  $D_{CP} \rightarrow K^+K^-$
- *CP*-odd modes:
  - $D_{CP}\pi^0, D_{CP}\eta$  and  $D^0\omega$  with  $D_{CP} \rightarrow K^+K^-$
  - $D_{CP}^*\pi^0$  and  $D_{CP}^*\eta$  with  $D_{CP} \rightarrow K_S^0\pi^0$



## Signal yield

BaBar:  $508 \pm 31$

Belle:  $757 \pm 44$

## Background

- Dominant source of background originates from  $e^+e^- \rightarrow q\bar{q}$ ,  $q \in \{u, d, s, c\}$
- Flavor-specific decays like  $B^- \rightarrow D^{(*)0}\rho^-$ . Less than 8% of the signal

## Main kinematic variables

$$M_{bc} = \sqrt{(E_{\text{beam}}^*)^2 - (p_B^*)^2} \quad * \text{ denotes the } e^+e^- \text{ center-of-mass frame}$$

$$\Delta E = E_B^* - E_{\text{beam}}^*$$



# Combined BaBar + Belle analysis of

$$\bar{B}^0 \rightarrow D_{CP}^{(*)} h^0$$

PRL 115, 121604 (2015)

## Time-dependent $B$ decay rate

$$g(\Delta t) \propto 1 + q[A \sin(\Delta m \Delta t) + B \cos(\Delta m \Delta t)]$$

$A = -\eta_f \sin(2\varphi_1)$  and  $B = 0$  for a  $CP$ -specific final state

## Maximum likelihood fit of the $\Delta t$ distributions

$$\sin(2\varphi_1) = 0.66 \pm 0.10 \text{ (stat.)} \pm 0.06 \text{ (syst.)}$$

- No significant direct  $CP$  violation found:

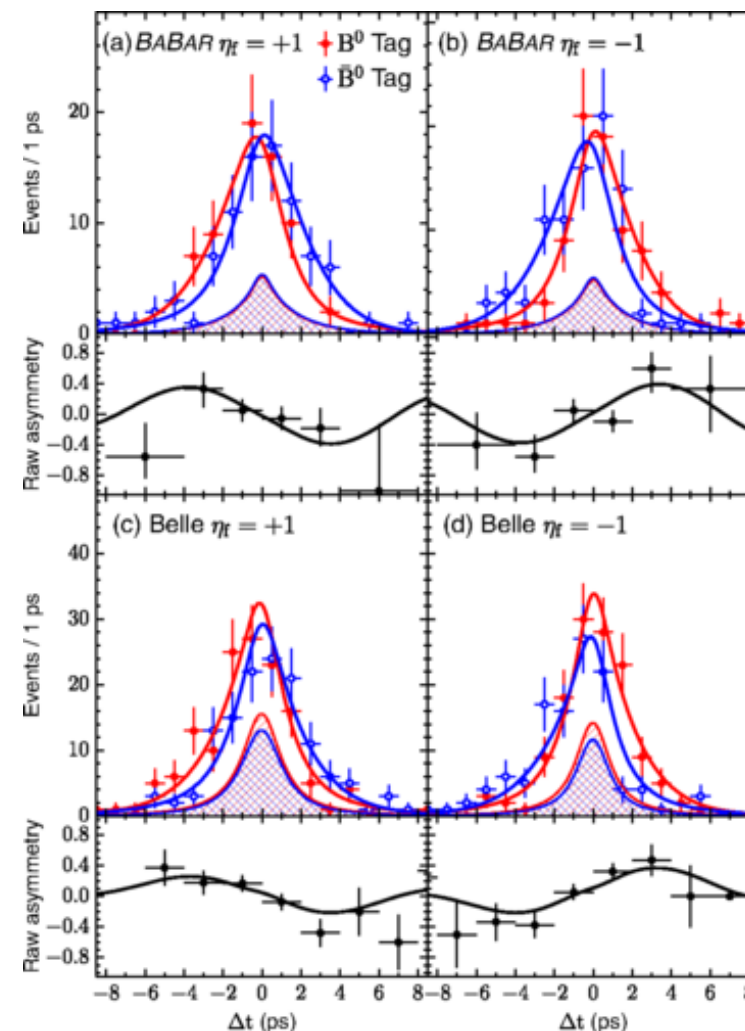
$$B = -0.02 \pm 0.07 \text{ (stat.)} \pm 0.03 \text{ (syst.)}$$

## Main systematics sources

- Peaking background (0.049)
- $\Delta t$  resolution functions (0.020)
- Vertex resolution (0.015)



**Observation of  $CP$  violation at  $5.4\sigma$  confidence level**





# Combined BaBar + Belle analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ Moriond 2017

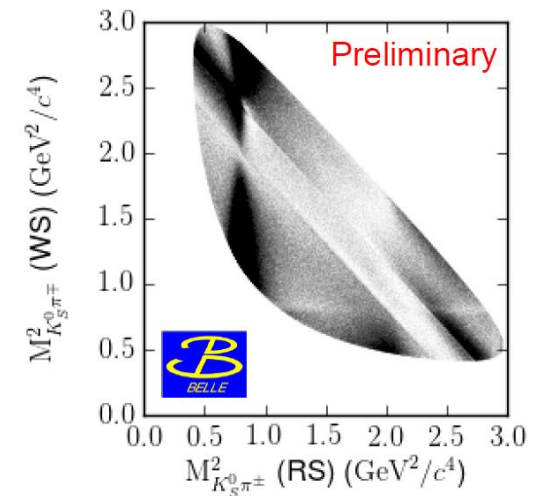
## The method

- **Time-dependent Dalitz analysis** enables to extract both  $\sin(2\varphi_1)$  and  $\cos(2\varphi_1)$  [Bondar, Krokovny, Gershon PLB 624, 1 (2005)]
- Variation of the (**unknown**)  $D^0$  decay amplitude phase over the Dalitz plot provides the sensitivity
- A (phenomenological)  **$D^0$  decay amplitude model** is required to predict the phase

## The $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay model

- The model is obtained from flavor-tagged  $e^+ e^- \rightarrow c\bar{c}$  ( $D^{*\pm} \rightarrow D^0 \pi^\pm$ ) data
- The model includes 14 intermediate two-body resonances
- The K-matrix and LASS parametrizations are used to model the  $\pi\pi$  and  $K\pi$  S-waves

[M. Rörcken, Moriond 2017]



# Combined BaBar + Belle analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

## Signal modes

- $D^{(*)0} h^0$ , with
  - $h^0$  in  $\pi^0 \rightarrow \gamma\gamma, \eta \rightarrow \gamma\gamma, \pi^+ \pi^- \pi^0$  and  $\omega \rightarrow \pi^+ \pi^- \pi^0$
  - $D^{*0} \rightarrow D^0 \pi^0$

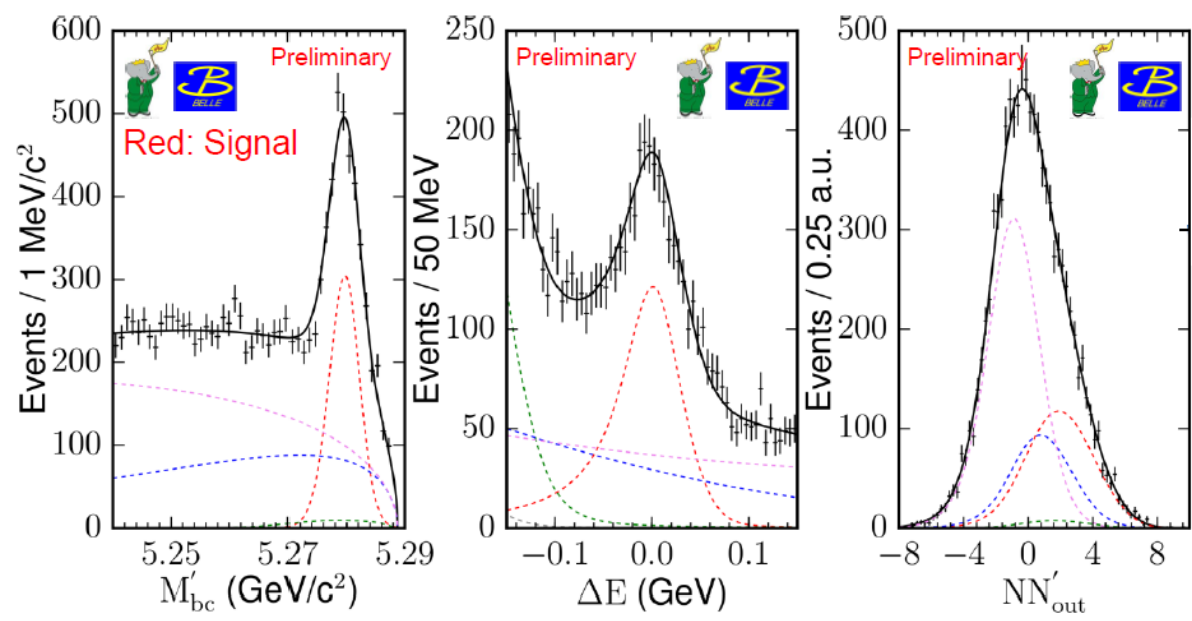
## Background

- Similar to the  $\bar{B}^0 \rightarrow D_{CP}^{(*)} h^0$  case

## Main variables

- $M'_{bc}$  – modified  $M_{bc}$
- $\Delta E$  – energy difference
- $NN'_{out}$  – neural net response

[M. Röhrken, Moriond 2017]



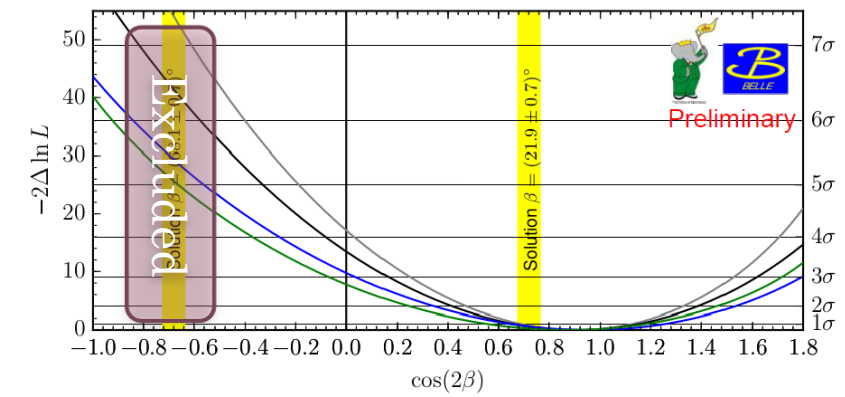
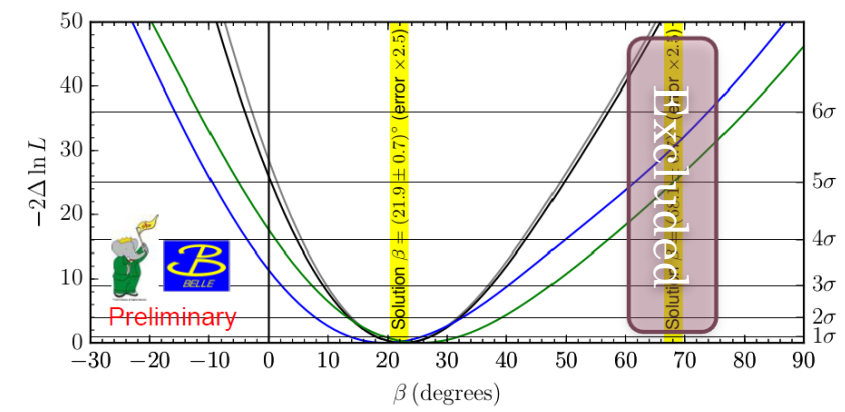
**Signal yield from 3D fit:** BaBar:  $1129 \pm 48$   
 Belle:  $1567 \pm 56$

# Combined BaBar + Belle analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

[M. Röhrken, Moriond 2017]

## Maximum likelihood fit of the $\Delta t$ distributions

$\sin(2\varphi_1) = 0.80 \pm 0.14$  (stat.)  $\pm 0.06$  (syst.)  $\pm 0.03$  (model)  
 $\cos(2\varphi_1) = 0.91 \pm 0.24$  (stat.)  $\pm 0.09$  (syst.)  $\pm 0.07$  (model)  
 $\varphi_1 = (22.5 \pm 4.4$  (stat.)  $\pm 1.2$  (syst.)  $\pm 0.6$  (model))<sup>0</sup>



## Main systematics sources

- Possible fit bias
- Vertex reconstruction
- $\Delta t$  resolution function
- Signal purity
- Background  $\Delta t$  p.d.f.s

- ✓ **First evidence for  $\cos(2\varphi_1) > 0$  @  $3.7\sigma$**
- ✓ **Direct exclusion of the 2<sup>nd</sup> solution @  $7.3\sigma$**
- ✓ **Observation of CP violation @  $5.1\sigma$**

# Model-independent analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

PRD 94, 052004 (2016)

## The binned Dalitz plot approach

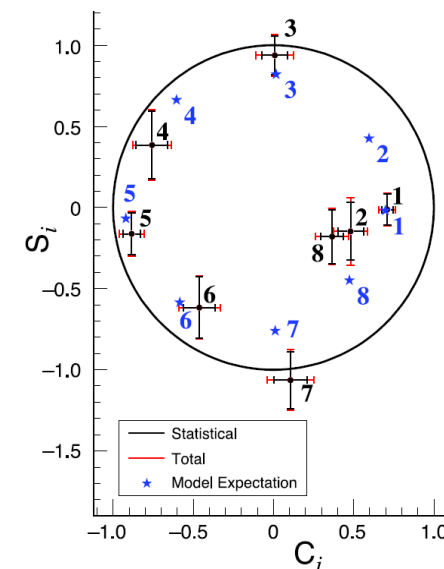
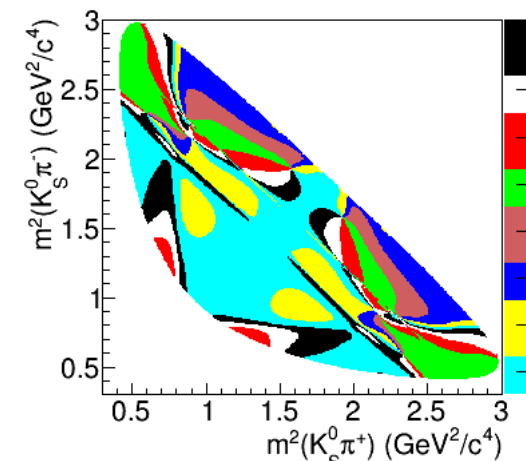
- Dalitz plot is divided into 16 regions [Giri et al. PRD 68, 054018 (2003)]
- Three parameters  $K_i$ ,  $C_i$  and  $S_i$  are defined for the  $i^{\text{th}}$  region:
  - $K_i$  – probability of  $D^0$  meson decay into the  $i^{\text{th}}$  region
  - $C_i$  and  $S_i$  – cos and sin of the decay amplitude phase difference between  $\bar{D}^0$  and  $D^0$  averaged over the  $i^{\text{th}}$  region

$$g_i(\Delta t) \propto U_i + q[A_i \sin(\Delta m \Delta t) - B_i \cos(\Delta m \Delta t)]$$

$$U_i = K_i + K_{-i}, \quad A_i = K_i - K_{-i},$$

$$B_i = 2\sqrt{K_i K_{-i}}(S_i \cos(2\varphi_1) + C_i \sin(2\varphi_1))$$

- The parameters  $C_i$  and  $S_i$  have been measured in coherent decays of  $D^0 \bar{D}^0$  pairs in CLEO experiment [PRD 82, 112006 (2010)]
- The equal-phase Dalitz plot partitioning increases sensitivity to  $\varphi_1$  [Bondar, Poluektov Eur. Phys. J. C47, 347 (2006); C55, 51 (2008)]

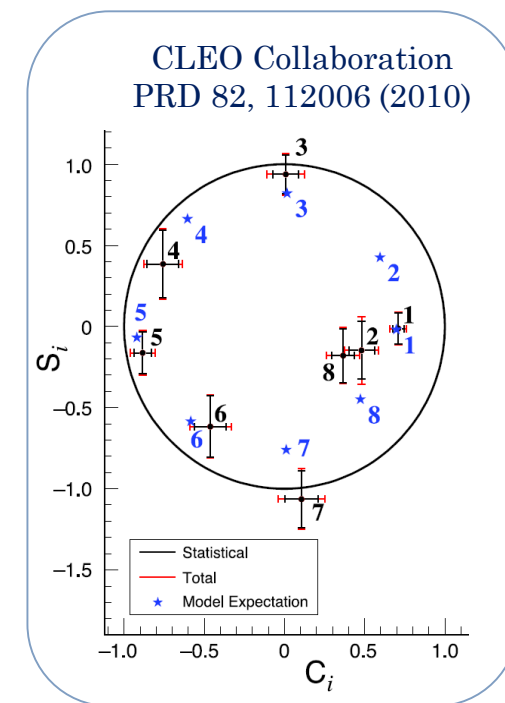
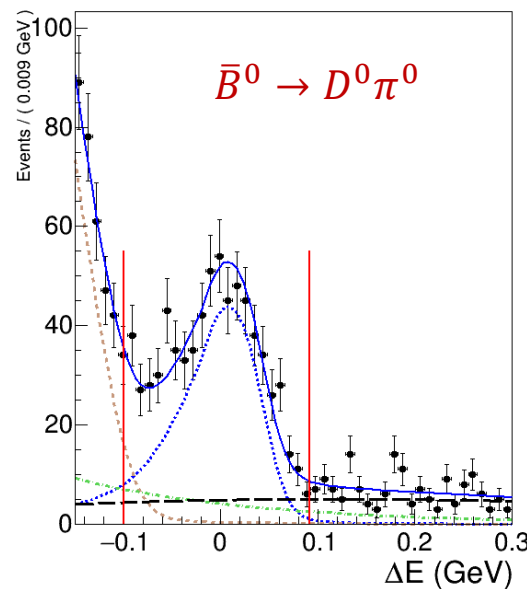
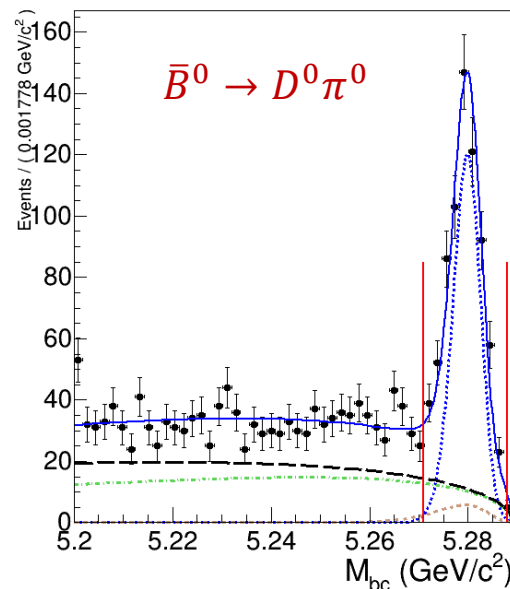


# Model-independent analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

PRD 94, 052004 (2016)

## Signal modes

- $D^0 h^0$ , with  $h^0$  in
  - $\pi^0 \rightarrow \gamma\gamma$ ,
  - $\eta \rightarrow \gamma\gamma, \pi^+ \pi^- \pi^0$ ,
  - $\eta' \rightarrow [\gamma\gamma]_{\eta} \pi^+ \pi^-$
  - $\omega \rightarrow \pi^+ \pi^- \pi^0$
- $D^{*0} h^0 \rightarrow D^0 \pi^0$  with
  - $D^{*0} \rightarrow D^0 \pi^0$
  - $h^0$  in  $\pi^0 \rightarrow \gamma\gamma, \eta \rightarrow \gamma\gamma$



## Main variables

- $M_{bc}$  – beam-energy constrained mass
- $\Delta E$  – energy difference

## The parameters of Dalitz plot

- $C_i$  and  $S_i$  from CLEO-c (**external input**)
- $K_i$  from  $B^- \rightarrow D^0 \pi^-$  decays

## Signal yield

$962 \pm 41$

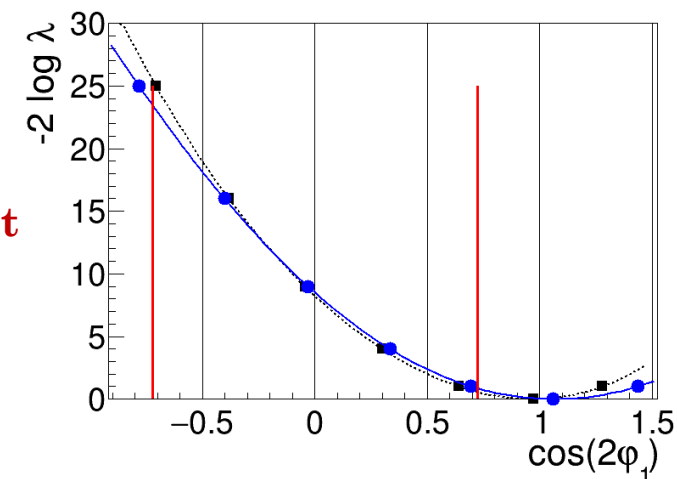
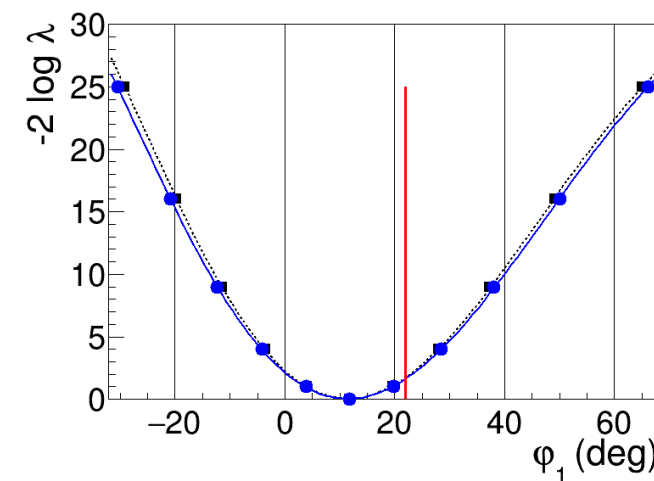
# Model-independent analysis of $\bar{B}^0 \rightarrow D^{(*)} h^0$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

## Maximum likelihood fit of the $\Delta t$ distributions

$$\sin(2\varphi_1) = 0.43 \pm 0.27 \text{ (stat.)} \pm 0.08 \text{ (syst.)}$$

$$\cos(2\varphi_1) = 1.06 \pm 0.33 \text{ (stat.)} {}^{+0.21}_{-0.15} \text{ (syst.)}$$

$$\varphi_1 = (11.7 \pm 7.8 \text{ (stat.)} \pm 2.1 \text{ (syst.)})^0$$



## Main systematics sources

- Uncertainties of  $C_i$  and  $S_i$  (dominant)
- $\Delta t$  resolution function
- Signal purity
- Background  $\Delta t$  p.d.f.s
- Uncertainties of  $K_i$



**Direct exclusion of the 2<sup>nd</sup> solution @ 5.1 $\sigma$**



**The first model-independent measurement of  $\cos(2\varphi_1)$**

# Prospects for LHCb and Belle II

Appropriate  $b \rightarrow c\bar{u}d$  processes

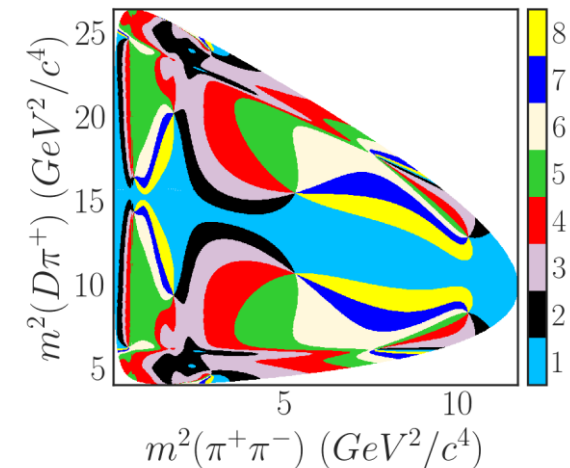
- $\bar{B}^0 \rightarrow D_{CP}^{(*)0} h^0$
- $\bar{B}^0 \rightarrow D^{(*)0} h^0$  with  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$
- $\bar{B}^0 \rightarrow D_{CP}^{(*)0} \pi^+ \pi^-$
- $\bar{B}^0 \rightarrow D^{(*)0} \pi^+ \pi^-$  with  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

The  $\bar{B}^0 \rightarrow D_{(CP)}^0 \pi^+ \pi^-$  decay

- May have only charged final-state particles
- Accessible for LHCb
- Can be analyzed with the binned Dalitz plot approach

- Model uncertainty can limit future precise measurements.
- A model-independent approach should be employed

$\bar{B}^0 \rightarrow D^0 \pi^+ \pi^-$  Dalitz plane



Estimates for the model-independent approach

- **Belle II** with  $50 \times$  (*Belle data set*) will be able to measure the angle  $\varphi_1$  in  $b \rightarrow c\bar{u}d$  transitions with precision **below one degree**
- **LHCb** with  $70 \times$  (*run I data set*) will be able to measure the angle  $\varphi_1$  in  $\bar{B}^0 \rightarrow D_{(CP)}^0 \pi^+ \pi^-$  decays with precision **about  $1.5^\circ$**



# Conclusions

- The  $b \rightarrow c\bar{u}d$  transition provides theoretically clean and the most precise approach to measure the  $\cos(2\varphi_1)$

$$\cos(2\varphi_1) = 0.91 \pm 0.24 \text{ (stat.)} \pm 0.09 \text{ (syst.)} \pm 0.07 \text{ (model)}$$

BaBar + Belle

$$\cos(2\varphi_1) = 1.06 \pm 0.33 \text{ (stat.)}^{+0.21}_{-0.15} \text{ (syst.)}$$

Belle model ind.

- Study of the  $\bar{B}^0 \rightarrow D^{(*)0}h^0$  decays with the full BaBar and Belle data sets resolved the angle  $\varphi_1$  ambiguity
- In the future, the angle  $\varphi_1$  can be measured in  $b \rightarrow c\bar{u}d$  transitions with precision below one degree in a model-independent way

# Backup

# The CKM $CP$ violation mechanism

$$\mathcal{L} \propto -\frac{g}{\sqrt{2}} (\bar{u}_L, \bar{c}_L, \bar{t}_L) \gamma^\mu W_\mu^+ V_{CKM} (d_L, s_L, b_L)^T + h.c.$$

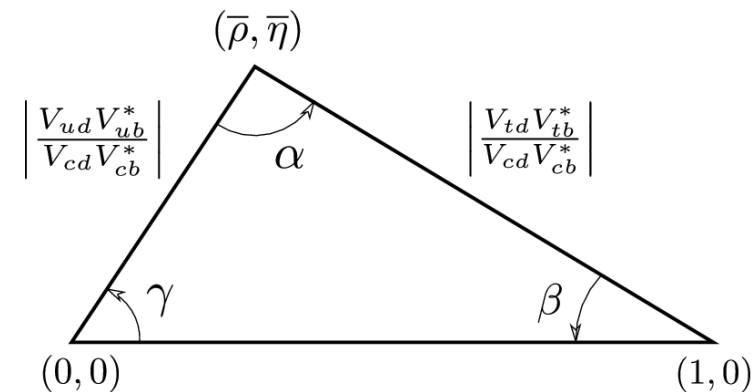
## The CKM matrix

- The unitary matrix of quark mixing for weak charged currents (Cabibbo, Kobayashi and Maskawa, CKM)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- Four independent parameters
- Can be parametrized with three Euler angles and **single phase**.

## The Unitarity Triangle



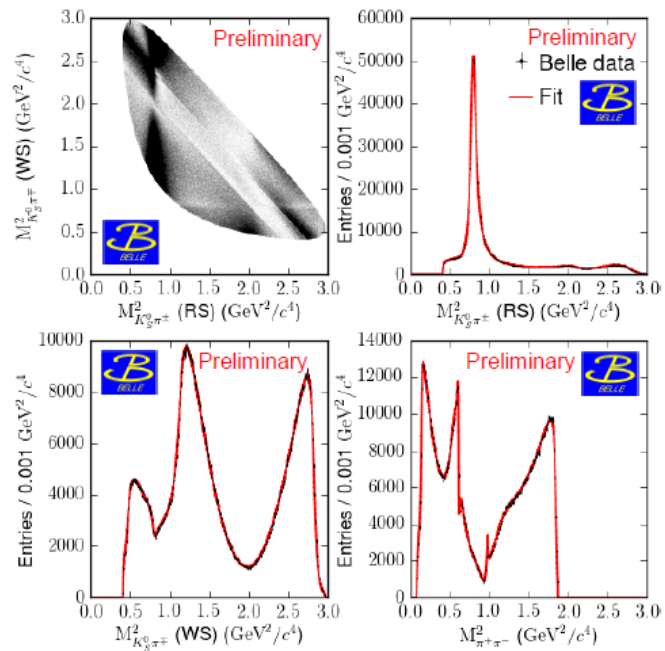
$$\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} + 1 = 0$$

## Combined *BABAR* + Belle Analysis of $B^0 \rightarrow D^{(*)} h^0$ decays

- The  $D \rightarrow K_S^0 \pi^+ \pi^-$  Dalitz model is directly obtained from flavor-tagged  $e^+e^- \rightarrow c\bar{c}$  data.

$$\mathcal{A}_{D^0}(m_+^2, m_-^2) = \sum_{r \neq (K\pi/\pi\pi)_{L=0}} a_r e^{i\phi_r} \mathcal{A}_r(m_+^2, m_-^2) + \mathcal{A}_{K\pi_{L=0}}(s) + F_1(s)$$

↑
↑
↑  
 Isobar model for L≠0      LASS      K-matrix



- The Dalitz model accounts for 14 intermediate two-body resonances.
- The K-matrix and LASS parameterizations are used to model the  $\pi\pi$  and  $K\pi$  S-waves.
- The  $D \rightarrow K_S^0 \pi^+ \pi^-$  Dalitz model extracted from  $e^+e^- \rightarrow c\bar{c}$  data is used to extract  $\sin(2\beta)$  and  $\cos(2\beta)$  from the  $B^0$  decay combining *BABAR* + Belle data.