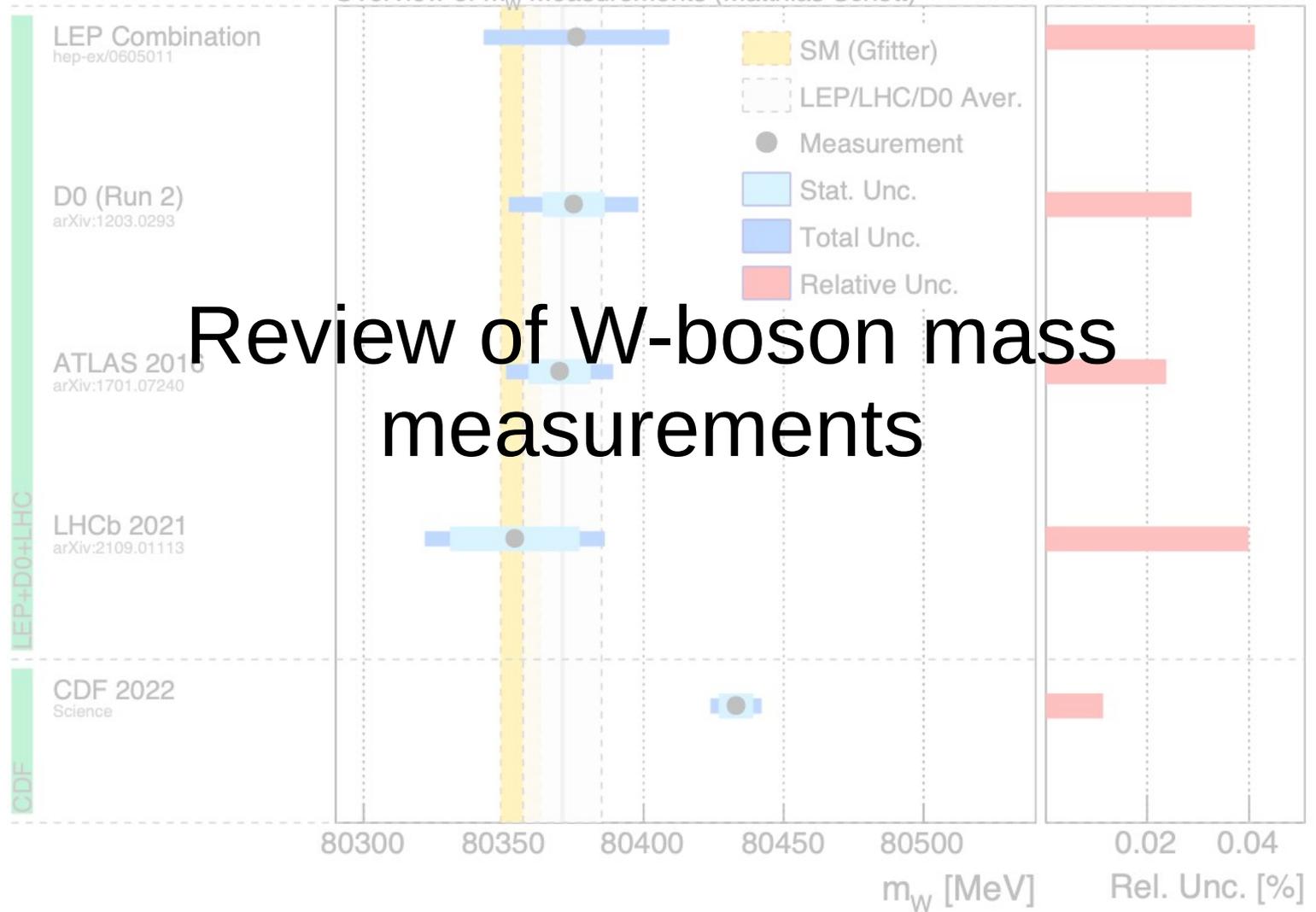


Overview of  $m_W$  Measurements (Matthias Schott)



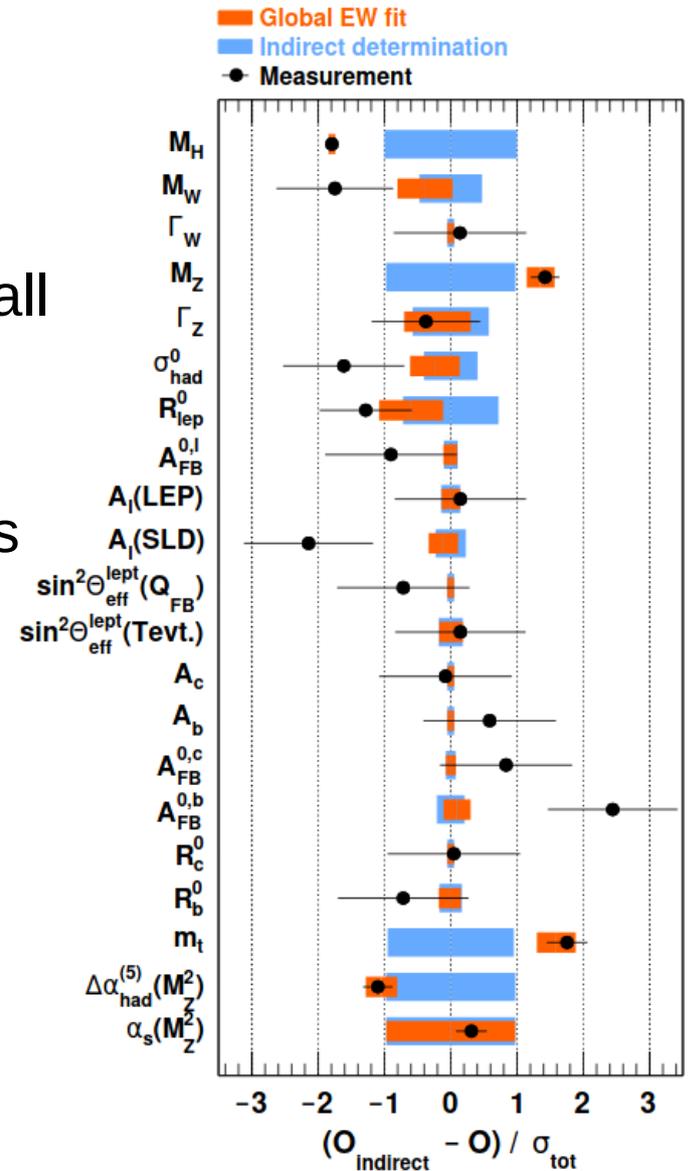
# Precision measurements of EW parameters

In the recent past, the global electroweak fit was able to predict the masses of the top quark and Higgs boson before their discovery

- After the measurement of the Higgs mass, all the free parameters of the Standard Model are known
- Relations between electroweak observables can be predicted at 2-loop level

Precise measurements of the electroweak parameters allow

- Stringent test of the self consistency of the SM
- Looking for hints of physics beyond the SM



Eur. Phys. J. C78, 675 (2018)

# Electroweak sector

The electroweak gauge sector of the Standard Model is constrained by three precisely measured parameters

$$\alpha = 1/137.035999139(31)$$

$$G_F = 1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$$

$$m_Z = 91.1876(21) \text{ GeV}$$



At tree level, other EW parameters can be expressed as

$$\left\{ \begin{array}{l} m_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F \left(1 - \frac{m_W^2}{m_Z^2}\right)} \\ \sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2} \\ \Gamma_W = \frac{3G_F m_W^3}{2\sqrt{2}\pi} \end{array} \right.$$

# Electroweak sector

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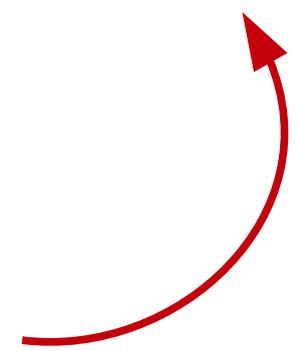
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At tree level, other EW parameters can be expressed as

$$\left\{ \begin{array}{l} m_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)} \\ \sin_{\text{eff}}^2 \theta_W = \left(1 - \frac{m_W^2}{m_Z^2}\right) \kappa \\ \Gamma_W = \frac{3G_F m_W^3}{2\sqrt{2}\pi} \rho \end{array} \right.$$

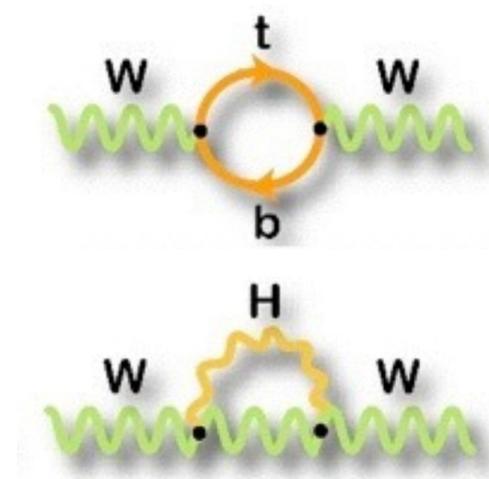
Higher order corrections modify these relations, and determine sensitivity to other particle masses and couplings



# Relation between top, Higgs and W masses

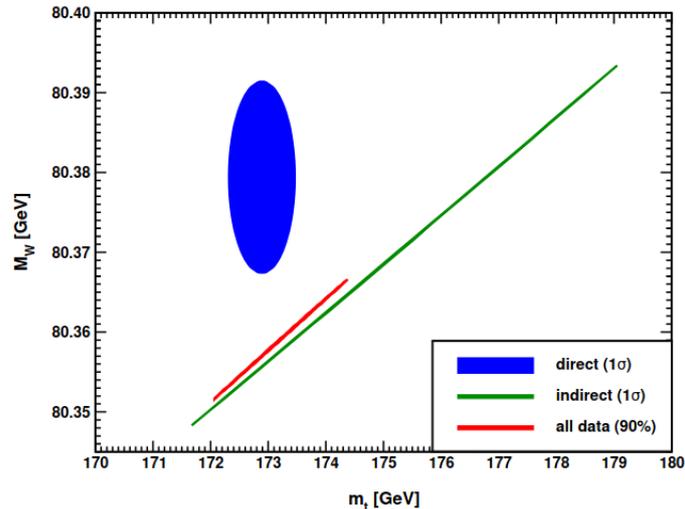
Radiative corrections  $\Delta r$  to  $m_W$  are dominated by top-quark and Higgs loops

$$m_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)}$$

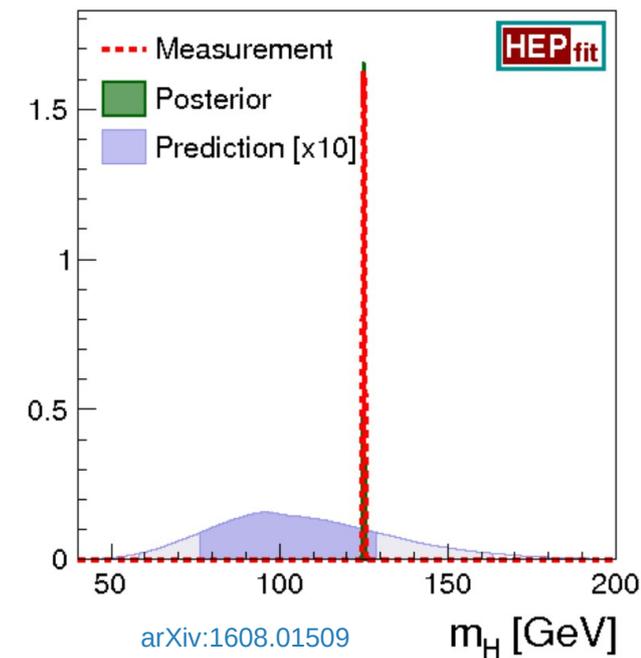


- The relation between  $m_t$ ,  $m_H$  and  $m_W$  provides a stringent test of the SM

Prog. Theor. Exp. Phys. 2020, 083C01 (2020)



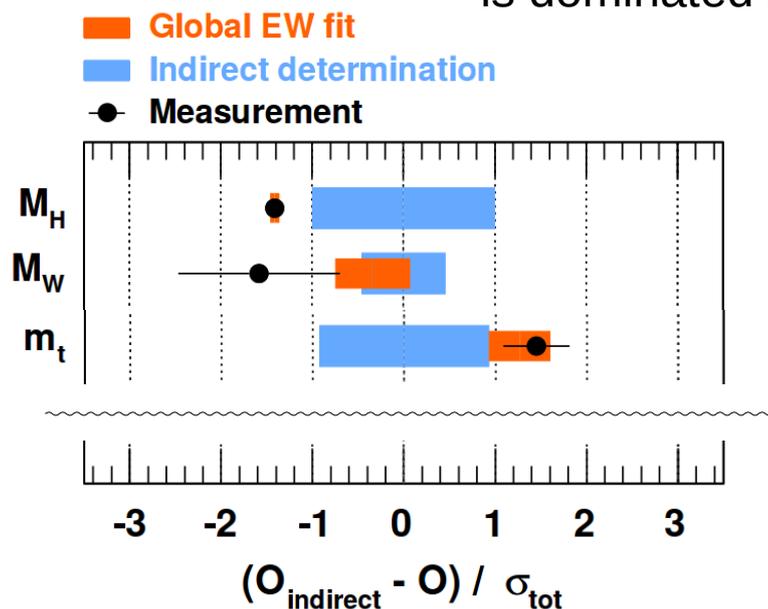
Probability density



- The comparison between the measured  $m_H$  and the predicted  $m_H$  is sensitive to new physics

# Motivation for $m_W$

The global fit of the electroweak observables is dominated by the measurement of  $m_W$



	Measurement	SM Prediction (*)
$m_H$	<b>125.09 ± 0.24</b>	<b>100.6 ± 23.6</b>
$m_t$	<b>173.1 ± 0.6</b>	<b>176.1 ± 2.2</b>
$m_W$	<b>80.379 ± 0.012</b>	<b>80.360 ± 0.007</b>

(\*) [arXiv:1710.05402](https://arxiv.org/abs/1710.05402)

The measurements of the Higgs and top-quark masses are currently more precise than their indirect determination from the global fit of the electroweak observables



Improving precision will not increase sensitivity to new physics

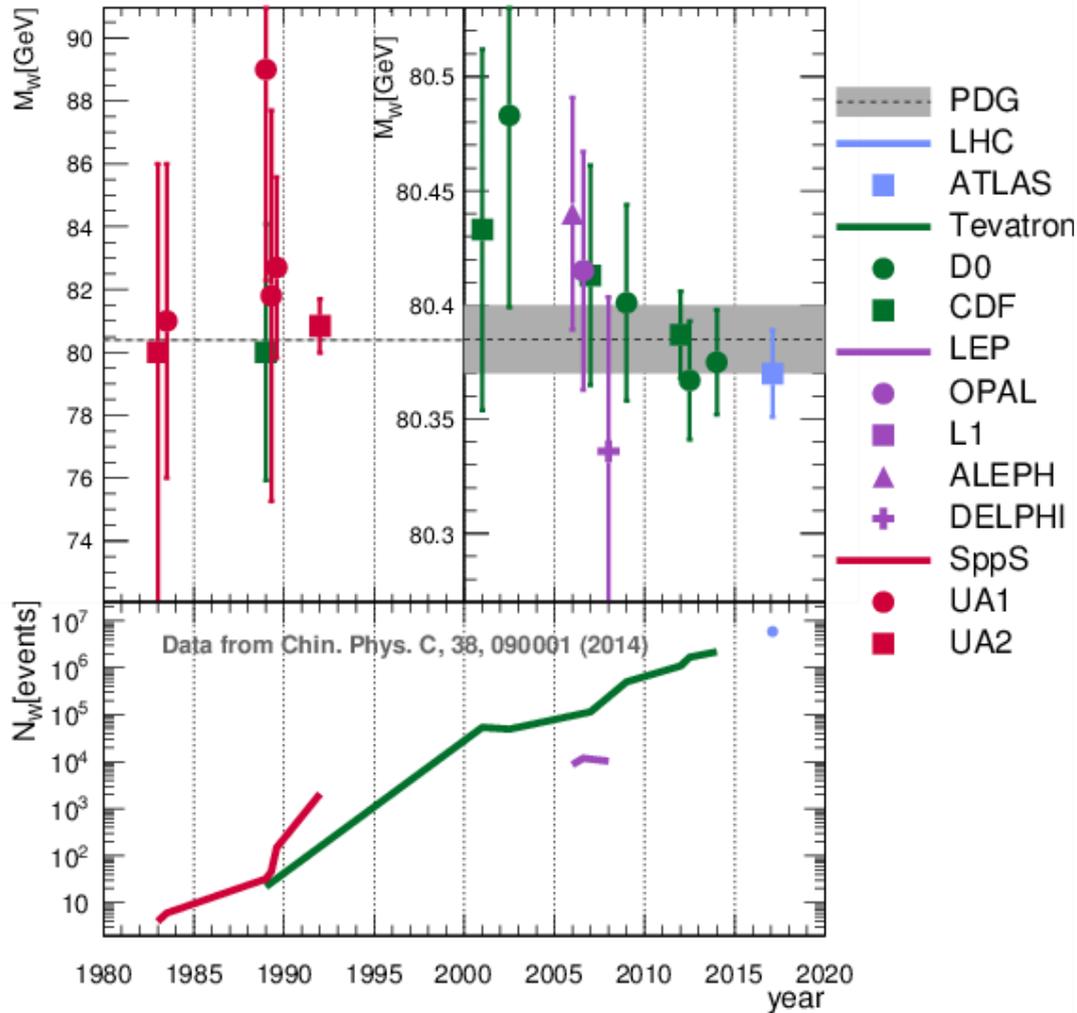
Indirect determination of  $m_W$  ( $\pm 7$  MeV) is more precise than the experimental measurement



Call for  $\delta m_W^{\text{exp}} \sim 5$  MeV

*The W mass is nowadays the crucial measurement to improve the sensitivity of the global EW fits to new physics*

# W-boson mass history

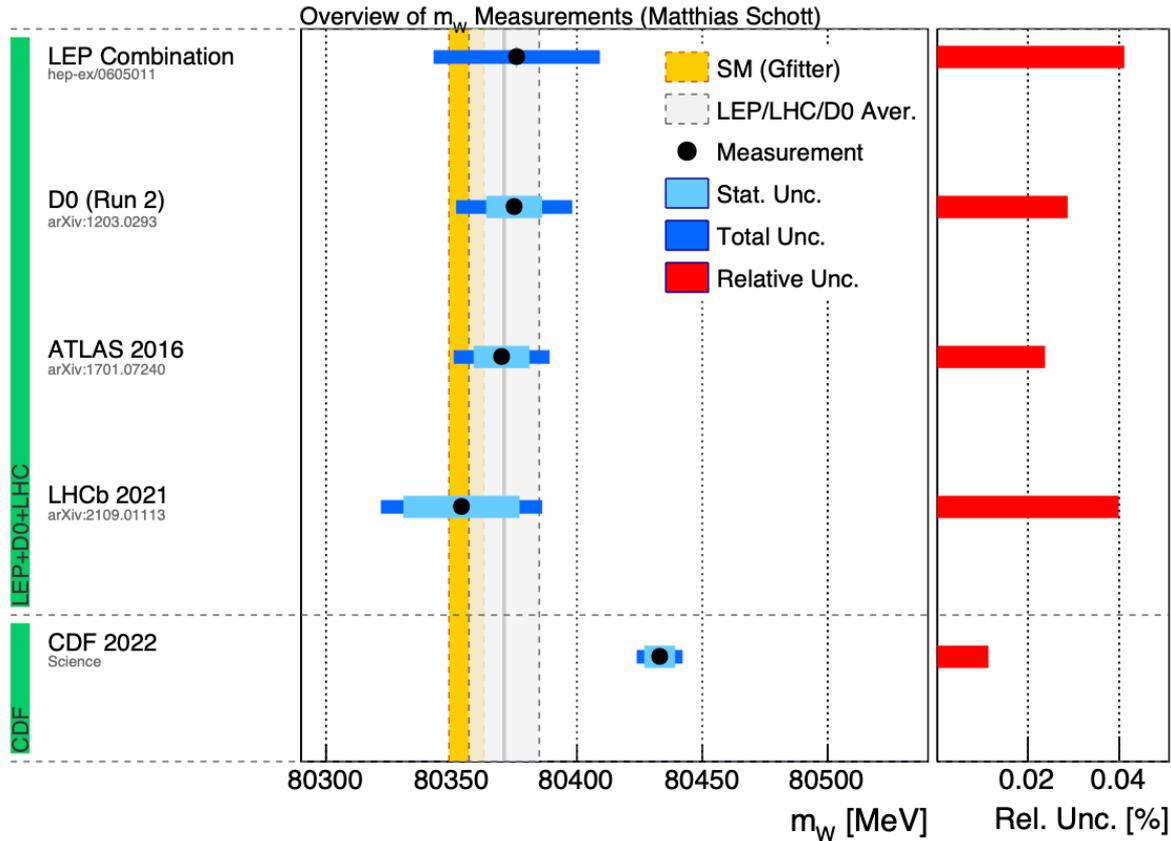


- 1983 CERN SPS – W discovery
- 1983 – UA1
  - $m_W = 81 \pm 5 \text{ GeV}$
- 1992 – UA2 (with  $m_Z$  from LEP)
  - $m_W = 80.35 \pm 0.37 \text{ GeV}$
- 2013 – LEP combined
  - $m_W = 80.376 \pm 0.033 \text{ GeV}$
- 2013 – Tevatron combined
  - $m_W = 80.387 \pm 0.016 \text{ GeV}$
- 2017 – LHC (ATLAS)
  - $m_W = 80.370 \pm 0.019 \text{ GeV}$

- Only four W-boson mass measurements in the last 10 years

➔ Complex measurements which require O(5-7) years

# W-boson mass today



Before we can make any conclusive statement on measurement/prediction, we should address tensions between measurements

# Experimental measurements at colliders

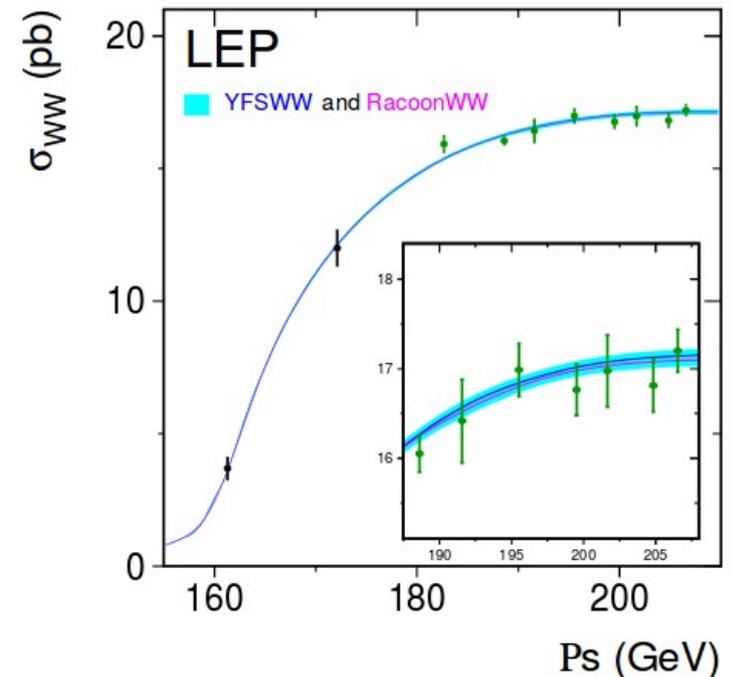
The W-boson mass can be measured from:

- Kinematic properties of decay leptons in the final state in  $pp \rightarrow W \rightarrow l\nu$  processes (hadron colliders)
- Direct reconstruction from the final state in  $ee \rightarrow WW \rightarrow q\bar{q}q\bar{q}/q\bar{q}l\nu$  ( $e^+e^-$  colliders)
- W-pair production at thresholds ( $e^+e^-$  colliders)

SPS, Tevatron,  
LHC

LEP best  
measurements

Limited by statistics at LEP,  
but most precise prospect  
at future colliders



# W mass at future colliders

- The ultimate precision on  $m_W$  can be achieved at  $e^+e^-$  colliders through an energy scan of the  $WW$  production threshold

- Near threshold, the  $WW$  cross section is proportional to the non-relativistic  $W$  velocity  

$$\sigma(WW) \propto \beta_W$$

arXiv:1306.6352

ILC Giga-Z program

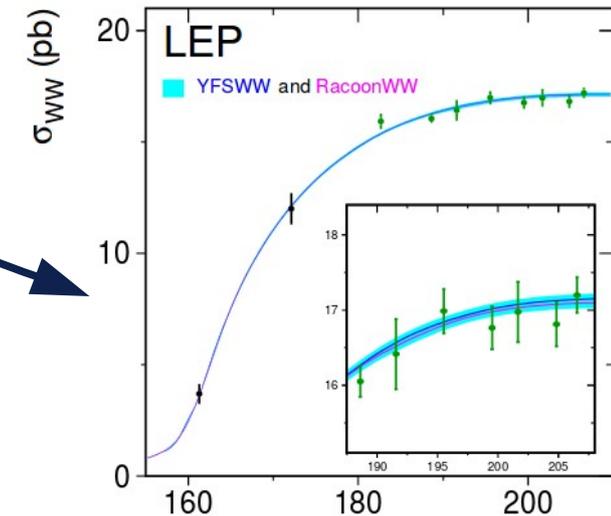
- Energy scan 160 to 170 GeV
- $\delta M_W = 6-7$  MeV

FCCee  $WW$  program

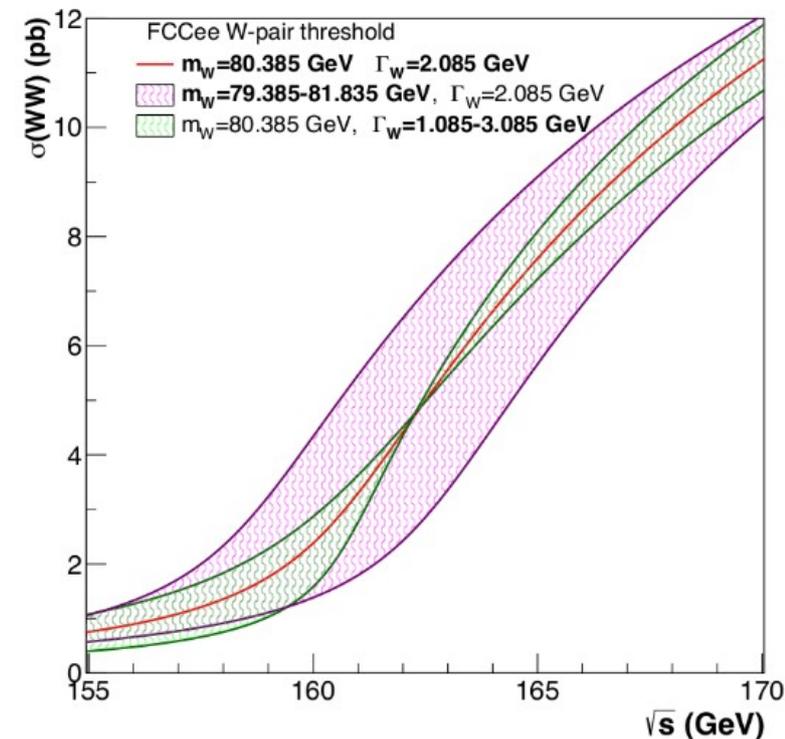
- $\delta M_W = 0.5$  MeV  
 → dominated by statistical uncertainty

Dominant theory uncertainties

- Initial state QED corrections
- Parametrization of cross section near threshold



Phys.Rept. 532 (2013) 119-244 Ps (GeV)

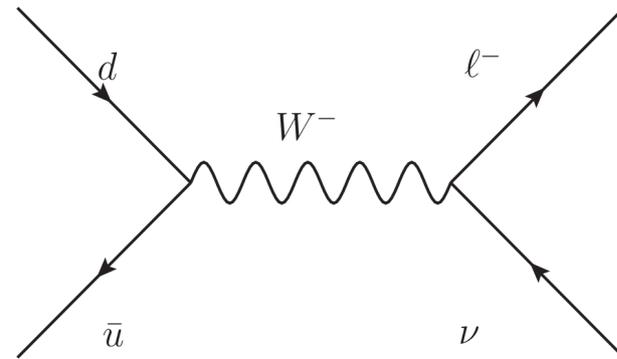
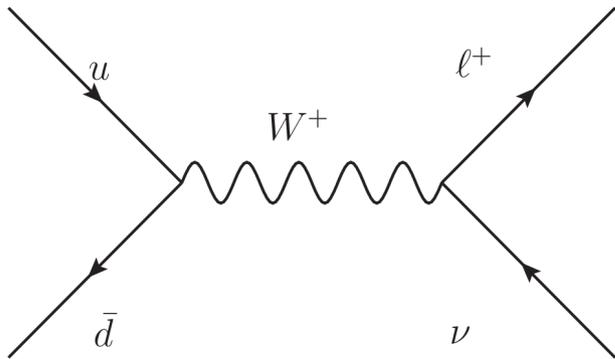


# PDF uncertainties for the W mass

- Sea quarks composition of protons is charge symmetric
  - same amount of  $q_s$  and  $\bar{q}_s$  from sea
- Valence quarks determines a charge asymmetry in the proton:

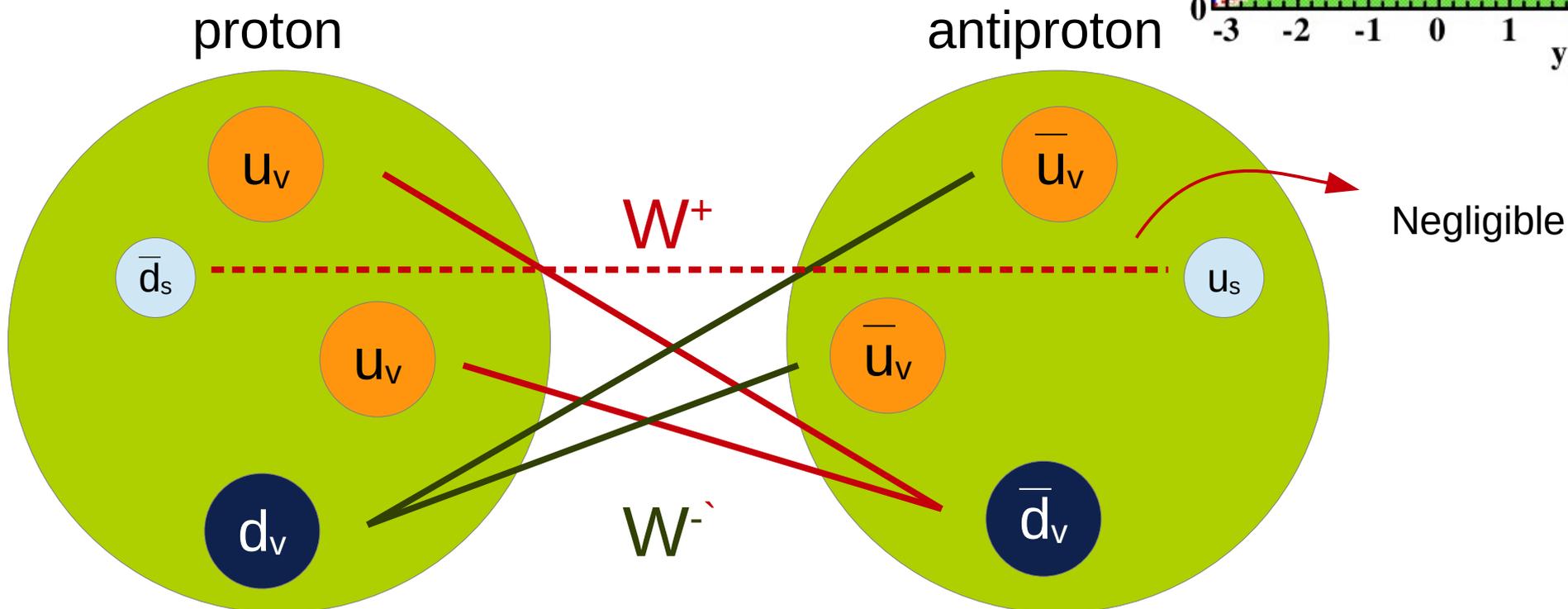
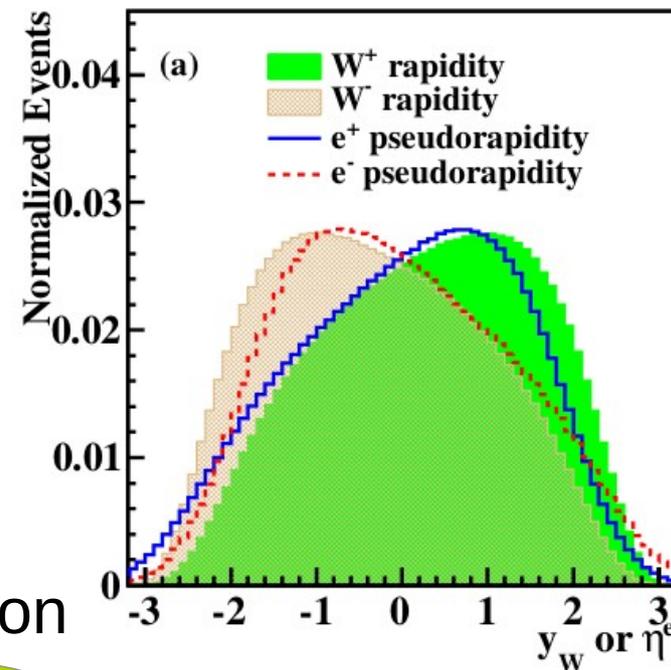
$$\begin{aligned} u &= u_v + u_s & \bar{u} &= \bar{u}_s \\ d &= d_v + d_s & \bar{d} &= \bar{d}_s \end{aligned}$$

What is the effect of this valence asymmetry for Charged Current Drell-Yan (W-boson) production?



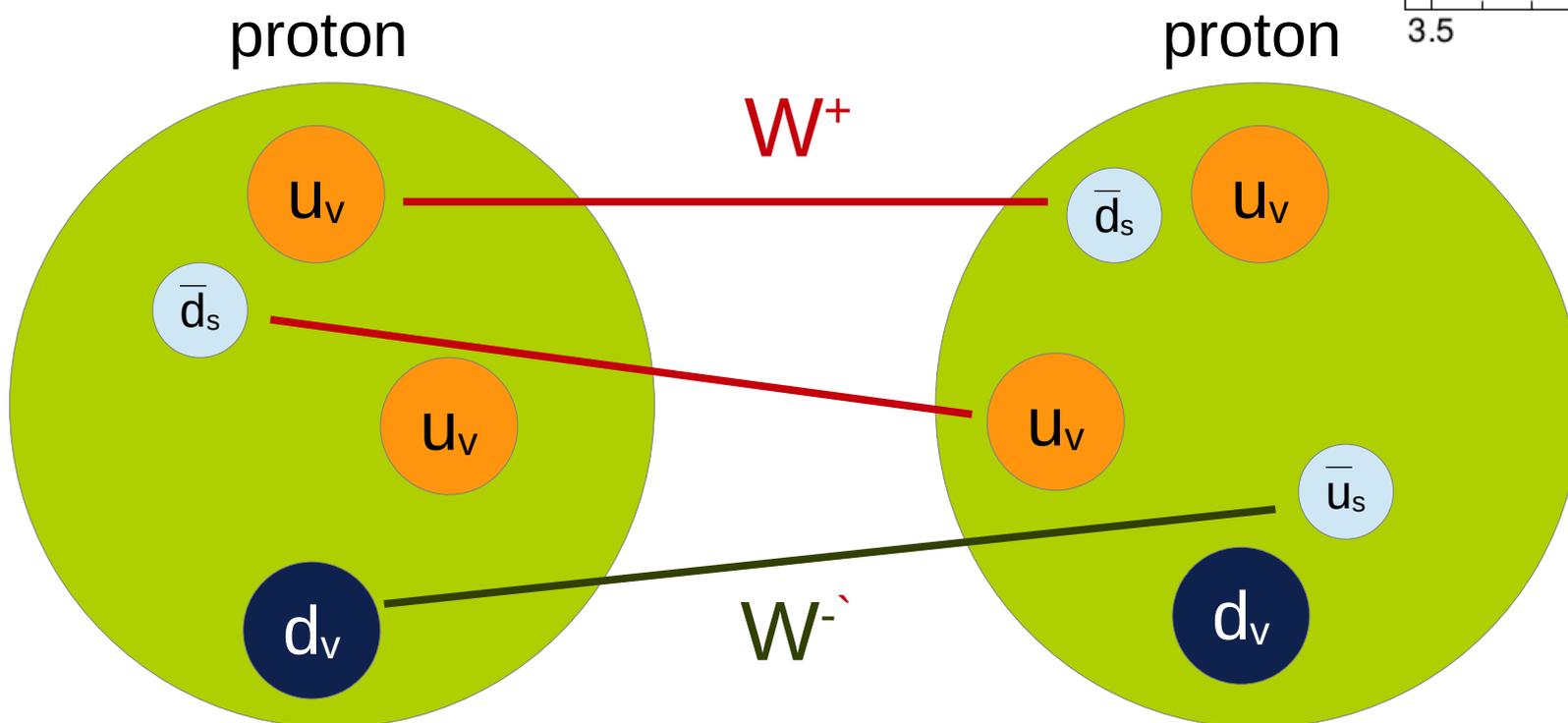
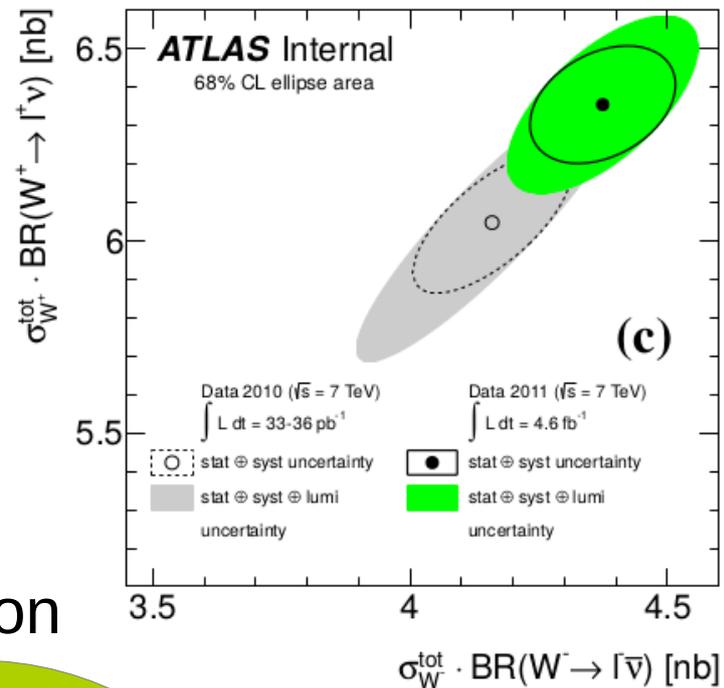
# PDF uncertainties for the W mass

- In proton-antiproton collision
- Asymmetry of the W rapidity
- Same cross section for  $W^+$  and  $W^-$
- Valence-dominated production
- Very small ambiguity for the incoming parton: quark from proton, antiquark from antiproton



# PDF uncertainties for the W mass

- In proton-proton collision
- Different cross section for  $W^+$  and  $W^-$
- Large ambiguity in the direction of the incoming quark



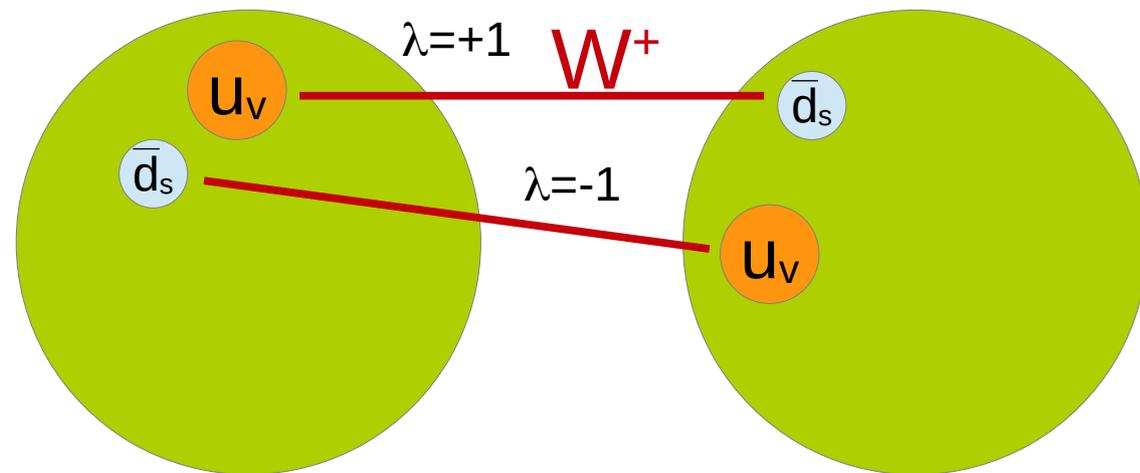
# PDF uncertainties for the W mass

- What is the consequence of the ambiguity in the direction of the incoming quark?

$$\sigma_{W^+}(y) \propto u(x_1) \cdot \bar{d}(x_2) + \bar{d}(x_1) \cdot u(x_2)$$

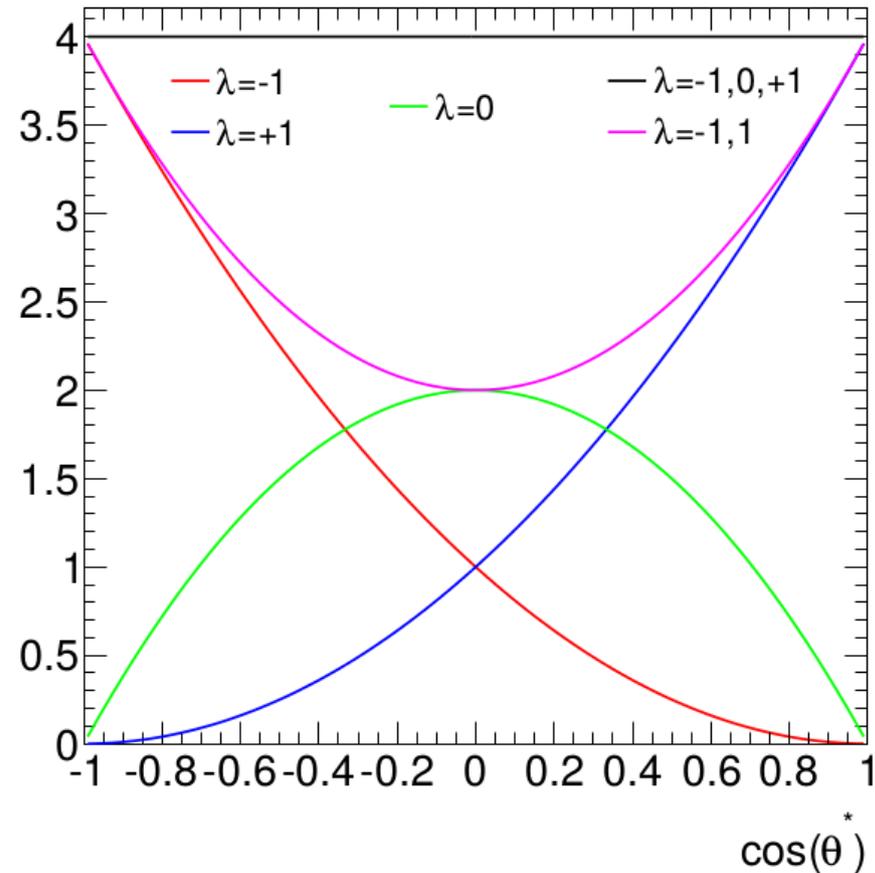
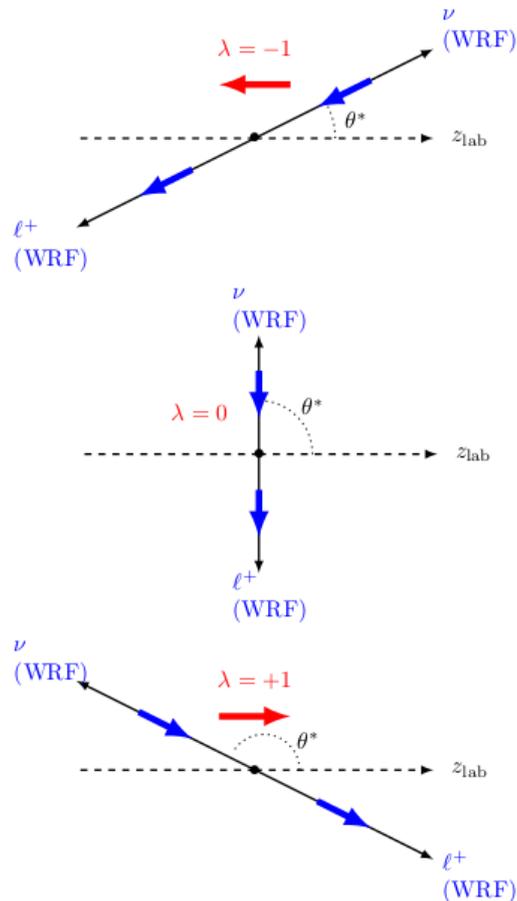
$$\sigma_{W^-}(y) \propto d(x_1) \cdot \bar{u}(x_2) + \bar{u}(x_1) \cdot d(x_2)$$

- The helicity is the projection of the spin on the momentum axis
- The W is a spin 1 particle, with 3 possible helicity states:  $\lambda = +1, 0, -1$
- Ambiguity in the average helicity of the W (polarisation)



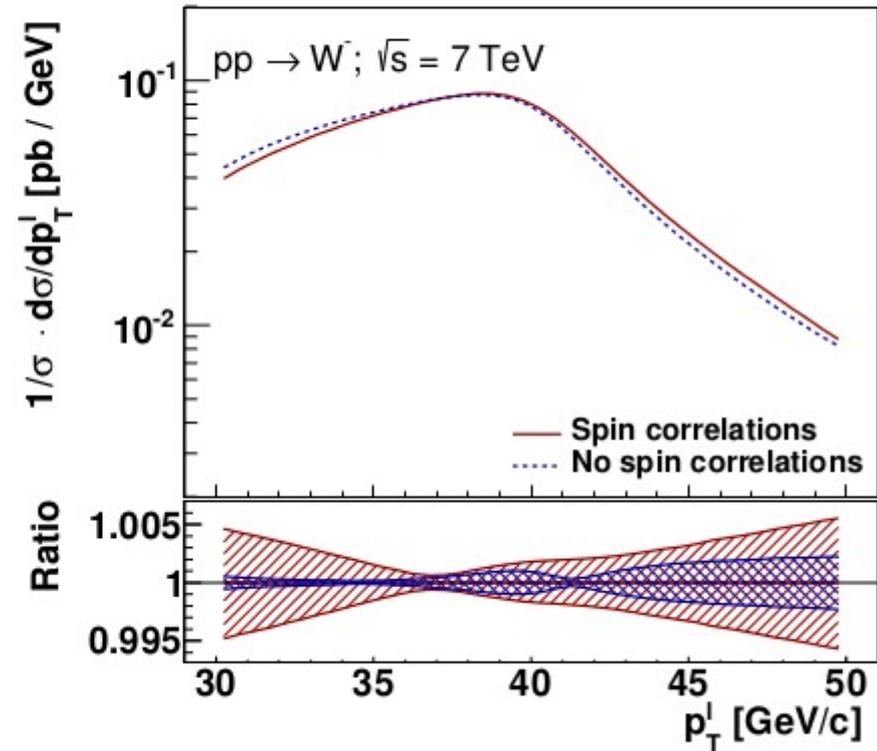
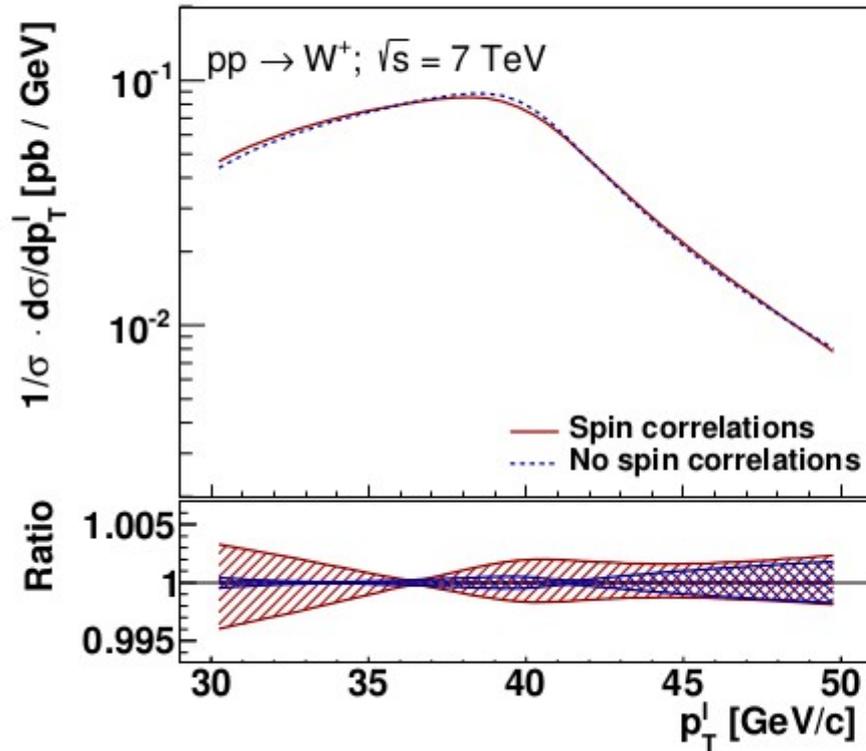
PDF uncertainty  $\rightarrow$  polarisation uncertainty

# W polarisation



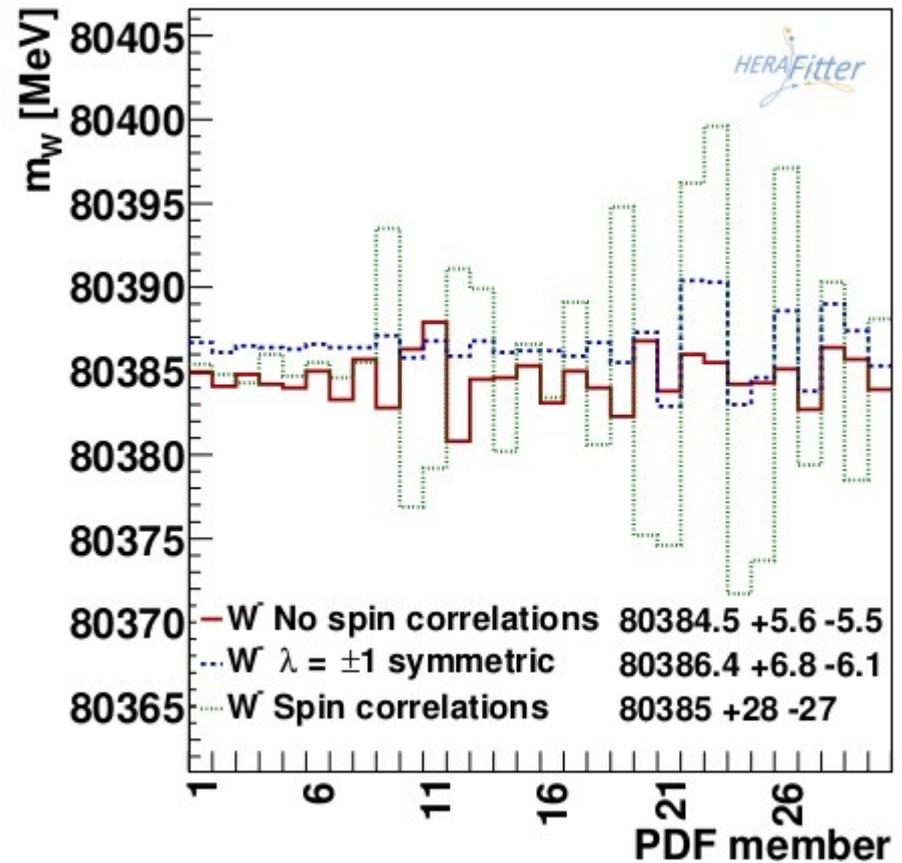
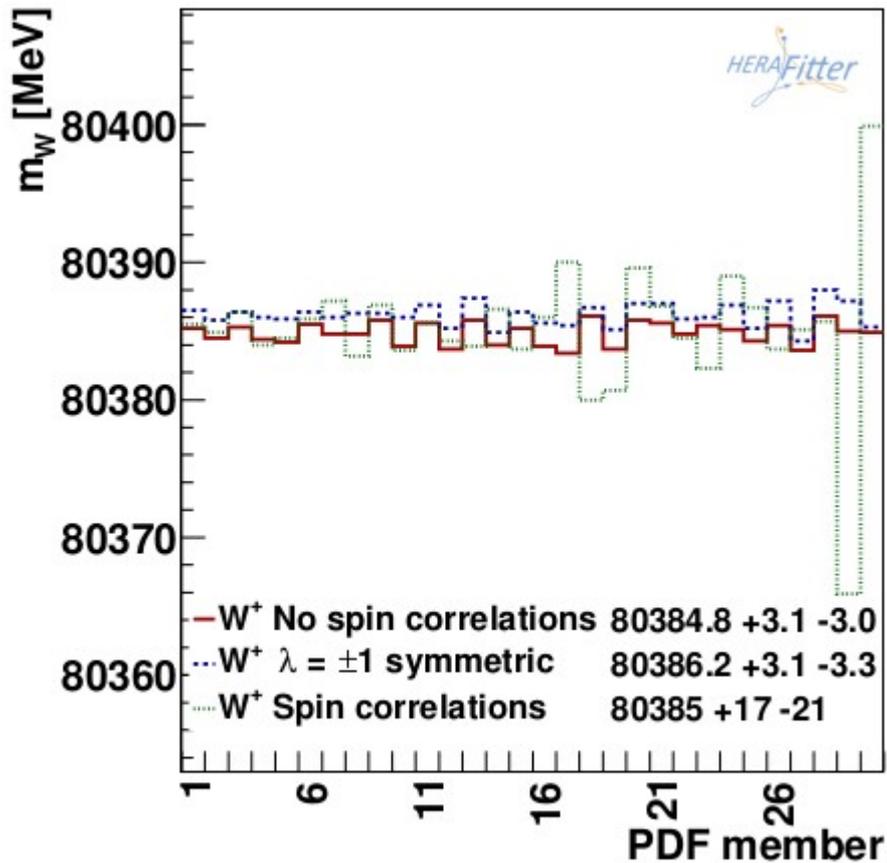
- The 3 helicity states have very different decay polar angles
- The average polarisation heavily affects the lepton kinematic

# W polarisation



- We can artificially remove the ambiguity in the W helicity by removing spin correlations  $\rightarrow$  Unpolarised W
- Dramatic effect on PDF uncertainties of lepton  $p_T$  distribution

# W polarisation



- This effect accounts for 20 (30) MeV uncertainty to the  $W$  mass extracted from  $W^+$  ( $W^-$ ) lepton  $p_T$

# W mass at the LHC

- Experimental  $m_W$  is limiting the precision of the EW fit
- Measuring  $m_W$  is very challenging: slow progress in uncertainty, few measurements, very long analysis
- Hierarchy in expected precision and trustworthiness of  $m_W$  measurements: pair production at threshold, proton-antiproton, proton-proton

ERC funded projects on the  $W$  mass measurement at the LHC

- ATLAS [UMWA](#) → completed

Ultimate measurement of the  $W$  boson mass with ATLAS, at the LHC

- LHCb [SPEAR](#) → ongoing

Standard model Precision Electroweak tests at Acute Rapidities

- CMS [ASYMOW](#) → starting

Power to the LHC data: an ASYmptotically MOdel-independent measurement of the  $W$  boson mass