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Puzzle in decoherence measurements of entangled annihilation photons

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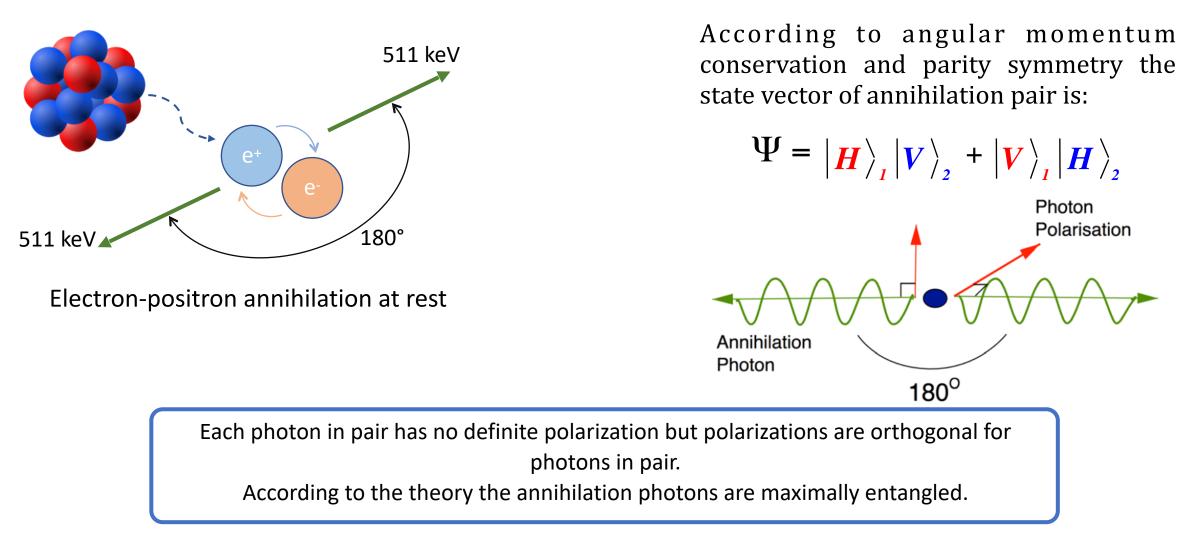
Tasks

- •Study of Compton scattering of decoherent annihilation photons;
- •Comparison of Compton scattering kinematics of annihilation photons in entangled and mixed states.

Importance

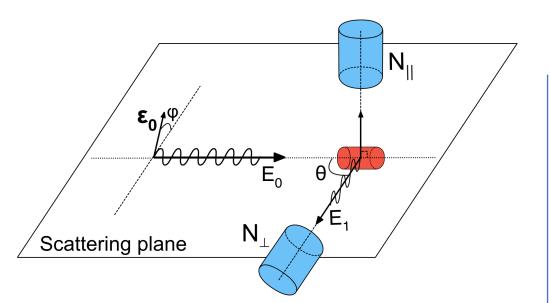
- Compton scattering of entangled and decoherent photons has not been studied thoroughly enough;
- Theoretical calculations in the scattering cross sections of entangled and decoherent photons lead to contradictory results;
- The differences in the Compton scattering of entangled and decoherent photons are planned to be used in a new generation PET tomographs.

Annihilation photons



Polarization correlations can only be studied with Compton polarimeters.

Compton polarimeter



Differential cross-section of Compton is given by Klein-Nishina formula:

$$\frac{d\sigma}{d\Omega}(\theta,\phi) = \frac{1}{2} \cdot \frac{e^2}{m_e c^2} \cdot \frac{E_{\gamma_1}^2}{E_{\gamma}^2} \cdot \left(\frac{E_{\gamma_1}}{E_{\gamma}} + \frac{E_{\gamma}}{E_{\gamma_1}} - 2\sin^2\theta\cos^2\phi\right)$$

Cross-section is maximum for $\phi = \pi/2$

Analyzing power is an asymmetry in scattering of gammas:

 $A = \frac{N_{\parallel} - N_{\perp}}{N_{\parallel} + N_{\perp}}$

Analyzing power for Compton polarimeter:

$$A = \frac{\frac{d\sigma}{d\Omega} \left(\theta, \phi = 90^{0}\right) - \frac{d\sigma}{d\Omega} \left(\theta, \phi = 0^{0}\right)}{\frac{d\sigma}{d\Omega} \left(\theta, \phi = 90^{0}\right) + \frac{d\sigma}{d\Omega} \left(\theta, \phi = 0^{0}\right)} = \frac{\sin^{2}\theta}{\frac{E_{\gamma_{1}}}{E_{\gamma}} + \frac{E_{\gamma}}{E_{\gamma_{1}}} - \sin^{2}\theta}$$

Maximum A=0.7 for 511 keV gammas in ideal case (scattering angle=82⁰). *A* is significantly smaller than 1. It provides the problems in polarization measurements for annihilation photons.

Probing entanglement (by measuring S-function of Bell's inequations)

Optimal angles between two-channels polarimeters

22.5°

Traditional method: construction of correlation coefficients and functions based on the (CHSH-) Bell inequality :

Correlation coefficients $E(\vec{a}, \vec{b}) = \frac{N(\vec{a}_{||}, \vec{b}_{||}) + N(\vec{a}_{\perp}, \vec{b}_{\perp}) - N(\vec{a}_{||}, \vec{b}_{\perp}) - N(\vec{a}_{\perp}, \vec{b}_{||})}{N(\vec{a}_{||}, \vec{b}_{||}) + N(\vec{a}_{\perp}, \vec{b}_{\perp}) + N(\vec{a}_{||}, \vec{b}_{\perp}) + N(\vec{a}_{\perp}, \vec{b}_{\perp})}$ N - number of coincidences between the corresponding counters of two two-channel polarimeters.

Correlation function for ideal polarimeter (A=1):

$$S = E\left(\overrightarrow{a}, \overrightarrow{b}\right) - E\left(\overrightarrow{a}, \overrightarrow{b^{\circ}}\right) + E\left(\overrightarrow{a}, \overrightarrow{b^{\circ}}\right) + E\left(\overrightarrow{a}, \overrightarrow{b^{\circ}}\right) + E\left(\overrightarrow{a^{\circ}}, \overrightarrow{b^{\circ}}\right)$$

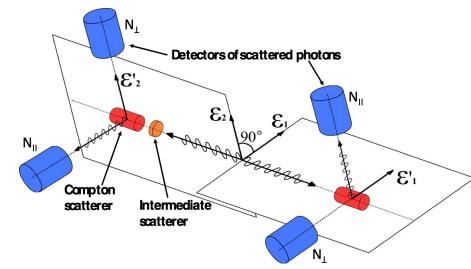
According to Bell's (CHSH) inequality: - S<2 for **non-entangled** system - Maximum $S = 2\sqrt{2}$ for **entangled** system if the angles between polarimeters are multiples of 22.5 degrees.

The entanglement can not be proven directly from Bell's (CHSH) inequality because of low analyzing power ($A \sim 0.7$)

> For non-ideal polarimeter: $S = > S' = S \bullet A^2 = >$ $S^{\sim} < 2$ for annihilation photons ($A^2 < 0.5$)

Azimuthal asymmetry in angular distributions of scattered gammas (instead of Bell's inequality) was used to prove the entanglement of annihilation photons

Probing entanglement (by measuring angular correlations)



$$P_{12}(E_1, E_2, \phi) = \left(\frac{d\sigma}{d\Omega_1}\right)_{NP} \left(\frac{d\sigma}{d\Omega_2}\right)_{NP} \left[1 - \alpha(\theta_1)\alpha(\theta_2)\cos(2\phi)\right]$$

Ratio of the numbers of scattered annihilation photons:

$$R_{theory}(\theta) = \frac{N\left(\phi = \frac{\pi}{2}\right)}{N\left(\phi = 0\right)} = 1 + \frac{2\sin^4\theta}{\gamma^2 - 2\gamma\sin^2\theta}; \qquad \gamma = 2 - \cos\theta + (2 - \cos\theta)^-$$

 $R=2.6 for \theta=90^0$

According to D. Bohm and Y. Aharonov (Phys. Rev. (1957) 108, 1070) the measurements of angular correlations would provide the experimental test of the **entanglement** if **R>2**. For decoherent photons *R=1*.

For non-entangled photons *R*<2.

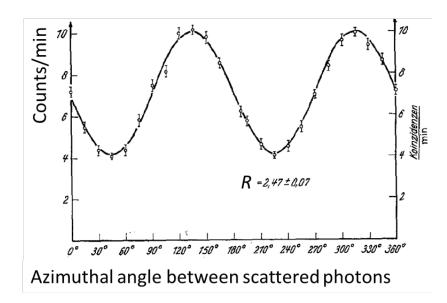
The best experimental values:

H. Langhof, Zeitschrift fur Physik 160, 186-193 (1960)

L.Kasday, J.Ullman and C.Wu C1971–1996, Nuovo Cimento B 25 633–61 (1975)

$$R=2.47\pm0.07$$

 $R = 2.33 \pm 0.10$



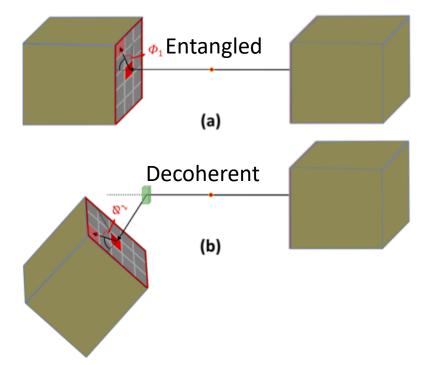
For a long time, it was assumed that these results confirmed entanglement of annihilation photons. The *decoherent* annihilation photons *were not measured* at all!

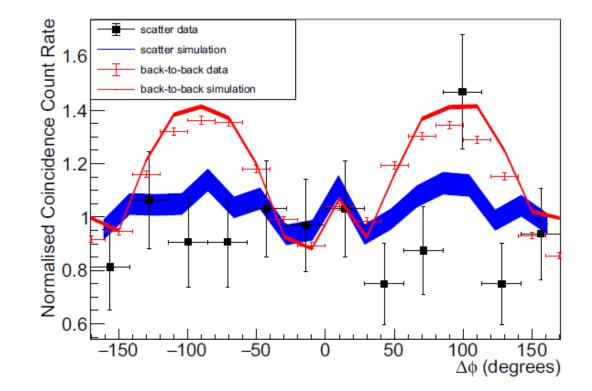
Current situation in theory

Hiesmayr B.C. and Moskal P. Witnessing entanglement in Compton scattering processes via mutually unbiased bases Sci. Rep.9 8166 (2019) The Compton scattering of annihilation photons is the same for both entangled and decoherent states. There is NO the experimental proof of the entanglement.

Peter Caradonna *et al.* Probing entanglement in Compton interactions *J. Phys. Commun.* **3** 105005 (2019) The Compton scattering of annihilation photons is principally different for entangled and decoherent states. There is no need to prove the entanglement. But... The measurements of decoherent photons are needed!

Recent experimental studies



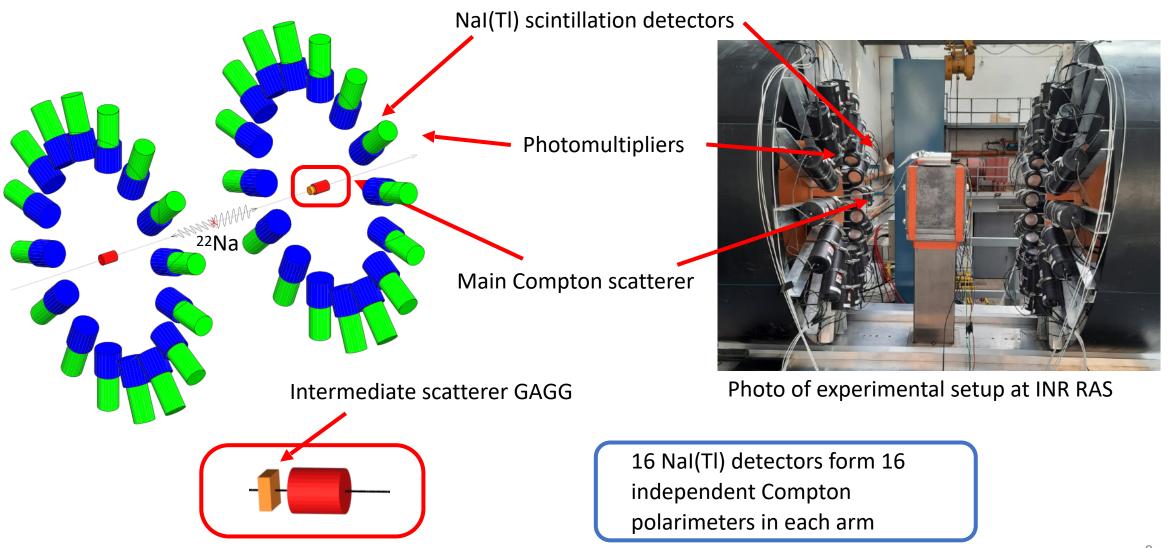


Watts, D.P., Bordes, J., Brown, J.R. *et al.* Photon quantum entanglement in the MeV regime and its application in PET imaging. *Nat Commun* **12**, 2646 (2021)

First measurement of decoherent annihilation photons was done last year with decoherent photons. Strong difference between entangled and decoherent states is observed. New experiment with better accuracy is needed. Such experiment is

running at INR RAS

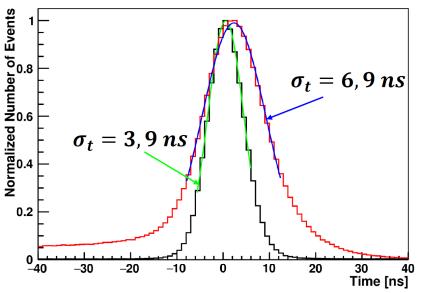
Experimental setup at INR RAS, Moscow



Decoherent photons

Intermediate scatterer : GAGG scintillator

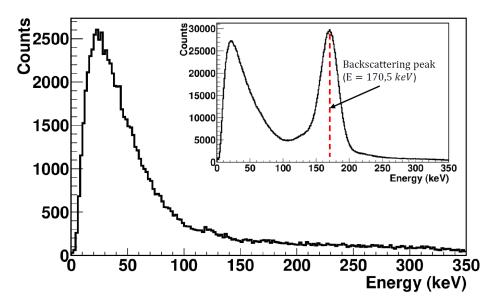




Time coincidence spectra between signals in GAGG intermediate and plastic scatterers.

Red and black lines correpond to events with energy deposition range in GAGG 2-40 keV and 40-120 keV, respectively.

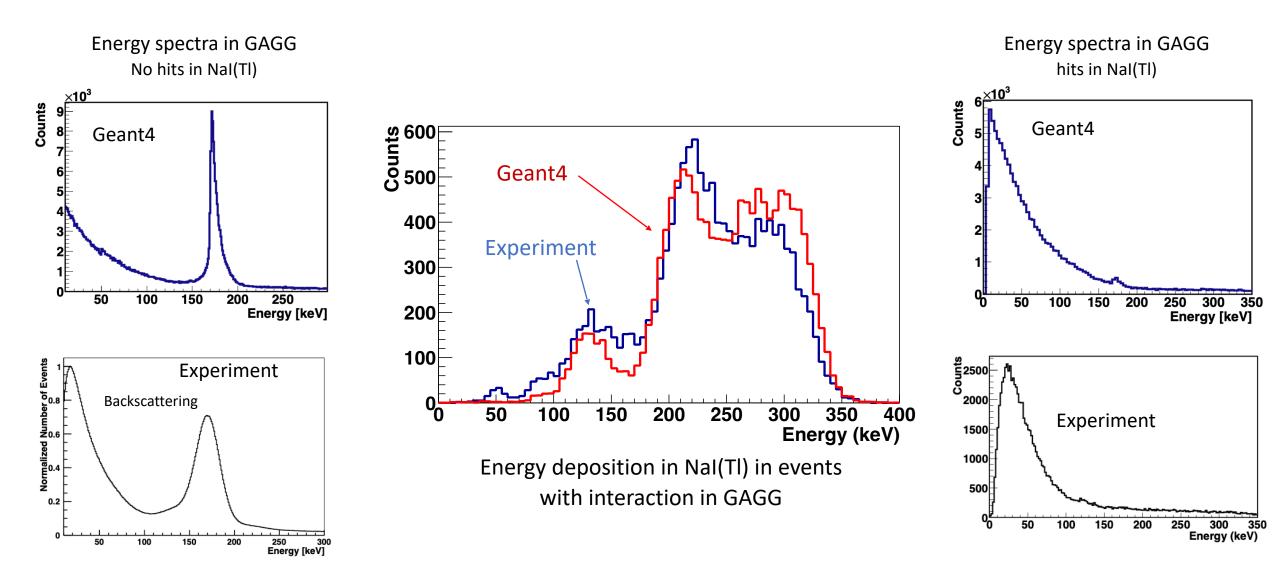
Interaction in the intermediate scatterer leads to the collapse of the entangled state and the development of a decoherent pair (mixed state).



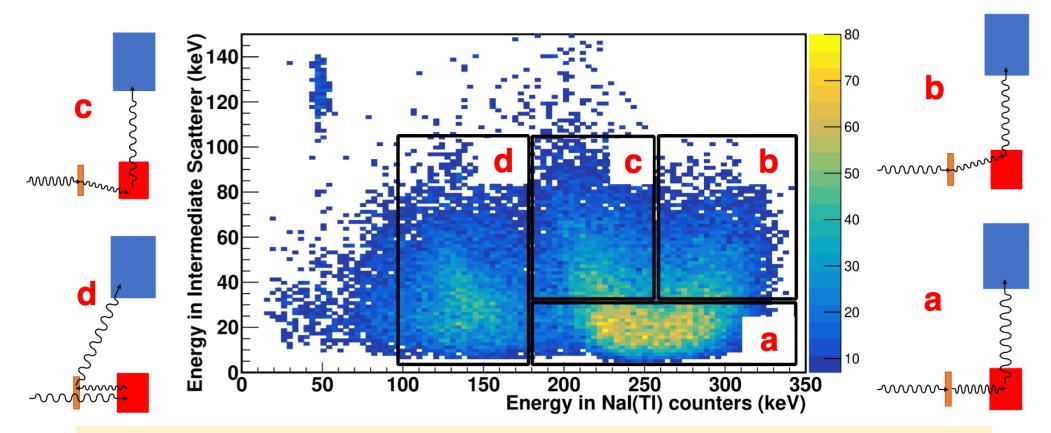
The energy spectra in GAGG scatterer for events inside the true time coincidence peak. The events with hits in NaI(TI) counters are selected here. Insert shows the extended GAGG energy spectrum for all events, regardless of the hits in NaI(TI) counters.

An event is considered decoherent if there is an energy deposition in the GAGG, and the signal is in the required time window.

Event selection with interaction in GAGG

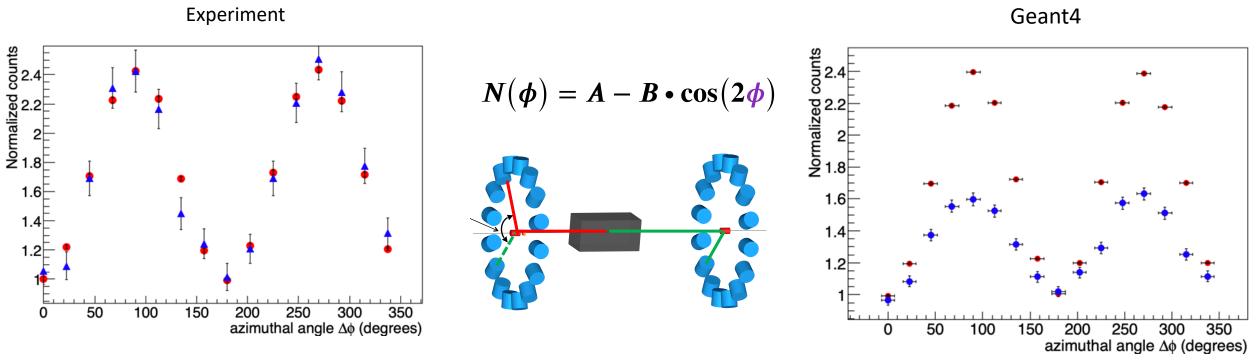


Energy deposition correlation between NaI(TI) and GAGG



Four types of Compton scattering in GAGG: a) scattering at very small angles $\theta < 10^{\circ}$; b) scattering at large angles $10^{\circ} < \theta < 20^{\circ}$ in the direction of NaI(TI); c) scattering at large angles $10^{\circ} < \theta < 20^{\circ}$ in the opposite direction from NaI(TI); d) backscattering at $\theta = 180^{\circ}$.

Angular correlations



Red dots correspond to events with entangled photons Blue dots - decoherent photons.

 $R_{ent} = 2.44 \pm 0.02$

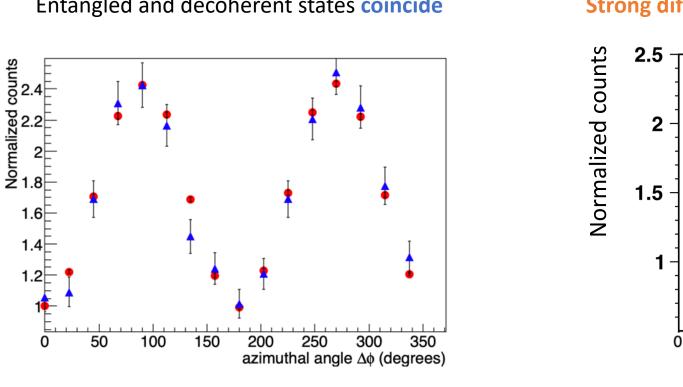
 $R_{dec} = 2.43 \pm 0.15$

 $R_{ent} = 2.399 \pm 0.015$

$$R_{dec} = 1.46 \pm 0.02$$

$$R(\theta) = \frac{N\left(\phi = \frac{\pi}{2}\right)}{N(\phi = 0)} \quad \mathbb{R}_{theory} = 2,6$$

Decoherence puzzle



Entangled and decoherent states coincide

Experimantal data from Watts et al.¹

150

200

250

50

100

Experimantal data from INR RAS

¹Data: Watts, D.P., Bordes, J., Brown, J.R. et al. Photon quantum entanglement in the MeV regime and its application in PET imaging. Nat Commun 12, 2646 (2021); Figure: Sharma, Sushil & Kumar, Deepak & Moskal, Pawel. (2022). Decoherence puzzle in measurements of photons originating from electron-positron annihilation. 10.48550/arXiv.2210.08541.

Strong difference between entangled and decoherent states

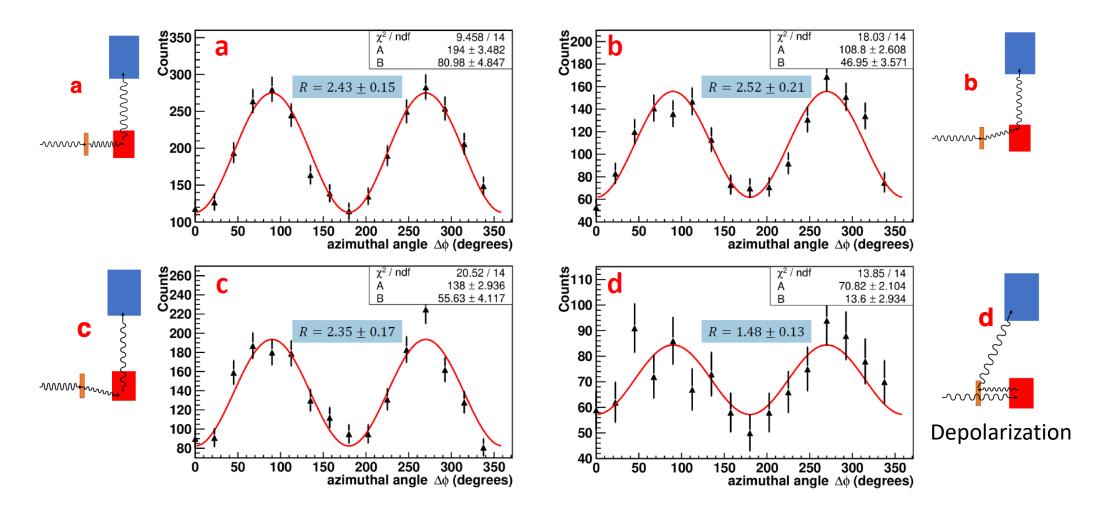
(a)

300

350

 $\Delta \phi$ (degrees)

Angular correlations for decoherent photons



The angular correlations of entangled and decoherent photons coincide for all cases of Compton scattering in experiment, with the exception of backscattering, where photon depolarization occurs.

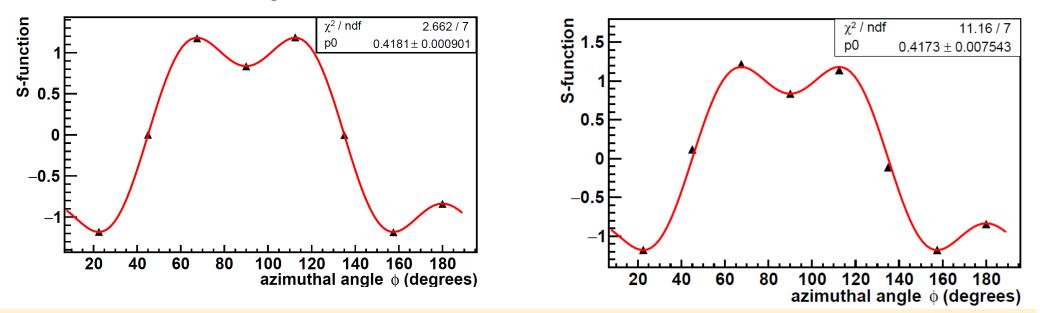
S-function in CHSH inequality

 $S = E\left(\vec{a}, \vec{b}\right) - E\left(\vec{a}, \vec{b}\right) + E\left(\vec{a}, \vec{b}\right) + E\left(\vec{a}, \vec{b}\right) + E\left(\vec{a}, \vec{b}\right) \qquad \Longrightarrow \qquad S = -p_0\left(3\cos(2\phi) - \cos(6\phi)\right) \quad \text{(Theoretical)}$

 P_0 is the product of the efficiencies (analyzing abilities) of two polarimeters.

Entangled:

Decoherent:



In experiment:

 $P_0 = \alpha(\theta_1)\alpha(\theta_2)$ is the same in all event classes.

The correlation functions are identical for the entangled and the mixed state.

Entangled and separable states show the same correlations.

Conclusion

- The high energy of annihilation photons (5 orders of magnitude higher than the energy of optical photons) makes it possible to use a controlled decoherence process and directly compare the polarization correlations of initial and decoherent photons.
- The polarization correlation data turned out to be identical for both quantum states
- A contradiction between the calculations of the current Geant4 model, which describes the kinematics of decoherent photons, and the experimental data is found.
- The entanglement of annihilation photons has not been experimentally proven, since the correlations of initial and decoherent photons coincide.
- The suggested positron emission tomographs using the entanglement of annihilation photons will not be able to suppress the background from parasitic scattering in the studied objects.

Publications:

Setup of Compton polarimeters for measuring entangled annihilation photons

Published in: JINST 17 (2022) 03, P03010 e-Print: <u>2204.04692</u> [physics.ins-det] DOI: <u>10.1088/1748-0221/17/03/P03010</u>

Study of the Compton Scattering of Entangled Annihilation Photons Published in: *Phys.Part.Nucl.Lett.* 19 (2022) 5, 509-512 DOI: <u>10.1134/S1547477122050405</u>

Entanglement of annihilation photons arXiv:2210.07623v1 [quant-ph] 14 Oct 2022

Thank you for your attention





Systematic error study

