Light-nuclei production in heavy-ion collisions at $\sqrt{s_{NN}} = 6.4 - 19.6$ GeV in 3-fluid dynamics

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Introduction

- Light-nuclei production is related to search for critical point in QCD phase diagram.
- There are various 3D dynamical models with coalescence mechanism of the lightnuclei production.
- Microscopic approaches PHQMD and SMASH
- The thermodynamical approach: no additional parameters needed for light-nuclei production.
- THESEUS generator is based on the thermodynamical approach.

Main areas of research: study the light-nuclei production at collision energies of the BES-RHIC, SPS, NICA and FAIR.

3FD model

Target-like fluid: $\partial_{\mu}J_{t}^{\mu}=0$ $\partial_{\mu}T_{t}^{\mu\nu}=-F_{tp}^{\nu}+F_{ft}^{\nu}$ Leading particles carry bar. chargeexchange/emissionProjectile-like fluid: $\partial_{\mu}J_{p}^{\mu}=0$, $\partial_{\mu}T_{p}^{\mu\nu}=-F_{pt}^{\nu}+F_{fp}^{\nu}$ Fireball fluid: $J_{f}^{\mu}=0$, $\partial_{\mu}T_{f}^{\mu\nu}=F_{pt}^{\nu}+F_{tp}^{\nu}-F_{fp}^{\nu}-F_{ft}^{\nu}$ Baryon-free fluidSource termExchangeThe source term is delayed due to a formation time τ

Total energy-momentum conservation: $\partial_{\mu}(T_{p}^{\mu\nu} + T_{t}^{\mu\nu} + T_{t}^{\mu\nu}) = 0$

Physical Input:

- Equation of State
- Friction
- Freeze-out energy density ε_{frz} = 0.4 GeV/fm³

3FD: Yu.B. Ivanov, V.N. Russkikh, V.D. Toneev, PHYSICAL REVIEW C 73, 044904 (2006)

The output = Lagrangian test particles (i.e. fluid droplets) for each fluid α (= p, t or f).

Fluid droplets = elements of freeze-out surface in hydrodynamic models.

Observables = numerically integrating hadron distribution functions over the set of droplets.

EoS:

- hadronic EoS (no phase transition)
- hadronic+QGP EoS with 1st-order PT
- hadronic+QGP EoS with crossover

EoS: A. Khvorostukhin, V.V. Skokov, V.D. Toneev, K. Redlich, EPJ C48, 531 (2006) 3

THESEUS event generator

In 2016 the THESEUS event generator was introduced.

(3FD+Particlization+UrQMD): P. Batyuk et al., PHYSICAL REVIEW C 94, 044917 (2016)

THESEUS = 3FD + Monte Carlo hadron sampling + rescatterings/decays via UrQMD

- There were no light nuclei included.
- THESEUS presents the 3FD output in terms of a set of observed particles.
- Since the time THESEUS was first presented, certain updates have been made, further referred to as THESEUS-v2.

THESEUS-v2: M. Kozhevnikova, Yu. Ivanov, Yu. Karpenko, D. Blaschke, O. Rogachevsky, PRC 103 (2021) 4, 044905

Hydrodynamic modelling of nuclear collisions for NICA / FAIR



THESEUS-v2: updates

No clusters in 3FD originally.

To include light nuclei in thermodynamics, baryon chemical potential should be recalculated.

Recalculation of baryon chemical potential taking into account light nuclei production, proceeding from the local baryon number conservation:

$$n_{\text{primordial }N}(x;\mu_B,T) + \sum_{\text{hadrons}} n_i(x;\mu_B,\mu_S,T)$$
$$= n_{\text{observable }N}(x;\mu'_B,T) + \sum_{\text{hadrons}} n_i(x;\mu'_B,\mu_S,T)$$
$$+ \sum_{\text{nuclei}} n_c(x;\mu'_B,\mu_S,T).$$

The list of light-nuclei species is shown in Table.

$\operatorname{Nucleus}(E[\operatorname{MeV}])$	J	decay modes, in $\%$
d	1	Stable
t	1/2	Stable
$^{3}\mathrm{He}$	1/2	Stable
$^{4}\mathrm{He}$	0	Stable
${}^{4}\text{He}(20.21)$	0	p = 100
${}^{4}\text{He}(21.01)$	0	n = 24, p = 76
${}^{4}\text{He}(21.84)$	2	n = 37, p = 63
${}^{4}\text{He}(23.33)$	2	n = 47, p = 53
${}^{4}\text{He}(23.64)$	1	n = 45, p = 55
${}^{4}\text{He}(24.25)$	1	n = 47, p = 50, d = 3
${}^{4}\text{He}(25.28)$	0	n = 48, p = 52
${}^{4}\text{He}(25.95)$	1	n = 48, p = 52
${}^{4}\text{He}(27.42)$	2	n = 3, p = 3, d = 94
${}^{4}\text{He}(28.31)$	1	n = 47, p = 48, d = 5
${}^{4}\text{He}(28.37)$	1	n = 2, p = 2, d = 96
${}^{4}\text{He}(28.39)$	2	n = 0.2, p = 0.2, d = 99.6
${}^{4}\text{He}(28.64)$	0	d = 100
${}^{4}\text{He}(28.67)$	2	d = 100
4 He(29.89)	2	n = 0.4, p = 0.4, d = 99.2

Table: Stable light nuclei and low-lying resonances of the ⁴He system (from BNL properties of nuclides).

THESEUS-v2: afterburner for light nuclei

There is no UrQMD afterburner stage for light nuclei, so we imitate the afterburner by later freeze-out for light nuclei.

▶ To choose suitable late freeze-out we fit protons by means of the late freeze-out:

 $\varepsilon_{\rm frz} = 0.2 \, {\rm GeV/fm^3}.$

We choose protons because they are closely related to the light nuclei.



Fig.: Transverse-momentum spectra of protons in central Au+Au collisions.

THESEUS-v2: rapidity distributions, $\varepsilon_{\rm frz} = 0.2 \, {\rm GeV}/{\rm fm}^3$.



Resonances of ⁴He are unimportant in midrapidity at the considered collision energies. **Puzzle:** reproduction of the ³He data is better than that of deuterons, in spite of that ³He heavier.

Particle ratios





Fig.: Energy dependence of d/p, t/p, and t/d midrapidity ratios for central (0-10%) Au+Au collisions. Simulations were performed at b = 4 fm for Au+Au and at b = 3 fm for Pb+Pb in rapidity bin |y| < 0.5. **Fig.:** Energy dependence of the midrapidity light-nuclei yield ratio $N(t) \times N(p)/N^2(d)$ in central Au+Au and Pb+Pb collisions. Simulations at b = 4 fm for Au+Au, at b = 3 fm ($\sqrt{s_{NN}} < 17.4$ GeV) and b = 4.6 fm ($\sqrt{s_{NN}} = 17.4$ GeV) for Pb+Pb in rapidity bin |y| < 0.5. N(p) is related to protons without feed-down from weak decays.

Observed growth near 20 GeV resembles the result of feed-down from weak decays into proton yield.

Summary

- The thermodynamical approach approximately reproduces data on light nuclei with a single parameters, $\varepsilon_{\rm frz} = 0.2 \, {\rm GeV/fm^3}$
- The functional dependencies (on y, p_T, centrality, mass of light nuclei) qualitatively are reproduced
- > There is a puzzle with v_1 of deuterons
- Imperfect reproduction of the light-nuclei data leaves room for medium effects

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Three-fluid dynamics (3FD) model

The 3FD approximation simulate the early, nonequilibrium stage of the strongly-interacting matter:

- baryon-rich fluids: nucleons of the projectile (p) and the target (t) nuclei;
- fireball (f) fluid: newly produced particles which dominantly populate the midrapidity region.





momentum along beam

THESEUS-v2: m_T -spectra of protons.



 m_T -spectra of protons: thermodynamics works good with soft particles and with hard particles not perfect.

m_T -spectra: deuterons and Helium 3



Small disagreement with proton m_T data transforms into a large disagreement with data on light nuclei.

Directed flow $v_1(y)$

The single particle distribution function:

$$E\frac{d^{3}N}{d^{3}p} = \frac{1}{2\pi} \frac{d^{2}N}{p_{T}dp_{T}dy} (1 + \sum_{n=1}^{\infty} 2v_{n}\cos(n(\phi - \Psi_{\rm RP})))$$

The first coefficient of Fourier expansion, i.e. **directed flow**:

$$v_1^{(a)}(y) = \frac{\int d^2 p_T \left(p_x/p_T \right) E \, dN_a/d^3 p}{\int d^2 p_T E \, dN_a/d^3 p}.$$
 $v_1 = \langle \cos \phi \rangle$, where ϕ – azimuthal angle.

In THESEUS: $v_1(y)$ is calculated in terms of sums over hadrons rather than integrals over momenta.

Directed flow $v_1(y)$: protons and deuterons



Fig.: Directed flow of **deuterons** (upper raw of panels) and **protons** (lower raw of panels) as function of rapidity in semicentral (b = 6 fm) Au+Au collisions.

Nearest plans

- Study of v_1 puzzle for deuterons: p_T -differential $v_1(p_T)$;
- Including medium effects;
- Predictions for NICA energies;
- HADES and AGS data;
- Hyper-(anti)nuclei.