

# The estimation methods of the background induced by the misidentification of a jet as a photon in $pp$ collisions at $\sqrt{s} = 13$ TeV with the ATLAS Detector

K. Kazakova, E. Soldatov, D. Pyatiizbyantseva  
on behalf of the ZnunuGamma group



MEPhI@Atlas meeting  
25/11/2022

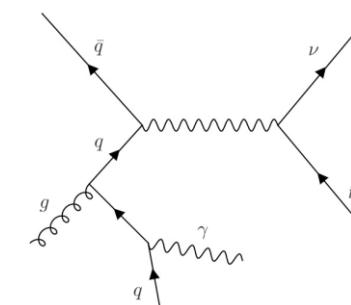
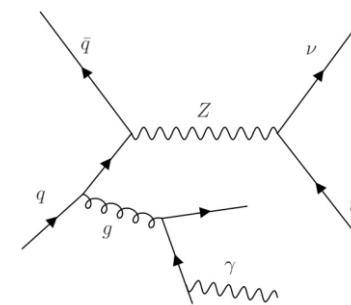
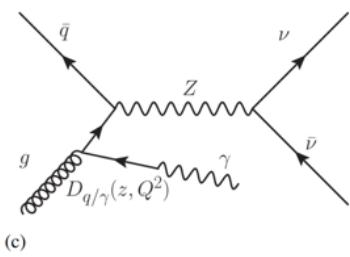
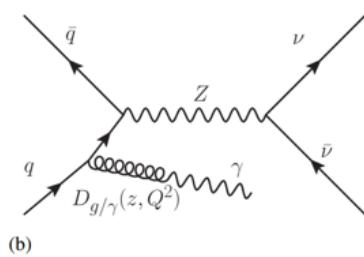


# Questions raised at the last meeting

1. Why the pseudorapidity of the photon is chosen for differential cross-section derivation? Why not the pseudorapidity of Z-boson for instance? Are they different? Is it better to use photon rapidity?

The pseudorapidity of Z boson is not applicable. Pseudorapidity and rapidity of a photon are the same since the photon is massless.

2. Are Feynman diagrams b) and c) correct? No.

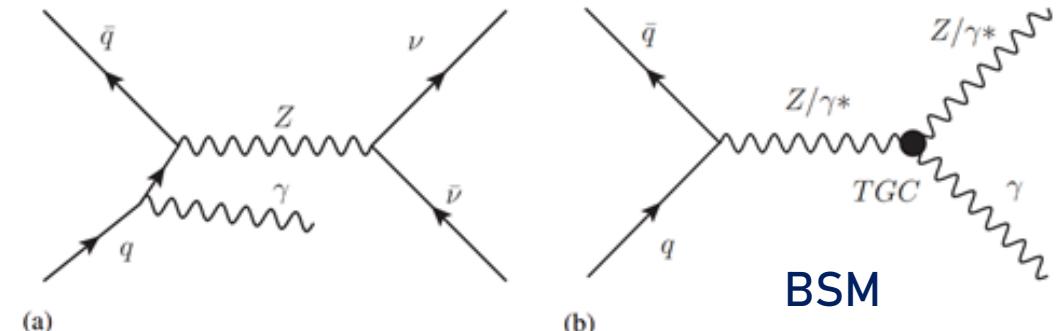


3. Double counting of t $\bar{t}\gamma$ . Lepton selection in Wy CR? The final states of t $\bar{t}\gamma$  decay are: 2l 2v 2j  $\gamma$  (unique final state), l v $\gamma$ +4j (is not generated),  $\gamma$  + 6j (is not generated).
4. Why do we compare the shapes of  $jet \rightarrow \gamma$  distribution in Z $\gamma$  QCD if we don't trust MC  $jet \rightarrow \gamma$ ? There is a plan to apply the slice method to the shape estimation.
5. Systematic coming from the choice of the variable. Fixed.
6. To make regions orthogonal. Yes it is planned.

# Motivation and goals

## Motivation:

- To measure the parameters of the Standard Model (SM) to very high precision;
- The search of new physics predicted by the beyond SM (BSM) theories;
- Precise measurements of triple and quartic gauge couplings sensitive to BSM physics. One of the sensitive processes is  $Z(vv)\gamma$  process.



## Goals:

- To calculate integral and differential in  $E_T^\gamma$ ,  $N_{\text{jets}}$ ,  $p_T^{\text{miss}}$ ,  $\Delta\phi(\gamma, p_T^{\text{miss}})$ ,  $p_T(Z\gamma)$ ,  $\eta_\gamma$ . cross-sections and compare the results with the theory predictions;
- To obtain the strongest up-to-date limits on anomalous neutral triple gauge-boson couplings (aTGCs).

→ We want to estimate backgrounds as accurate as possible but background processes emerging from object misidentification **are not well-modeled in Monte-Carlo**. All analyses at the LHC experiments use data-driven methods to solve this issue.

# The backgrounds and the phase space definition

Signal:  $Z(vv)\gamma$

Backgrounds:

- 35% •  $\gamma + \text{jets}$  – via MC → ABCD method based on  $E_T^{\text{miss}}$  significance and additional variable (or slice method?);
  - 26% •  $W(\rightarrow l\nu)\gamma$  – fit to data in additional CR based on  $N_{\text{lep}}$  (shape from MC);
  - 20% •  $e \rightarrow \gamma$  – fake-rate estimation using Z-peak (tag-n-probe) method;
  - 14% •  $jet \rightarrow \gamma$  – ABCD method based on photon ID and isolation and slice method;
  - 1.9% •  $Z(l\bar{l})\gamma$  – via MC;
  - 1.6% •  $t\bar{t}\gamma$  – via MC.
- FixedCutLoose isolation working point is chosen.

## Preselections

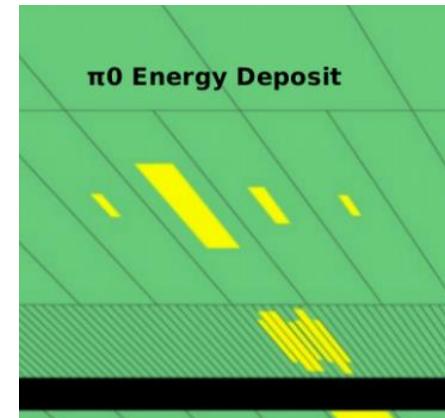
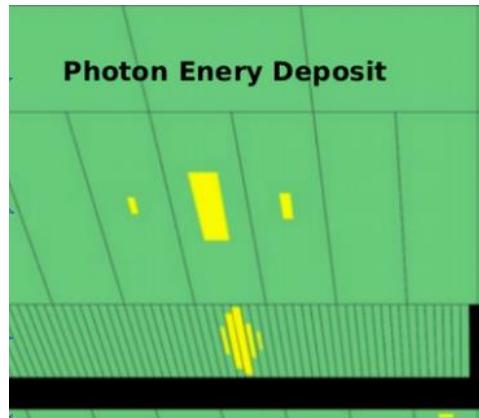
Preselections	Cut value
$E_T^{\text{miss}}$	$> 130 \text{ GeV}$
$E_T^\gamma$	$> 150 \text{ GeV}$
Number of photons	$N_\gamma = 1$
Lepton veto	$N_e = 0, N_\mu = 0$

## Selections

Selections	Cut value
$E_T^{\text{miss}}$ significance	$> 11$
$ \Delta\phi(E_T^{\text{miss}}, \gamma) $	$> 0.7$
$ \Delta\phi(E_T^{\text{miss}}, j_1) $	$> 0.4$

# jet $\rightarrow \gamma$ background

- The background induced by the misidentification of a jet as a photon is studied in this analysis.



Hadronic jets in which neutral mesons carry a significant fraction of energy may be misidentified as isolated photons.

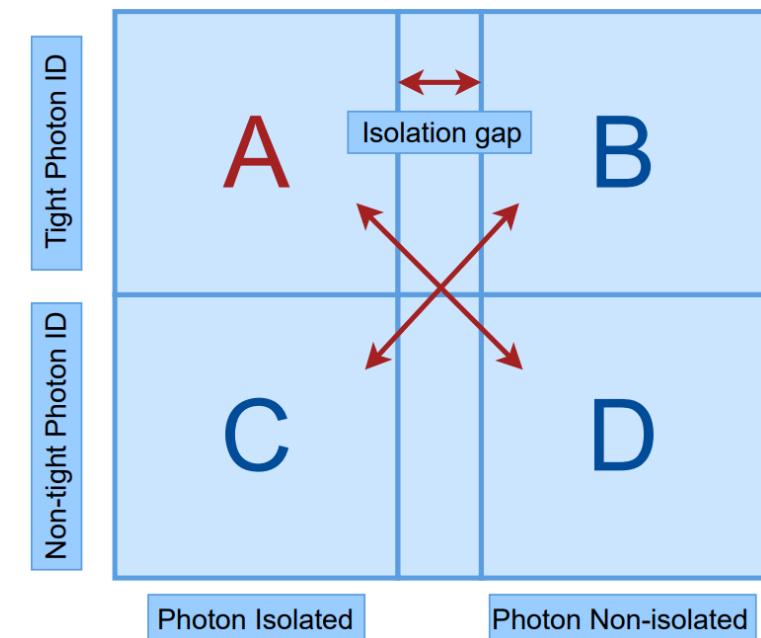
→ the SR will be contaminated with  $jet \rightarrow \gamma$

## ABCD method for $jet \rightarrow \gamma$ :

- the phase space is splitted into 4 regions based on the identification (*tight or loose'*) and isolation (*isolated or non-isolated*) criteria for photons;
- the main assumption is the absence of correlation between identification and isolation criteria.

The estimate of  $jet \rightarrow \gamma$  events in signal region A derived by ABCD method is  $2100 \pm 100 \pm 300$

→ A large uncertainty is observed. Thus, we have a motivation to estimate  $jet \rightarrow \gamma$  with other methods.

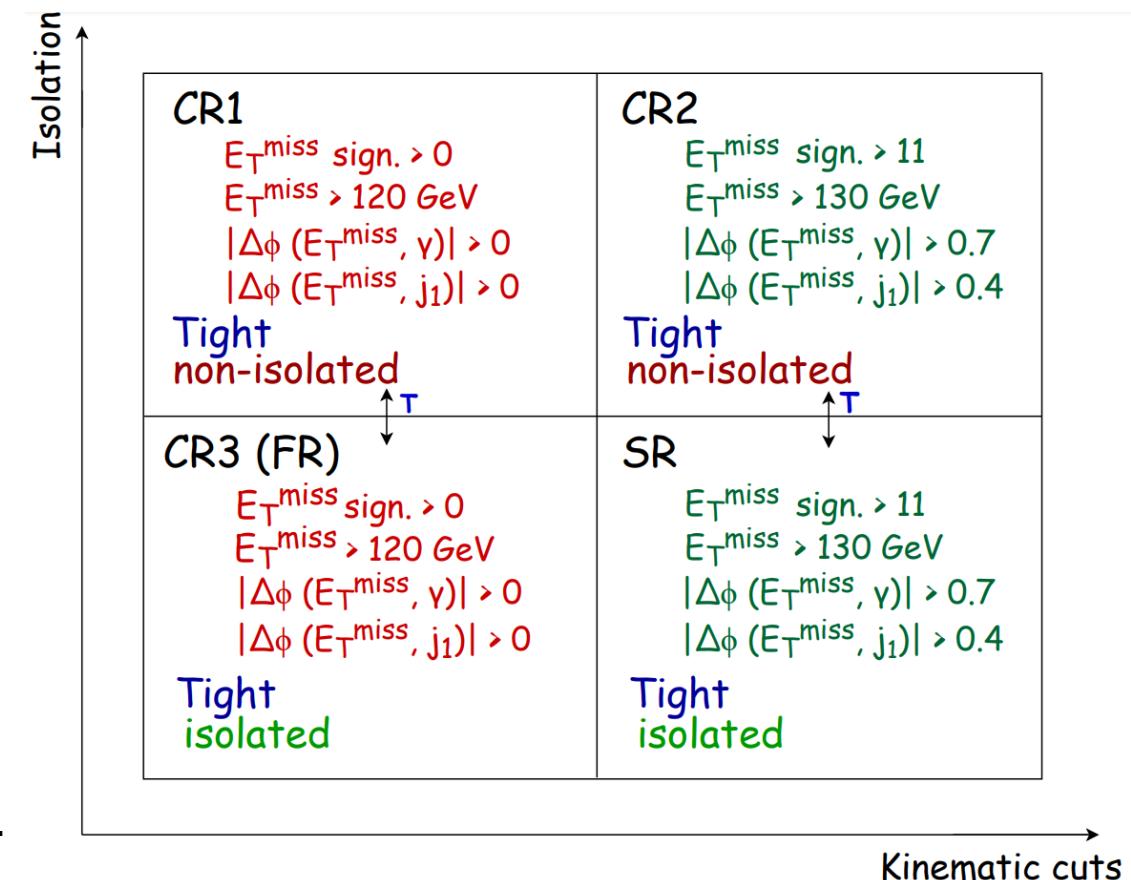


More details in back-up

# Estimation techniques of the slice method I

## Strategy:

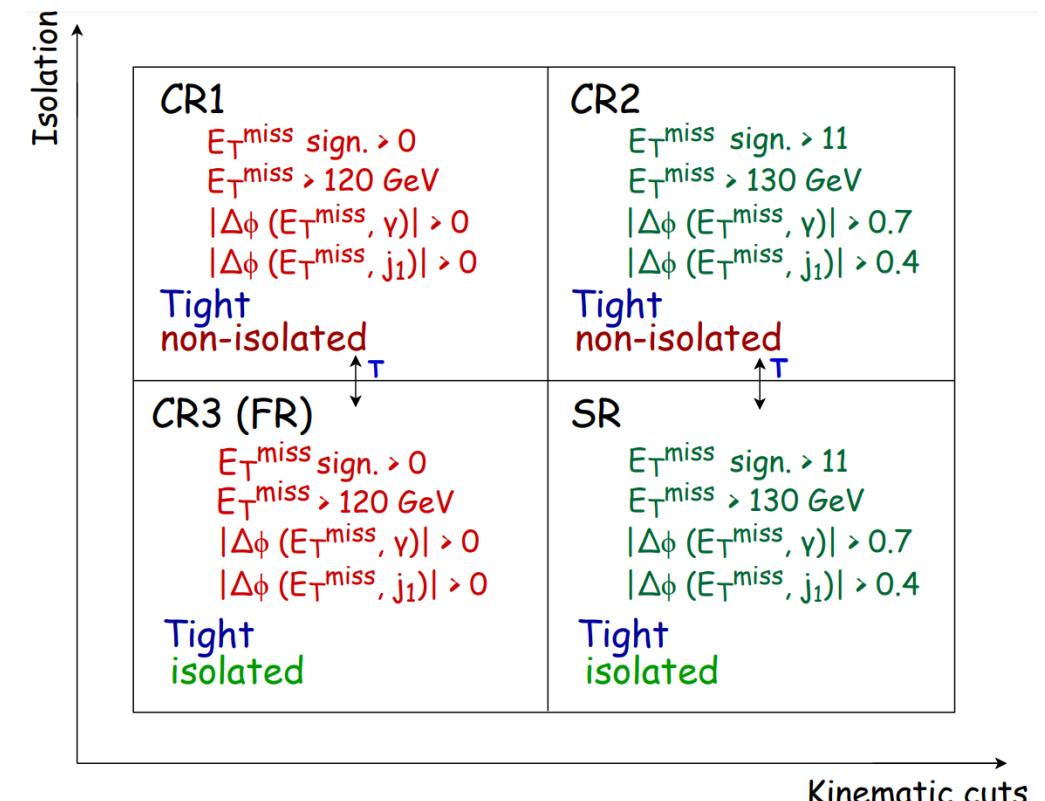
1. Split the phase space into 4 regions based on kinematic cuts and isolation. The fit region (FR) is a region with relaxed cuts on several variables, where events have a **leading photon candidate that is isolated**. The SR is a subset of the FR, events in the SR pass all signal kinematic selections.
2. The CR1 is a region with relaxed cuts on several variables, where events have a **leading photon candidate that is not isolated**. The CR2 is a subset of the CR1, events in CR2 pass all signal kinematic selections.
3. Photons in all four regions pass the **tight** selection criteria.
4. The fit is performed in the FR, where the  $jet \rightarrow \gamma$  process used for the fit is derived from CR1. The relaxed cuts in the FR and the CR1 are applied to dispose of enough statistics.
5. Photon is required to pass  $p_T^{\text{cone}20}/p_T^\gamma < 0.05$  track isolation in isolated regions. To increase the statistics in non-isolated regions the inverted track isolation  $p_T^{\text{cone}20}/p_T^\gamma > 0.05$  is applied.



# Estimation techniques of the slice method II

6. The fit can be performed for different variables in the phase-space region with relaxed cuts on these variables.
7. To study the dependence of the result on the isolation criteria, control regions CR1 and CR2 are split into successive intervals by the isolation variable, instead of a single integrated anti-isolated region.
8. In this way, the number of  $jet \rightarrow \gamma$  background events for a given isolation slice  $i$  can be estimated as follows:

$$N_{\text{CR1}(i)}^{jet \rightarrow \gamma} = N_{\text{CR1}(i)}^{\text{data}} - N_{\text{CR1}(i)}^{Z(\nu\bar{\nu})\gamma} - N_{\text{CR1}(i)}^{\text{bkg}}$$



9. The fit is performed in the FR. Thus, the total number of events in the FR estimated from non-isolated slice of the CR1 is given by:

$$N_{\text{FR}(i)}^{\text{data}} = \alpha \cdot (N_{\text{FR}(i)}^{Z(\nu\bar{\nu})\gamma} + N_{\text{FR}(i)}^{\text{bkg}}) + N_{\text{FR}(i)}^{jet \rightarrow \gamma}$$

10. The fitting parameter  $T_{(i)}$  gives the estimated number of  $jet \rightarrow \gamma$  events in the FR:  $N_{\text{FR}(i)}^{jet \rightarrow \gamma} \approx T_{(i)} \cdot N_{\text{CR1}(i)}^{jet \rightarrow \gamma}$

# Estimation techniques of the slice method III

11. In this study, a parameter  $\alpha$  is taken to be equal 1. The fit parameter  $T_{(i)}$  is derived for each slice and kinematic variable.
12. Finally, the fitted  $jet \rightarrow \gamma$  yield is extrapolated to the signal region. The estimate for each slice and kinematic variable is determined by the equation:

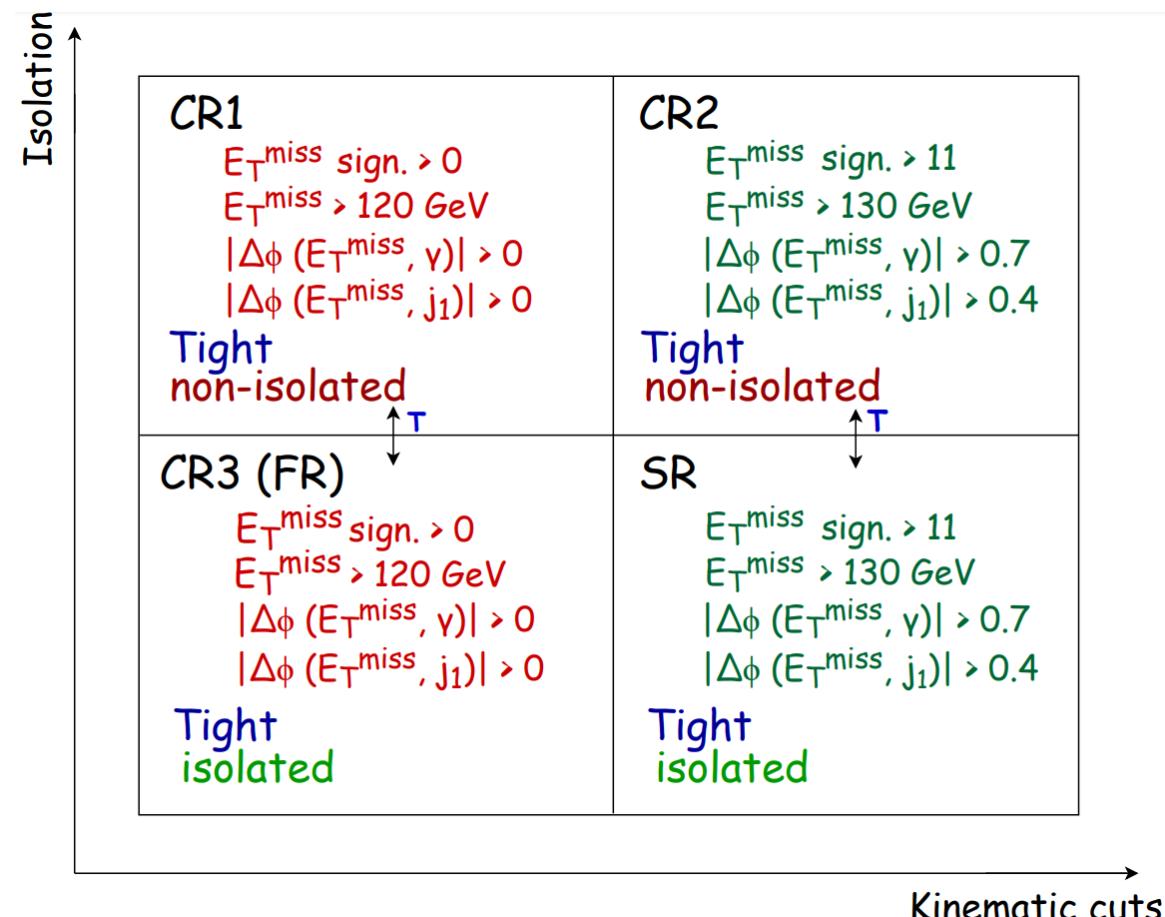
$$N_{SR(i)}^{jet \rightarrow \gamma} = T_{(i)} \cdot (N_{CR2(i)}^{\text{data}} - N_{CR2(i)}^{Z(\nu\bar{\nu})\gamma} - N_{CR2(i)}^{\text{bkg}})$$

- FixedCutLoose isolation working point is chosen.  
Isolation working point is defined as:

$$E_T^{\text{cone}20}/p_T^\gamma < 0.065$$



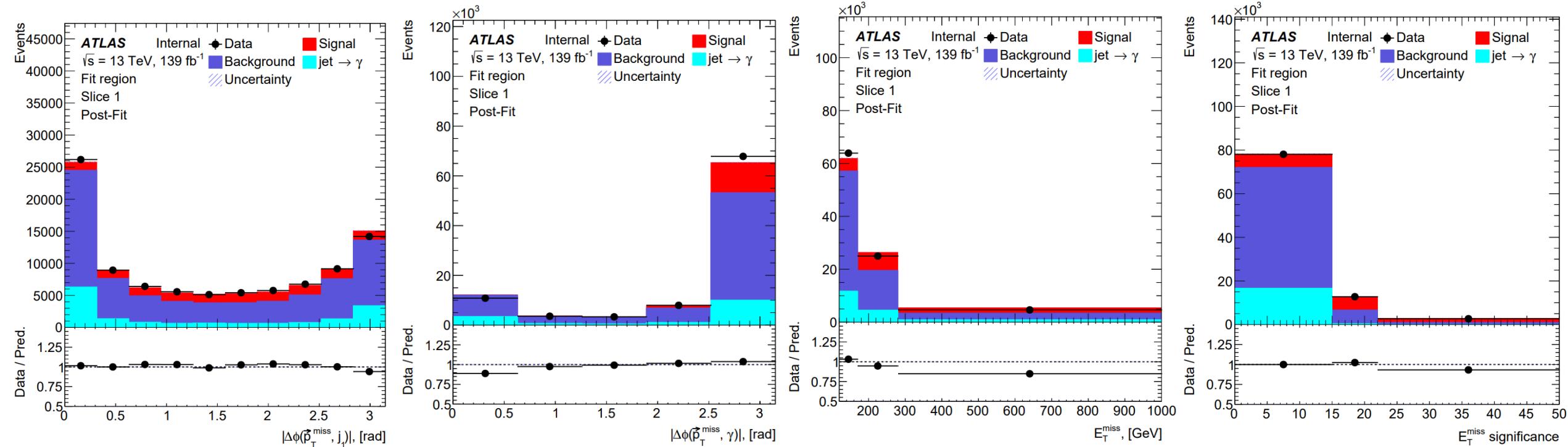
Five isolation slices are chosen: [0.065, 0.08, 0.095, 0.115, 0.14]



# Fit process

- The fit was performed for 4 variables:  $E_T^{\text{miss}}$ ,  $E_T^{\text{miss}}$  significance ,  $|\Delta\phi(\gamma, \vec{p}_T^{\text{miss}})|$  and  $|\Delta\phi(j_1, \vec{p}_T^{\text{miss}})|$
- The fitting parameter  $T_{(i)}$  is derived from the fit for each slice and variable.

The results of the fit for slice 1 [0.065, 0.08]:



Pre-fits and post-fits for other slices are performed in back-up

# The results of the fit

Result of the fit for Z $\gamma$  QCD Sherpa generator:

Slice	$T_1, E_T^{\text{miss}}$	$T_2, E_T^{\text{miss}}$ sign.	$T_3,  \Delta(E_T^{\text{miss}}, j_1) $	$T_4,  \Delta(E_T^{\text{miss}}, \gamma) $
1	$3.80 \pm 0.07$	$3.82 \pm 0.08$	$3.73 \pm 0.08$	$3.51 \pm 0.07$
2	$4.63 \pm 0.10$	$4.58 \pm 0.09$	$4.37 \pm 0.09$	$4.01 \pm 0.08$
3	$4.87 \pm 0.10$	$4.77 \pm 0.10$	$4.49 \pm 0.10$	$4.08 \pm 0.09$
4	$6.06 \pm 0.12$	$5.91 \pm 0.12$	$5.48 \pm 0.12$	$4.80 \pm 0.11$
5	$2.37 \pm 0.05$	$2.30 \pm 0.05$	$1.91 \pm 0.04$	$1.54 \pm 0.04$

The fit parameters  $T_{(i)}$

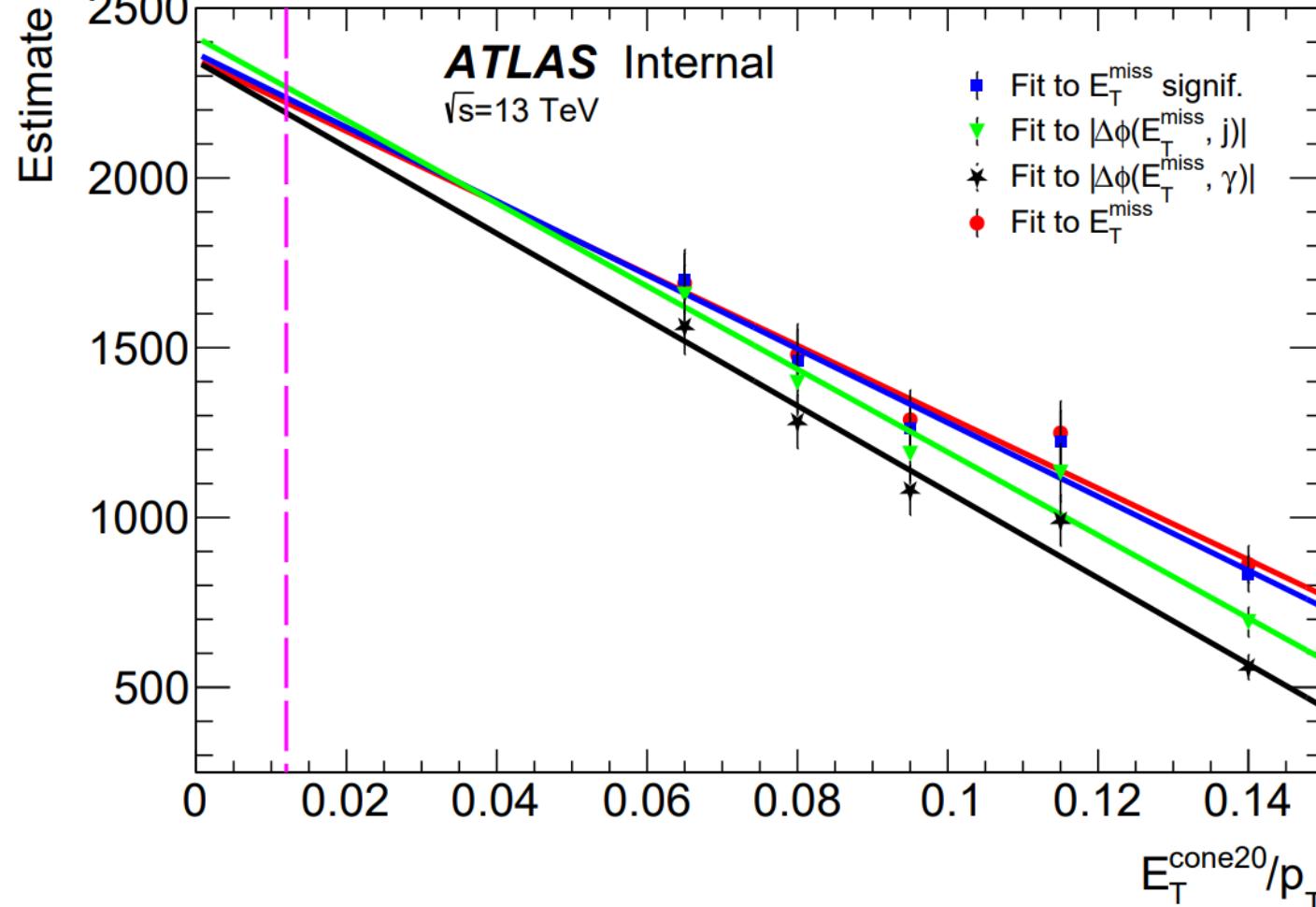
Slice	Observed $N_{CR2(i)}^{jet \rightarrow \gamma}$
1	$444 \pm 22$
2	$320 \pm 19$
3	$265 \pm 17$
4	$207 \pm 15$
5	$363 \pm 22$

Observed  $jet \rightarrow \gamma$  events in the CR2

Slice	$N_{SR(i)}^{jet \rightarrow \gamma}, E_T^{\text{miss}}$	$N_{SR(i)}^{jet \rightarrow \gamma}, E_T^{\text{miss}}$ sign.	$N_{SR(i)}^{jet \rightarrow \gamma},  \Delta(E_T^{\text{miss}}, j_1) $	$N_{SR(i)}^{jet \rightarrow \gamma},  \Delta(E_T^{\text{miss}}, \gamma) $
1	$1690 \pm 88$	$1700 \pm 89$	$1656 \pm 87$	$1562 \pm 82$
2	$1479 \pm 91$	$1463 \pm 90$	$1397 \pm 87$	$1282 \pm 79$
3	$1288 \pm 87$	$1262 \pm 85$	$1188 \pm 80$	$1080 \pm 73$
4	$1249 \pm 94$	$1222 \pm 92$	$1132 \pm 86$	$991 \pm 75$
5	$862 \pm 55$	$834 \pm 53$	$692 \pm 44$	$559 \pm 37$

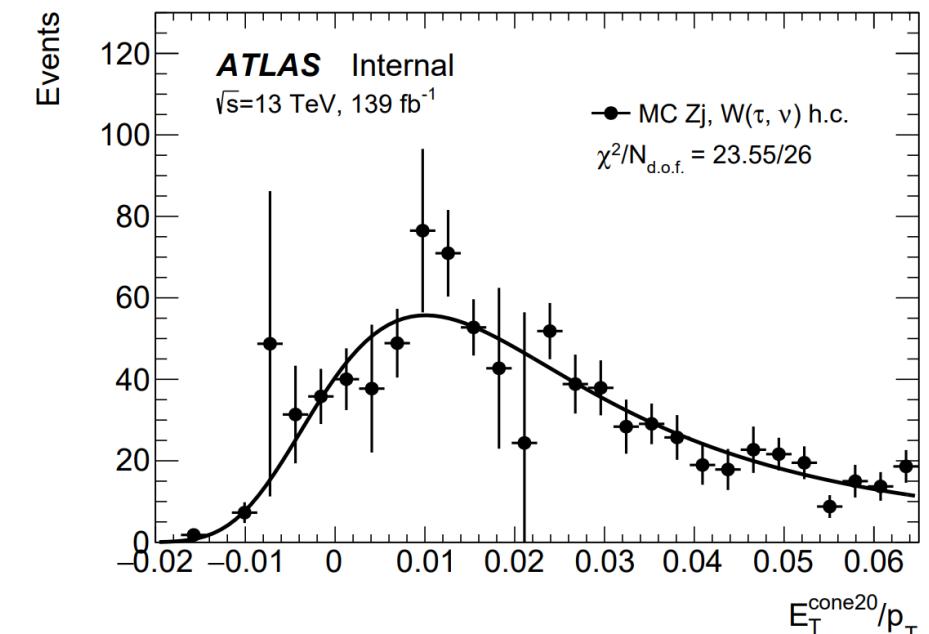
$jet \rightarrow \gamma$  events in the SR for each slice

# Linear extrapolation



- The estimate of  $\text{jet} \rightarrow \gamma$  background is  $2220 \pm 60$  events.

Isolation distribution for  $\text{jet} \rightarrow \gamma$  MC samples



Landau fit  $\Rightarrow X = 0.012 \pm 0.010$

$\chi^2/N_{\text{d.o.f.}}$  for Gaus fit is  $92.78/26$

Variable	Estimate in $x = 0.012$
$E_T^{\text{miss}}$	$2220 \pm 140$
$E_T^{\text{miss}}$ sign.	$2240 \pm 130$
$ \Delta(E_T^{\text{miss}}, j_1) $	$2270 \pm 130$
$ \Delta(E_T^{\text{miss}}, \gamma) $	$2190 \pm 110$

$$\bar{X} = \frac{\sum \frac{x_i}{\sigma_i^2}}{\sum \frac{1}{\sigma_i^2}}$$

# The sources of the systematics

Systematic uncertainties come from:

- The uncertainty in the choice of the extrapolation target for the isolation scan, estimated by changing the isolation target by  $\pm 1\sigma$ ;
- The uncertainty comes from different generators.
- The uncertainty comes from the choice of the variable. (30 events)

Variable	Estimate in $x = 0.002$
$E_T^{\text{miss}}$	$2330 \pm 140$
$E_T^{\text{miss}}$ sign.	$2350 \pm 130$
$ \Delta(E_T^{\text{miss}}, j_1) $	$2390 \pm 130$
$ \Delta(E_T^{\text{miss}}, \gamma) $	$2320 \pm 110$

→ 2345 events,  $\delta = 122$  events

Variable	Z $\gamma$	QCD	MadGraph
$E_T^{\text{miss}}$	$2440 \pm 140$		
$E_T^{\text{miss}}$ sign.	$2390 \pm 140$		
$ \Delta(E_T^{\text{miss}}, j_1) $	$2430 \pm 130$		
$ \Delta(E_T^{\text{miss}}, \gamma) $	$2370 \pm 120$		

→ 2403 events,  $\delta = 180$  events

- Total systematic uncertainty is 220 events.
- Thus, the estimate of  $jet \rightarrow \gamma$  events in signal region A by slice method is  $2220 \pm 60 \pm 220$ .
- The estimate of  $jet \rightarrow \gamma$  events in signal region A derived by ABCD method is  $2100 \pm 100 \pm 300$ .
- The final estimates for different methods coincide within the uncertainty.

# Likelihood-based approach I

- **The main idea:** to fit signal and other backgrounds distributions except jet → γ to data in all ABCD regions

The essence of the method is to perform a fit of the likelihood function, which is defined as:

$$L(N_{ji}|f_{F_{ji}}, f_{N_j}) = \prod_{j=A}^{B,C,D} \prod_{i=1}^{N_{bins}} \text{Pois}(N_{ji}|\nu_{b_{ji}} + \nu_{\gamma_{ji}}f_{F_{ji}} + \nu_{s_{ji}}f_{N_j})$$

where model parameters are defined as:

- $N_{ji}$  – the number of the data events in each region and bin;
- $f_{N_j}$  – varying parameter for signal in each region;
- $f_{F_{ji}}$  – varying parameter for estimated background in each region and bin;
- $\nu_{b_{ji}}$  – the number of events in MC backgrounds (excl. jet → γ );
- $\nu_{s_{ji}}$  – the number of signal events;
- $\nu_{\gamma_{ji}}$  – the number of estimated background (jet → γ ) events.

# Likelihood-based approach II

- Likelihood based approach is constructed with the assumption that  $R = 1$  for each bin in the distribution for jet  $\rightarrow \gamma$  background:

$$1 = \frac{\nu_{\gamma A_i} f_{F_{Ai}} \cdot \nu_{\gamma D_i} f_{F_{Di}}}{\nu_{\gamma B_i} f_{F_{Bi}} \cdot \nu_{\gamma C_i} f_{F_{Ci}}}$$

- To avoid the redundancy of the model the following limitation is applied:  $f_{F_{Bi}} = f_{F_{Di}}$

The search of maximum of likelihood function is performed with **RooFit** toolkit:

$$\frac{\partial L}{\partial f_{F_{ji}}} = 0, \quad \frac{\partial L}{\partial f_{N_j}} = 0$$

This way the number of jet  $\rightarrow \gamma$  events in **SR**:

$$N_A^{jet \rightarrow \gamma} = \nu_{\gamma A_i} f_{F_{Ai}}$$

- The proposed method significantly reduces the number of steps to be done to obtain the estimate compared to ABCD-method

# MC samples

- The likelihood-based approach is applied to associated  $Z\gamma$  production with Z-boson decaying into neutrinos ( $Z \rightarrow \nu\nu$ ). One of the backgrounds comes from  $\gamma+j$  events.  $Zj$  events come from jet  $\rightarrow \gamma$  misidentification
- The processes considered in the analysis are generated in MadGraph5 MC event generator using pp collisions with  $\sqrt{s} = 13$  TeV and the integrated luminosity of  $139 \text{ fb}^{-1}$
- Pythia8 is used for parton showering and hadronization, Delphes is used for detector simulation.

Selection	Cut value
$E_T^{\text{miss}}$	$> 130 \text{ GeV}$
$E_T^\gamma$	$> 150 \text{ GeV}$
Number of tight photons	$N_\gamma = 1$
Lepton veto	$N_e = 0, N_\mu = 0$

Event selection criteria for  
 $Z\gamma$  candidate events

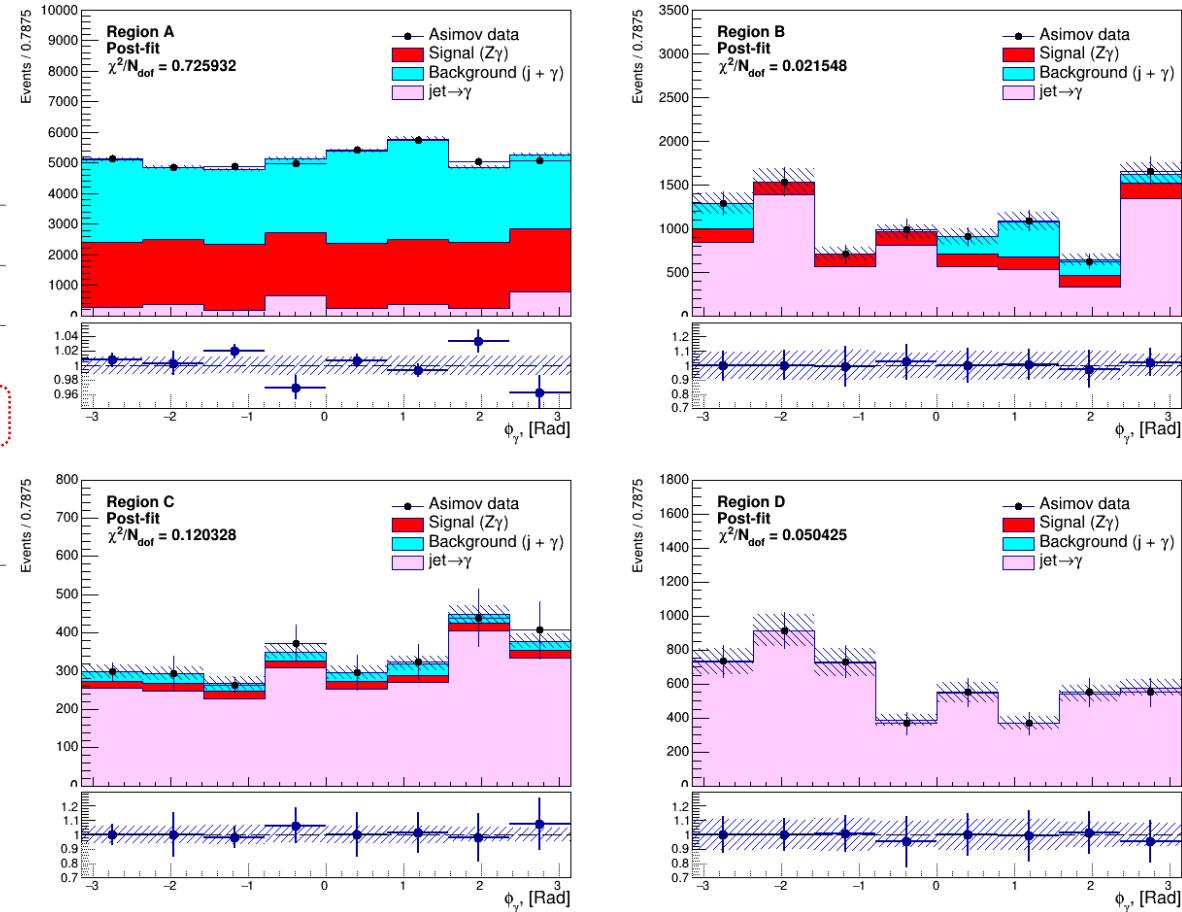
Thus the study uses Asimov data which is not real data but the sum of MC generated processes, the likelihood-based estimate of jet  $\rightarrow \gamma$  background and MC prediction should coincide. It is so-called «closure test».

# The results of the fit

The fit was performed for  $\phi_\gamma$  and  $\eta_\gamma$ :

The final estimate is chosen based on the  $\chi^2/N_{d.o.f.}$  value in the SR and R-factor.

$N_{bins}$	$\phi_\gamma$			$\eta_\gamma$		
	Estimate	R-factor	$\chi^2/N_{d.o.f.}$	Estimate	R-factor	$\chi^2/N_{d.o.f.}$
6	$3255^{+111}_{-106}$	$1.04 \pm 0.03$	0.45	$3238^{+129}_{-125}$	$1.03 \pm 0.03$	0.39
7	$2906^{+110}_{-108}$	$0.94 \pm 0.03$	0.73	$3243^{+126}_{-122}$	$1.04 \pm 0.02$	0.55
8	$3179^{+117}_{-108}$	$1.04 \pm 0.03$	0.73	$3276^{+141}_{-137}$	$1.04 \pm 0.02$	0.26
9	$3119^{+130}_{-127}$	$1.01 \pm 0.03$	0.62	$3251^{+133}_{-130}$	$1.05 \pm 0.02$	0.50



- The systematic uncertainties were derived by
  - variating the value of isolation gap by  $\pm\sigma$  in non-isolated control regions.
- The estimate of  $\text{jet} \rightarrow \gamma$  events in SR obtained by likelihood method is  $N_A^{\text{jet} \rightarrow \gamma} = 3179^{+117}_{-108} \pm 69$  for  $\phi_\gamma$  and  $N_A^{\text{jet} \rightarrow \gamma} = 3243^{+126}_{-122} \pm 48$  for  $\eta_\gamma$
- The MC prediction is  $N_A^{\text{jet} \rightarrow \gamma} = 3093 \pm 178$  events

# Summary

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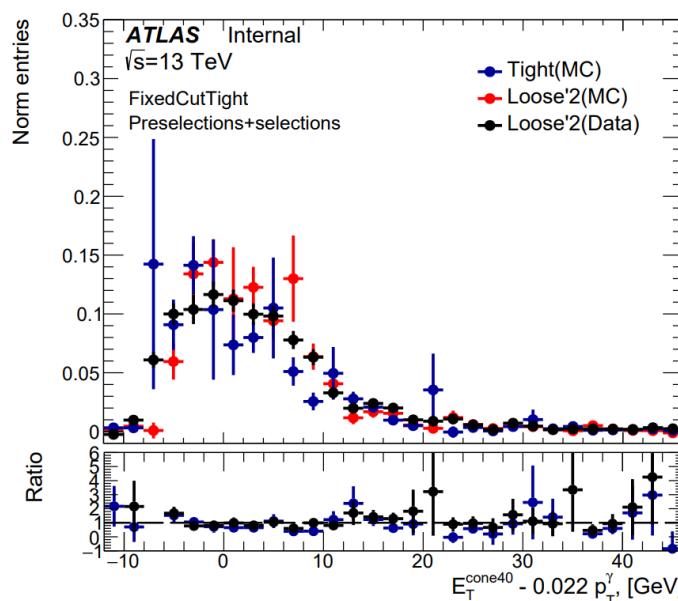
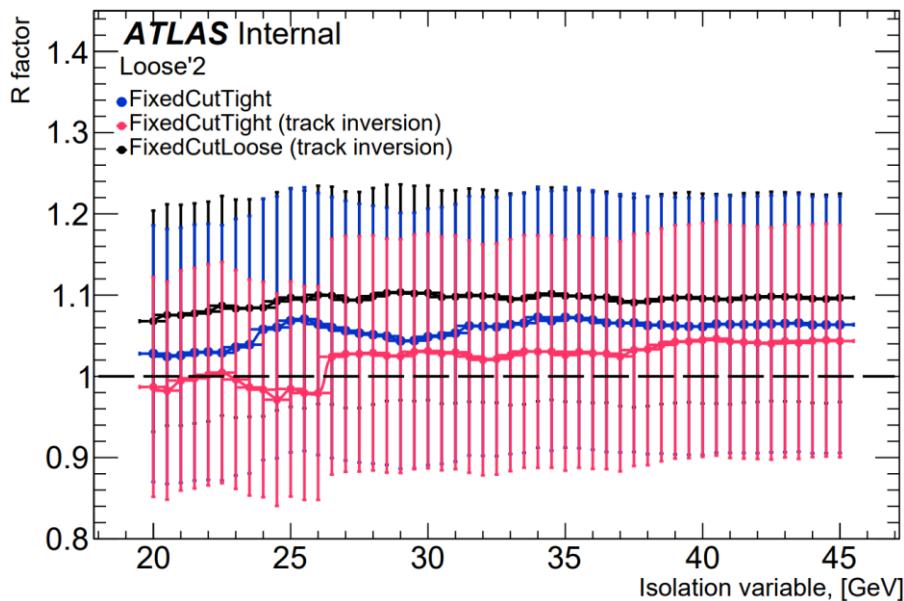
- The estimate of  $jet \rightarrow \gamma$  events in signal region A is derived by ABCD method. The estimate is  $2100 \pm 100 \pm 300$  events.
- The alternative slice method is performed for  $jet \rightarrow \gamma$  estimation process. The estimate of  $jet \rightarrow \gamma$  events in signal region A derived by slice method is  $2220 \pm 60 \pm 220$ . The final estimates for the methods coincide within the uncertainty.
- The alternative likelihood-based method of estimation of  $jet \rightarrow \gamma$  events was developed. It uses the information about the shape of the distributions in the regions and provides a much simpler way to obtain the estimate of the number of background events.

Thank you for your attention!

**BACK-UP**

# R factor Zj and W( $\tau\nu$ ) in MC

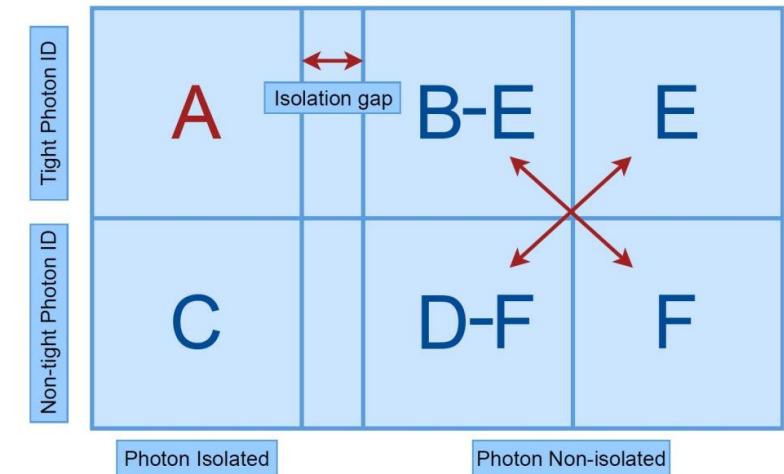
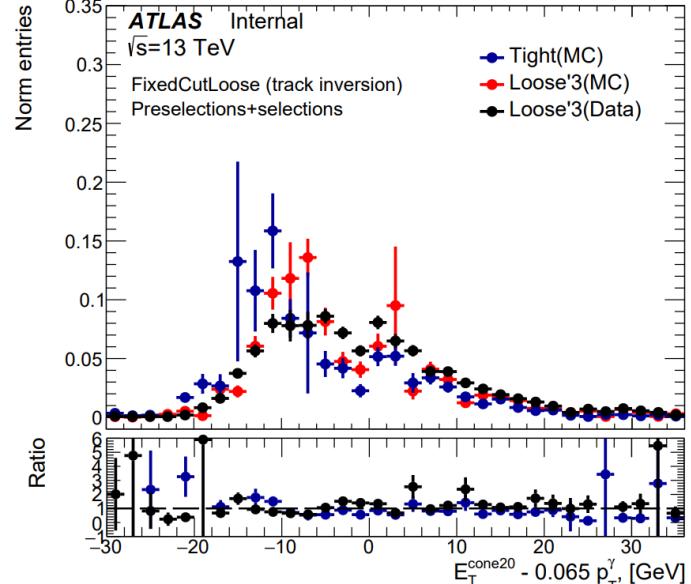
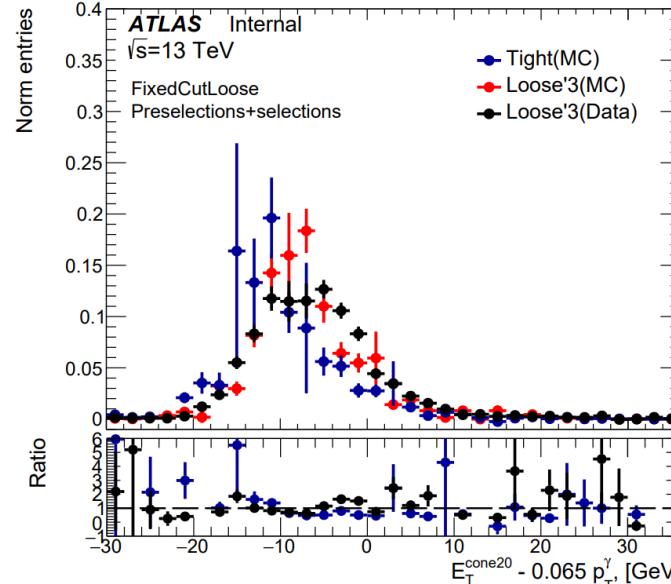
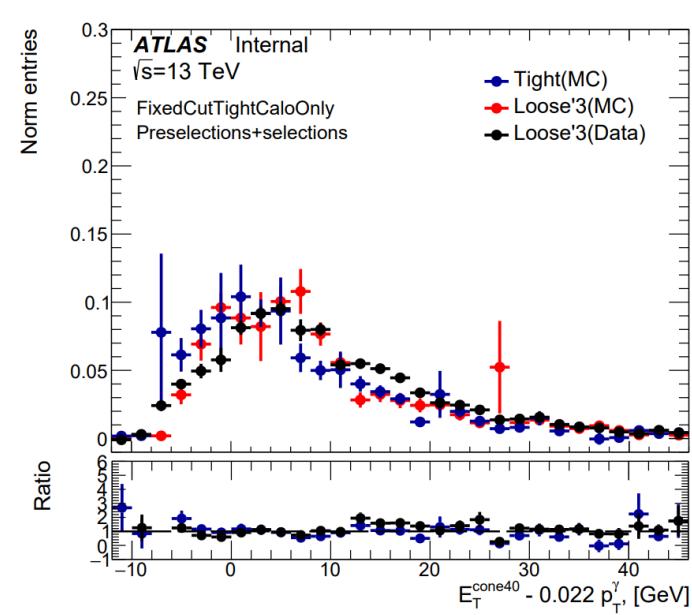
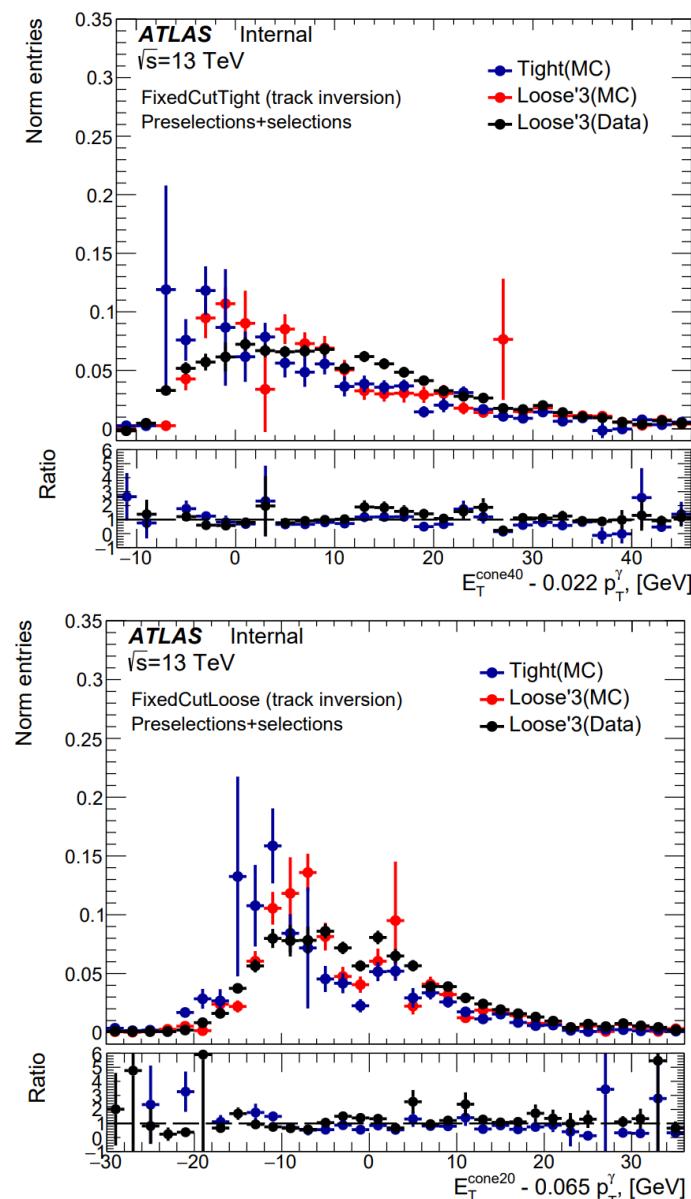
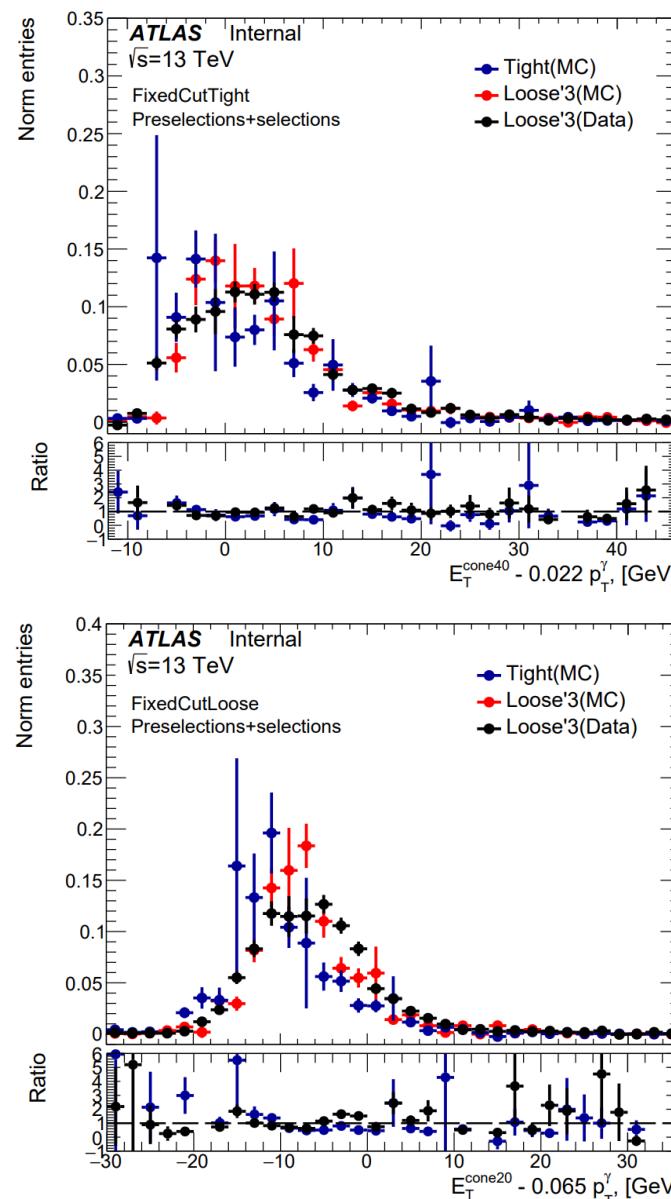
Working point	loose'2	loose'3	loose'4	loose'5
FCTight	$1.06 \pm 0.16$	$1.15 \pm 0.16$	$1.17 \pm 0.15$	$1.30 \pm 0.17$
FCTight (inversion)	$1.05 \pm 0.14$	$1.21 \pm 0.15$	$1.38 \pm 0.16$	$1.65 \pm 0.19$
FCTCaloOnly	$1.18 \pm 0.13$	$1.31 \pm 0.13$	$1.37 \pm 0.13$	$1.54 \pm 0.14$
FCLoose	$1.0 \pm 0.2$	$1.0 \pm 0.2$	$1.0 \pm 0.2$	$1.3 \pm 0.2$
FCLoose (inversion)	$1.11 \pm 0.13$	$1.23 \pm 0.12$	$1.34 \pm 0.12$	$1.60 \pm 0.13$



$$E_T^{\text{miss}} \text{ significance} = |E_T^{\text{miss}}|^2 / (\sigma_L^2 (1 - \rho_{LT}^2))$$

$\sigma_L$  is the total variance in the longitudinal direction to the  $E_T^{\text{miss}}$   
 $\rho_{LT}$  is the correlation factor of the longitudinal L and transverse T measurement

# Isolation distributions (loose'3)



# R factor in data

FixedCutLoose (inverted), w/o upper cut

	MC			
	loose'2	loose'3	loose'4	loose'5
R-factor	1.11 ± 0.13	1.23 ± 0.12	1.34 ± 0.12	1.60 ± 0.13
Data-driven				
Cut	loose'2	loose'3	loose'4	loose'5
4.5	0.97 ± 0.10	1.05 ± 0.10	1.05 ± 0.09	1.06 ± 0.08
4.6	1.00 ± 0.10	1.08 ± 0.10	1.06 ± 0.09	1.07 ± 0.08
4.75	1.03 ± 0.10	1.05 ± 0.10	1.07 ± 0.09	1.09 ± 0.08
9.5	1.04 ± 0.09	1.03 ± 0.08	0.98 ± 0.07	0.97 ± 0.07
10.0	1.04 ± 0.09	1.03 ± 0.08	0.98 ± 0.07	0.98 ± 0.07
10.5	1.02 ± 0.09	1.02 ± 0.08	0.95 ± 0.07	0.96 ± 0.07
11.0	1.06 ± 0.09	1.02 ± 0.08	0.97 ± 0.07	0.96 ± 0.07

FixedCutTightCaloOnly, w/o upper cut

	MC			
	loose'2	loose'3	loose'4	loose'5
R-factor	1.18 ± 0.13	1.31 ± 0.13	1.37 ± 0.13	1.54 ± 0.14
Data-driven				
Cut	loose'2	loose'3	loose'4	loose'5
9.45	1.15 ± 0.07	1.21 ± 0.06	1.20 ± 0.06	1.23 ± 0.06
9.95	1.14 ± 0.06	1.20 ± 0.06	1.19 ± 0.06	1.22 ± 0.06
10.45	1.15 ± 0.06	1.20 ± 0.06	1.19 ± 0.05	1.21 ± 0.05
10.45	1.21 ± 0.07	1.26 ± 0.06	1.24 ± 0.06	1.26 ± 0.06

FixedCutTight (inverted), w/o upper cut

	MC			
	loose'2	loose'3	loose'4	loose'5
R-factor	1.05 ± 0.14	1.21 ± 0.15	1.38 ± 0.16	1.65 ± 0.19
Data-driven				
Cut	loose'2	loose'3	loose'4	loose'5
9.45	1.10 ± 0.08	1.15 ± 0.07	1.11 ± 0.06	1.16 ± 0.06
9.95	1.09 ± 0.07	1.15 ± 0.07	1.12 ± 0.06	1.16 ± 0.06
10.20	1.08 ± 0.07	1.14 ± 0.07	1.11 ± 0.06	1.15 ± 0.06
10.45	1.10 ± 0.07	1.15 ± 0.07	1.13 ± 0.06	1.17 ± 0.06

FixedCutTight, upper cut = 25.45 GeV

	MC			
	loose'2	loose'3	loose'4	loose'5
R-factor	1.07 ± 0.16	1.17 ± 0.17	1.18 ± 0.16	1.31 ± 0.17
Data-driven				
Cut	loose'2	loose'3	loose'4	loose'5
8.45	1.15 ± 0.13	1.16 ± 0.12	1.16 ± 0.11	1.21 ± 0.11
8.95	1.11 ± 0.13	1.11 ± 0.12	1.14 ± 0.11	1.17 ± 0.11
9.45	1.19 ± 0.14	1.22 ± 0.13	1.27 ± 0.13	1.30 ± 0.12
9.95	1.16 ± 0.14	1.17 ± 0.13	1.23 ± 0.12	1.28 ± 0.12
10.45	1.19 ± 0.14	1.20 ± 0.14	1.22 ± 0.12	1.26 ± 0.12

FixedCutLoose was chosen. In order to decrease syst.  
uncert. the loose'3 was chosen

# jet → γ background estimation (loose'3)

Event yields for the data and non-jet → γ background processes considered in the ABCD method

	Data	Wγ QCD	Wγ EWK	e → γ	ttγ	γ + jet	Z(l l)γ
A	$26523 \pm 163$	$3936 \pm 23$	$136.3 \pm 0.7$	$3039 \pm 12$	$234 \pm 3$	$5262 \pm 53$	$285 \pm 5$
B	$1475 \pm 38$	$52 \pm 4$	$1.86 \pm 0.08$	$8.95 \pm 0.03$	$1.3 \pm 0.2$	$0.6 \pm 0.4$	$1.0 \pm 0.6$
C	$2568 \pm 51$	$60 \pm 2$	$2.16 \pm 0.09$	$61.4 \pm 0.2$	$4.2 \pm 0.4$	$76 \pm 6$	$4.8 \pm 0.5$
D	$1443 \pm 38$	$2.7 \pm 0.6$	$0.17 \pm 0.02$	$0.0715 \pm 0.0002$	$0.35 \pm 0.13$	$0 \pm 0$	$0 \pm 0$

$$N_A^{\text{sig}} = \tilde{N}_A - R(\tilde{N}_B - c_B N_A^{\text{sig}}) \frac{\tilde{N}_C - c_C N_A^{\text{sig}}}{\tilde{N}_D - c_D N_A^{\text{sig}}}$$

$$N_A^{\text{sig}} = \frac{b - \sqrt{b^2 - 4ac}}{2a}$$

$$\begin{cases} a = c_D - R c_B c_C; \\ b = \tilde{N}_D + c_D \tilde{N}_A - R(c_B \tilde{N}_C + c_C \tilde{N}_B); \\ c = \tilde{N}_D \tilde{N}_A - R \tilde{N}_C \tilde{N}_B. \end{cases}$$

The signal leakage parameters:

(Isolation gap = 2GeV)

	$c_B$	$c_C$	$c_D$
A	$0.00939 \pm 0.00007$		
B		$0.01536 \pm 0.00010$	
C			$0.00051 \pm 0.00002$
D			

Event yields signal:

	$Z(\nu\bar{\nu})\gamma$ QCD	$Z(\nu\bar{\nu})\gamma$ EWK
A	$10513 \pm 8$	$152.1 \pm 0.3$
B	$98.0 \pm 0.8$	$2.14 \pm 0.04$
C	$161.5 \pm 1.0$	$2.31 \pm 0.04$
D	$5.3 \pm 0.2$	$0.135 \pm 0.009$

With R by data-driven



$$N_A^{\text{jet} \rightarrow \gamma} = 2078^{+100}_{-97}$$

# Systematic uncertainty I

Systematic uncertainties come from:

- non-tight definition and isolation gap choice.
- Variation for  $\pm 1\sigma$  changes in data yield
- different generators
- imperfect photon iso/ID modeling

## Different loose prime and isolation gap

Central value (with $R_{\text{data}}$ )	2078
loose'2	+327
loose'4	-111
loose'5	-173
Iso gap +0.25 GeV	+48
Iso gap -0.35 GeV	+29

$$R_{\text{data}}^{\text{iso gap } +0.25 \text{ GeV}} = 1.07 \pm 0.11$$

$$R_{\text{data}}^{\text{iso gap } -0.35 \text{ GeV}} = 1.06 \pm 0.09$$

Iso gap, GeV	$N_B$	$N_D$
-0.40	$1524 \pm 39$	$1488 \pm 39$
-0.35	$1518 \pm 39$	$1482 \pm 38$
-0.30	$1513 \pm 39$	$1477 \pm 38$
-0.25	$1503 \pm 39$	$1474 \pm 38$
-0.20	$1497 \pm 39$	$1468 \pm 38$
2.0	$1475 \pm 38$	$1443 \pm 38$
+0.15	$1448 \pm 38$	$1416 \pm 38$
+0.20	$1443 \pm 38$	$1404 \pm 37$
+0.25	$1437 \pm 38$	$1398 \pm 37$



$$\delta = 16\%$$

► The choice of loose prime 3 reduced the systematic uncertainty from 32% to 16%

# Systematic uncertainty II

## Different generators:

Signal leakage parameters	Different generators		Relative deviation
	MadGraph+Pythia8, Sherpa 2.2	MadGraph+Pythia8, MadGraph+Pythia8	
$c_B$	$0.00939 \pm 0.00007$	$0.0155 \pm 0.0004$	39%
$c_C$	$0.01536 \pm 0.00010$	$0.0156 \pm 0.0004$	1.5%
$c_D$	$0.00051 \pm 0.000028$	$0.00077 \pm 0.00009$	34%
$jet \rightarrow \gamma$ est. (with $R_{\text{data}}$ )	2078	2061	0.8%

- Uncertainty coming from signal leakage is obtained  $\delta = 0.8\%$

$$R_{\text{data}}^{\text{diff.gen.}} = 1.10 \pm 0.10$$

Systematic uncertainty come from imperfect photon iso/ID modeling:

- $\sigma_{\text{iso}}^{c_B} = \delta_{\text{iso}}^{\text{eff}} \cdot (c_B + 1)/c_B$
- $\sigma_{\text{ID}}^{c_C} = \delta_{\text{ID}}^{\text{eff}} \cdot (c_C + 1)/c_C$
- $\sigma_{\text{iso}}^{c_D} = \delta_{\text{iso}}^{\text{eff}} \cdot (c_D + 1)/c_D$
- $\sigma_{\text{ID}}^{c_D} = \delta_{\text{ID}}^{\text{eff}} \cdot (c_D + 1)/c_D$

$$\delta_{\text{iso}}^{\text{eff}} = 0.013$$
$$\delta_{\text{ID}}^{\text{eff}} = 0.013$$



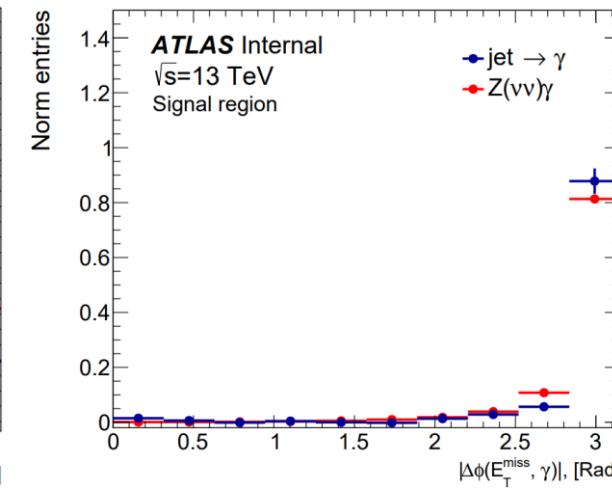
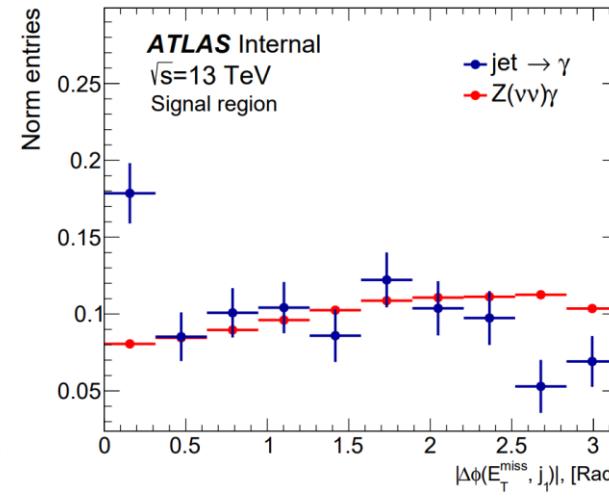
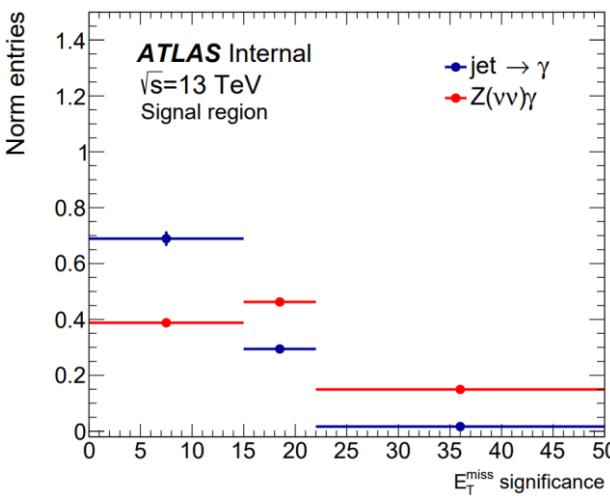
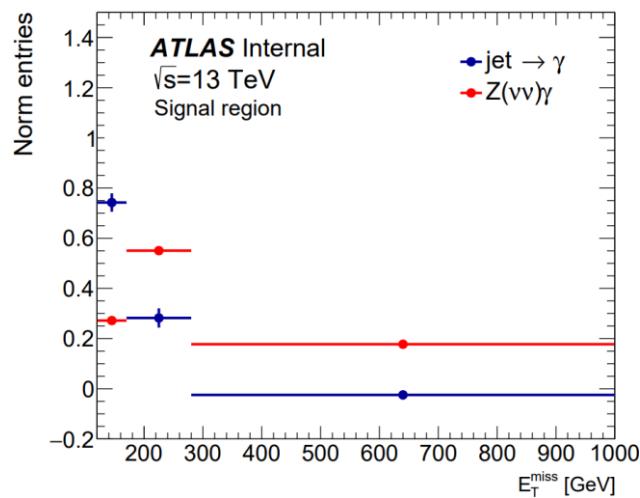
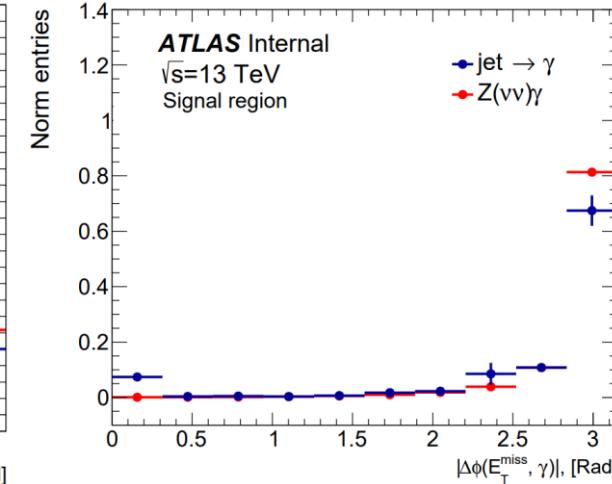
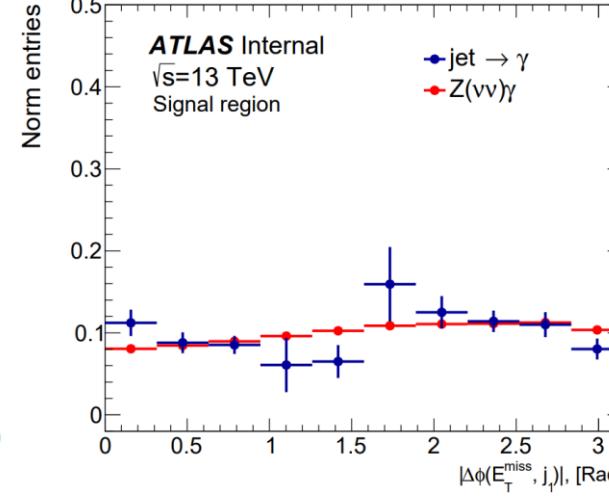
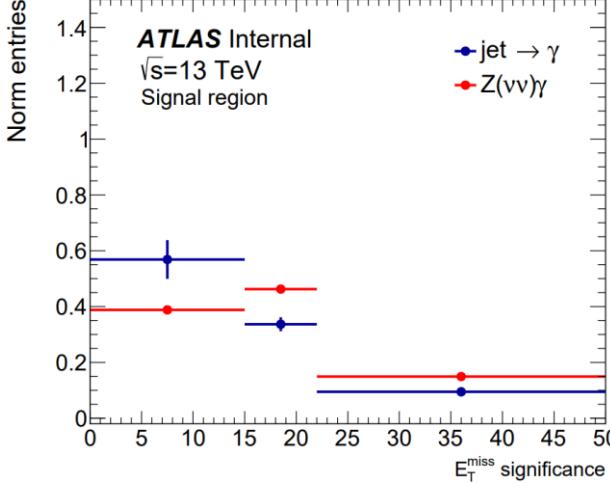
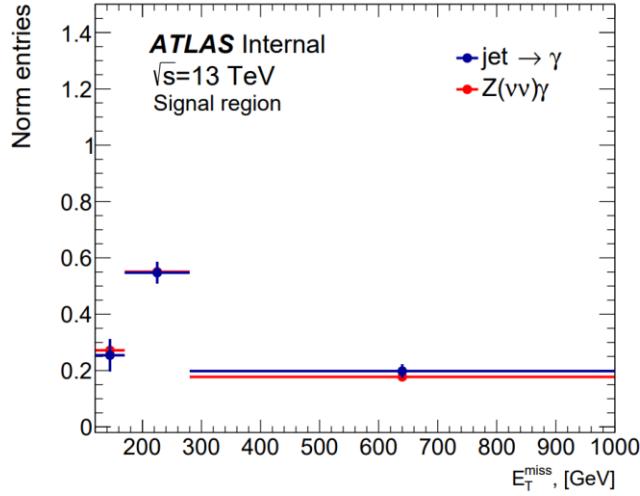
$$\delta_{\text{eff}}^{\text{iso/ID}} = 1.3\%$$

Estimate

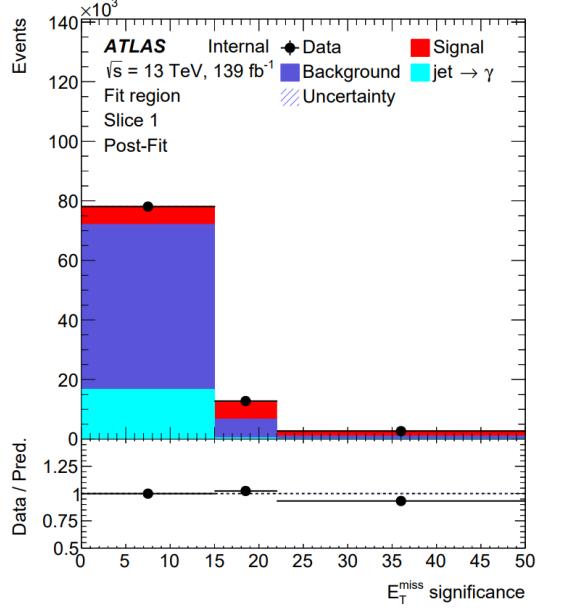
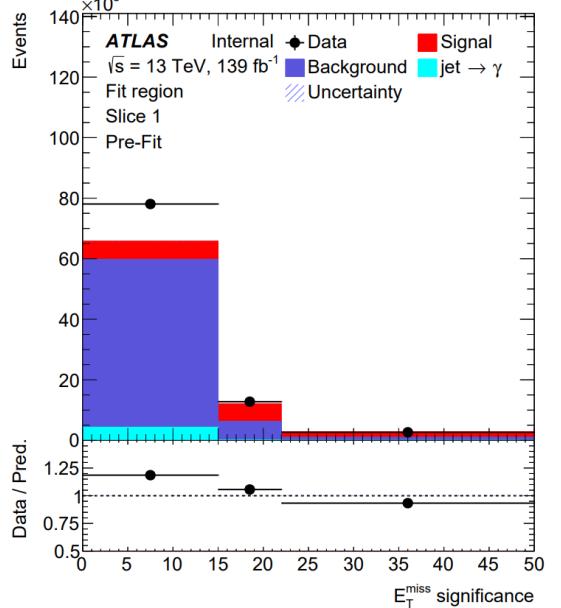
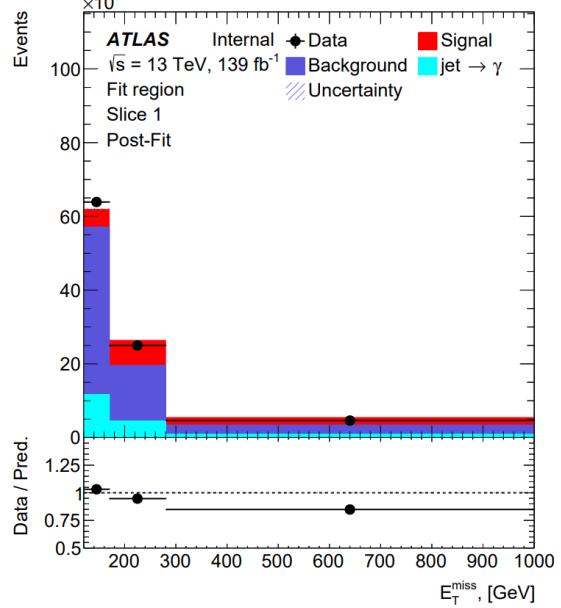
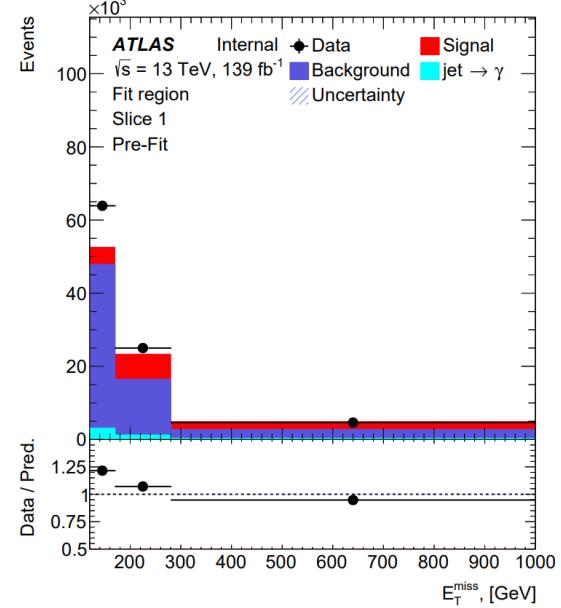
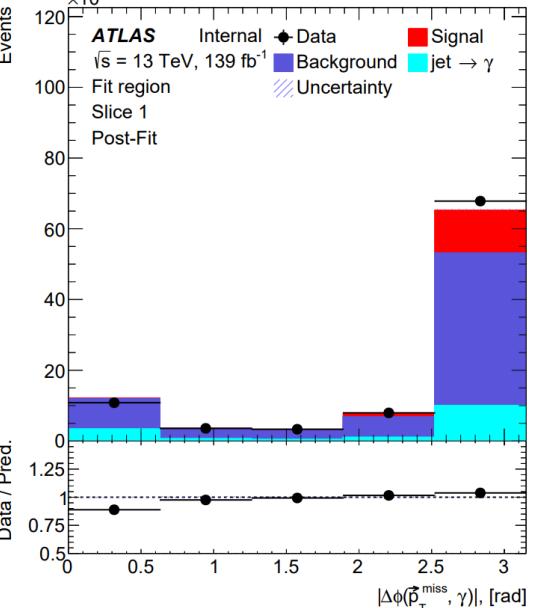
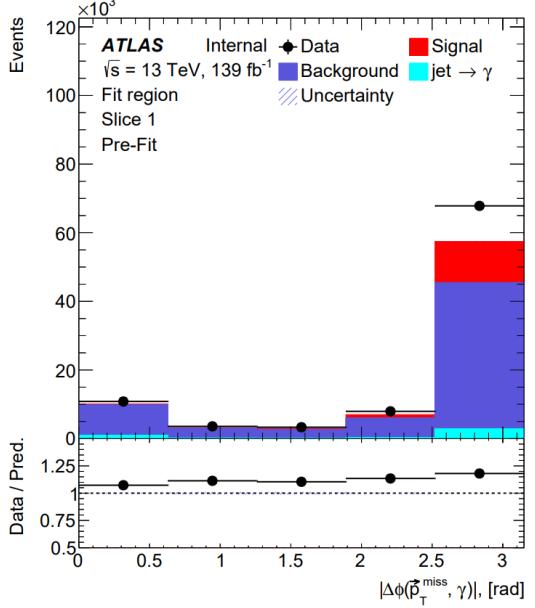
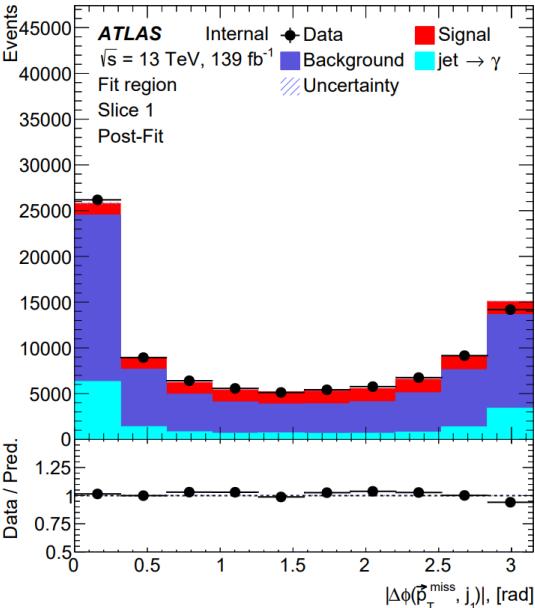
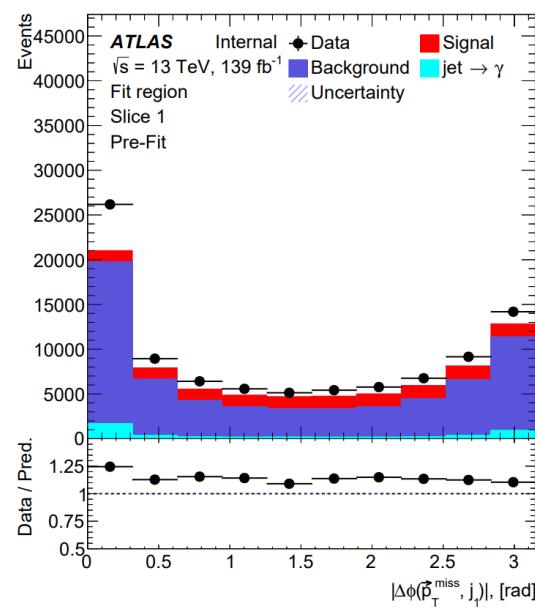
with  $R_{\text{Data}}: 2100^{+100}_{-100}(\text{stat.}) \pm 300(\text{syst.})$

- Total systematics:  $\delta_{\text{Data}} = 16\%$

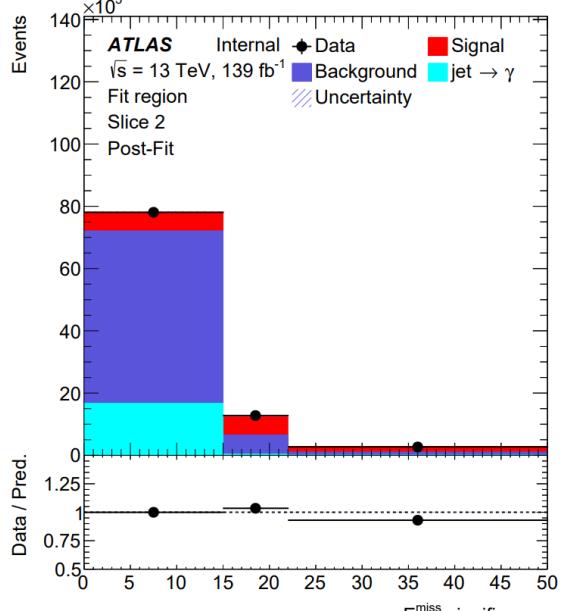
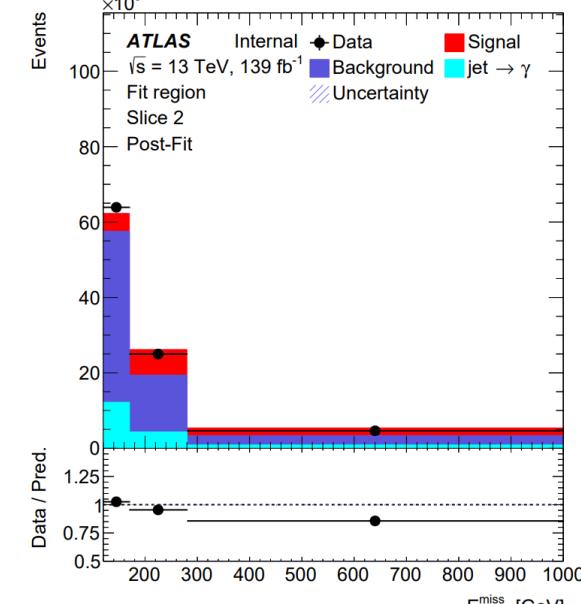
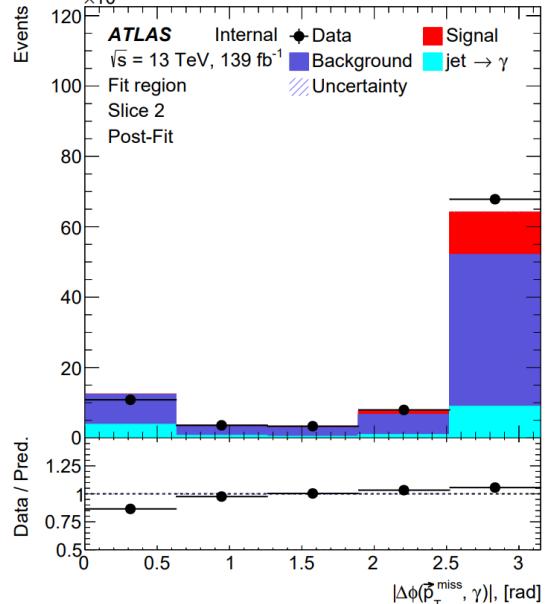
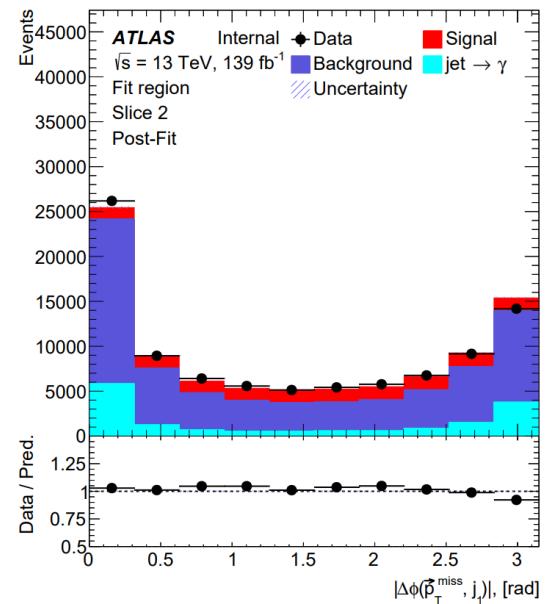
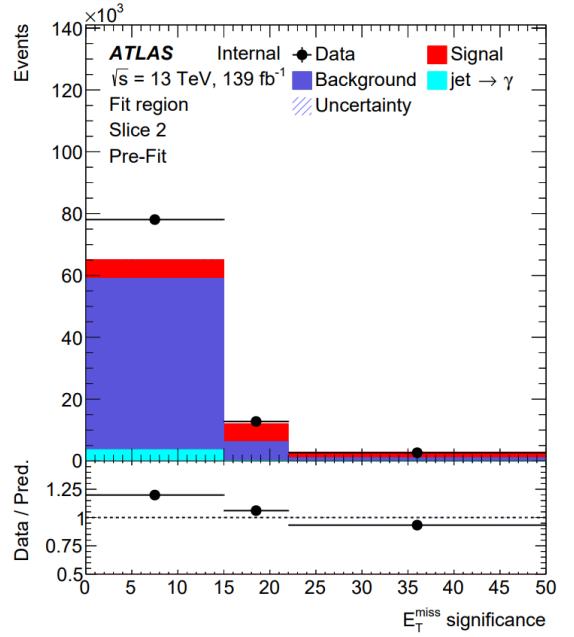
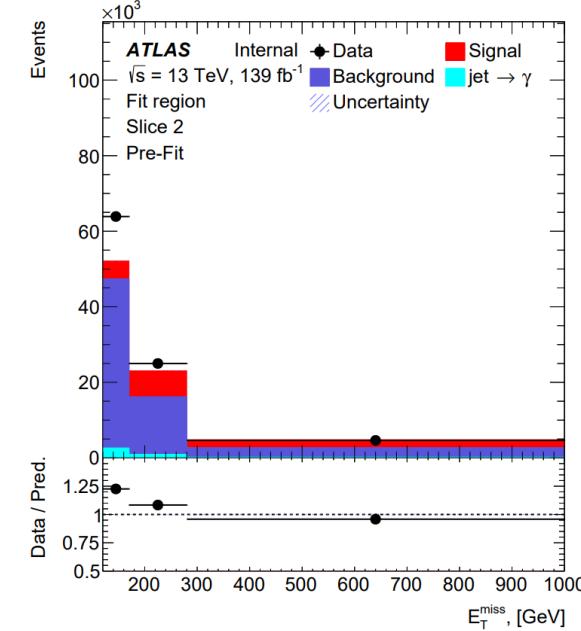
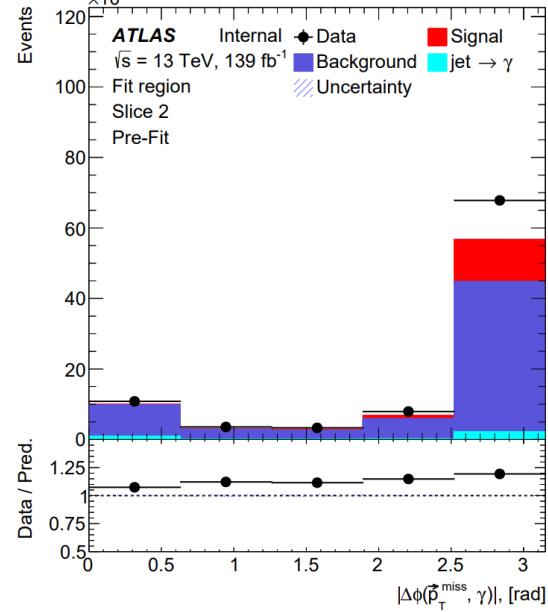
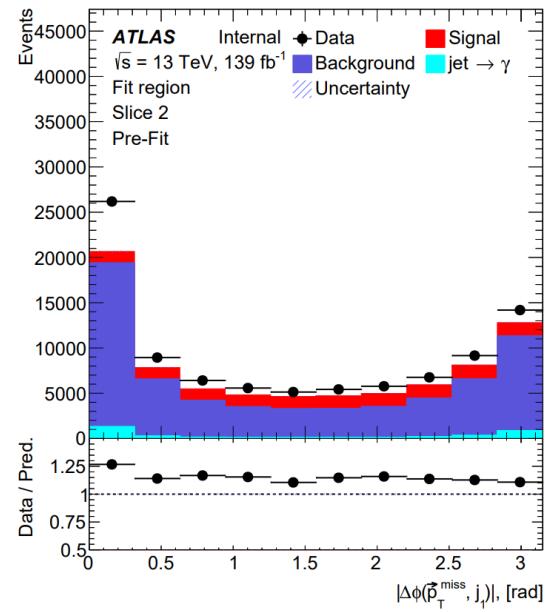
# *jet* $\rightarrow \gamma$ and Z $\gamma$ comparison in the SR



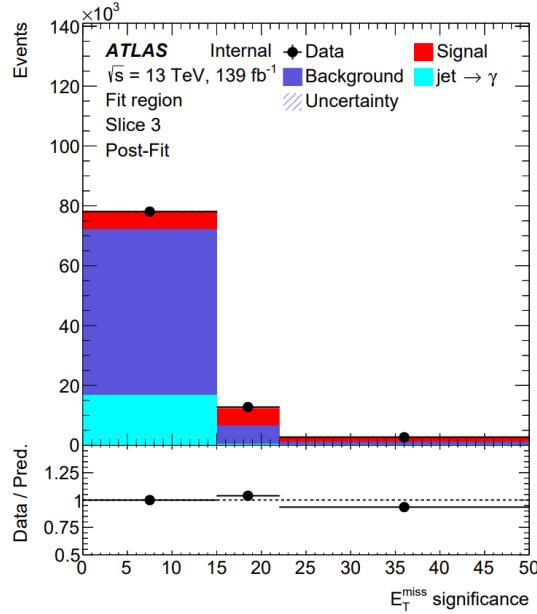
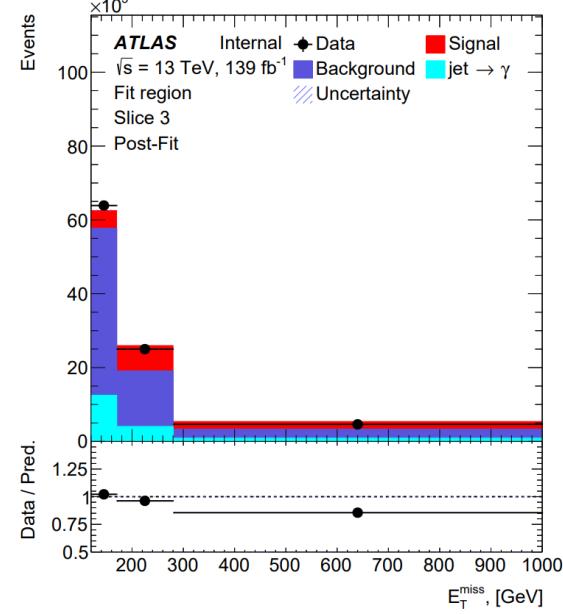
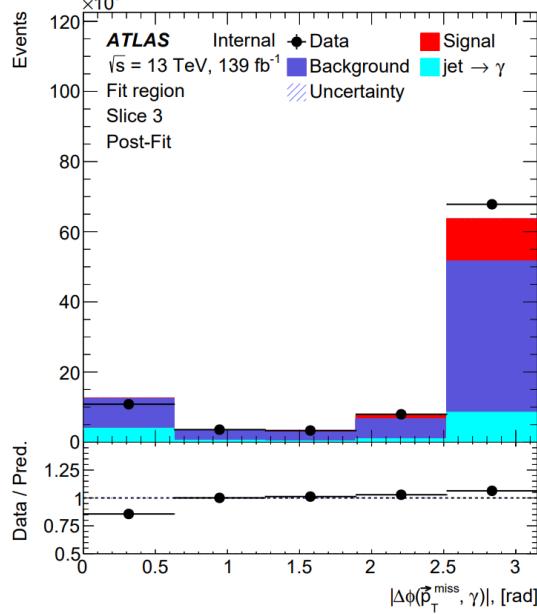
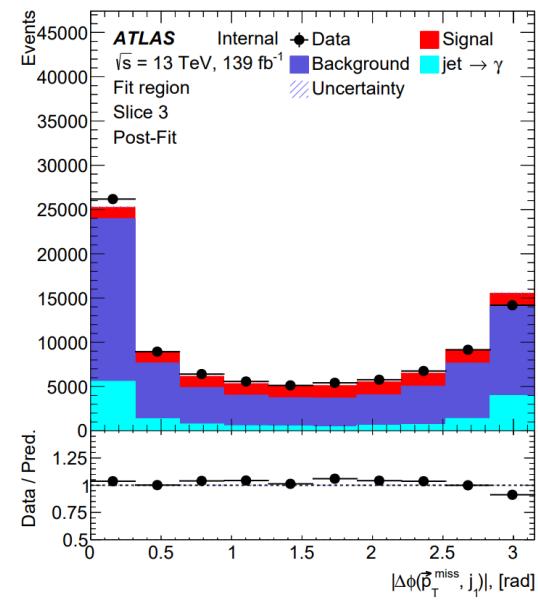
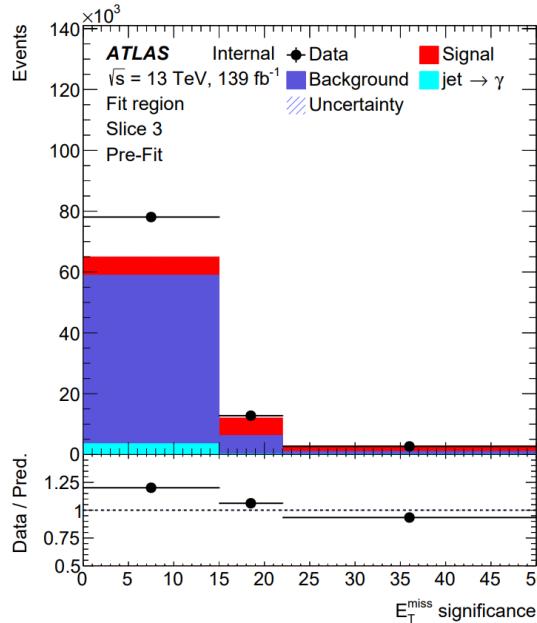
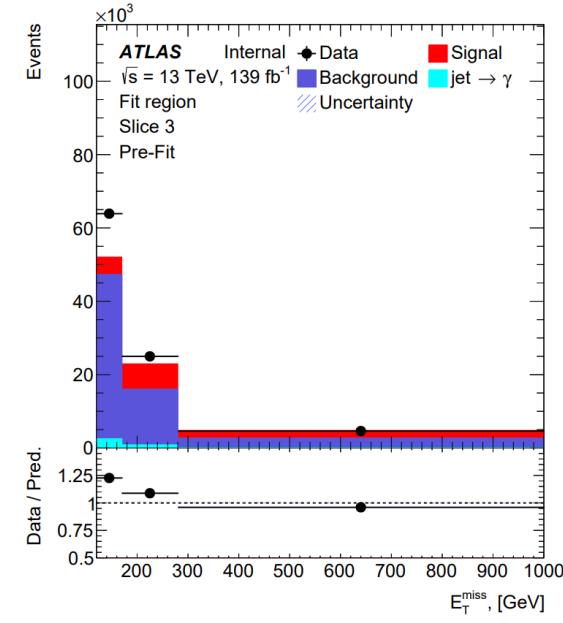
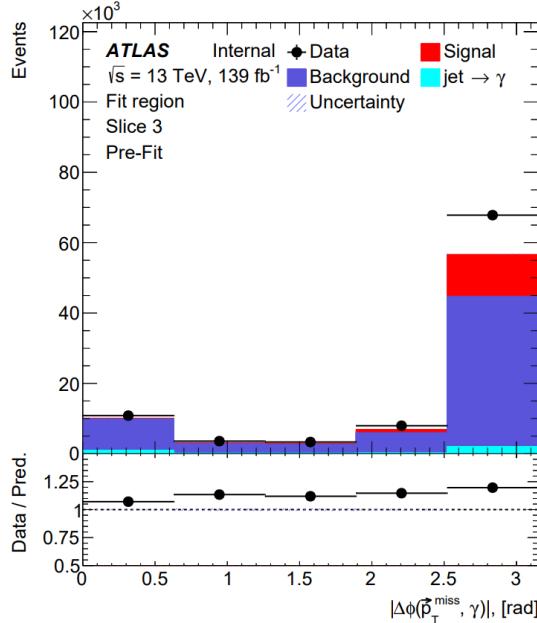
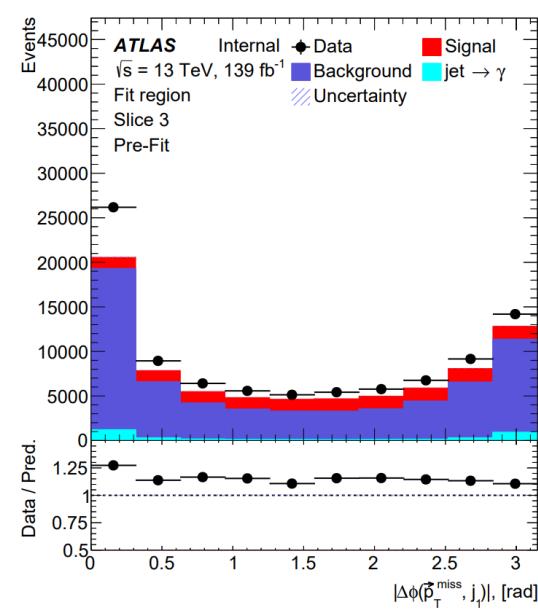
# Fit process. Slice 1



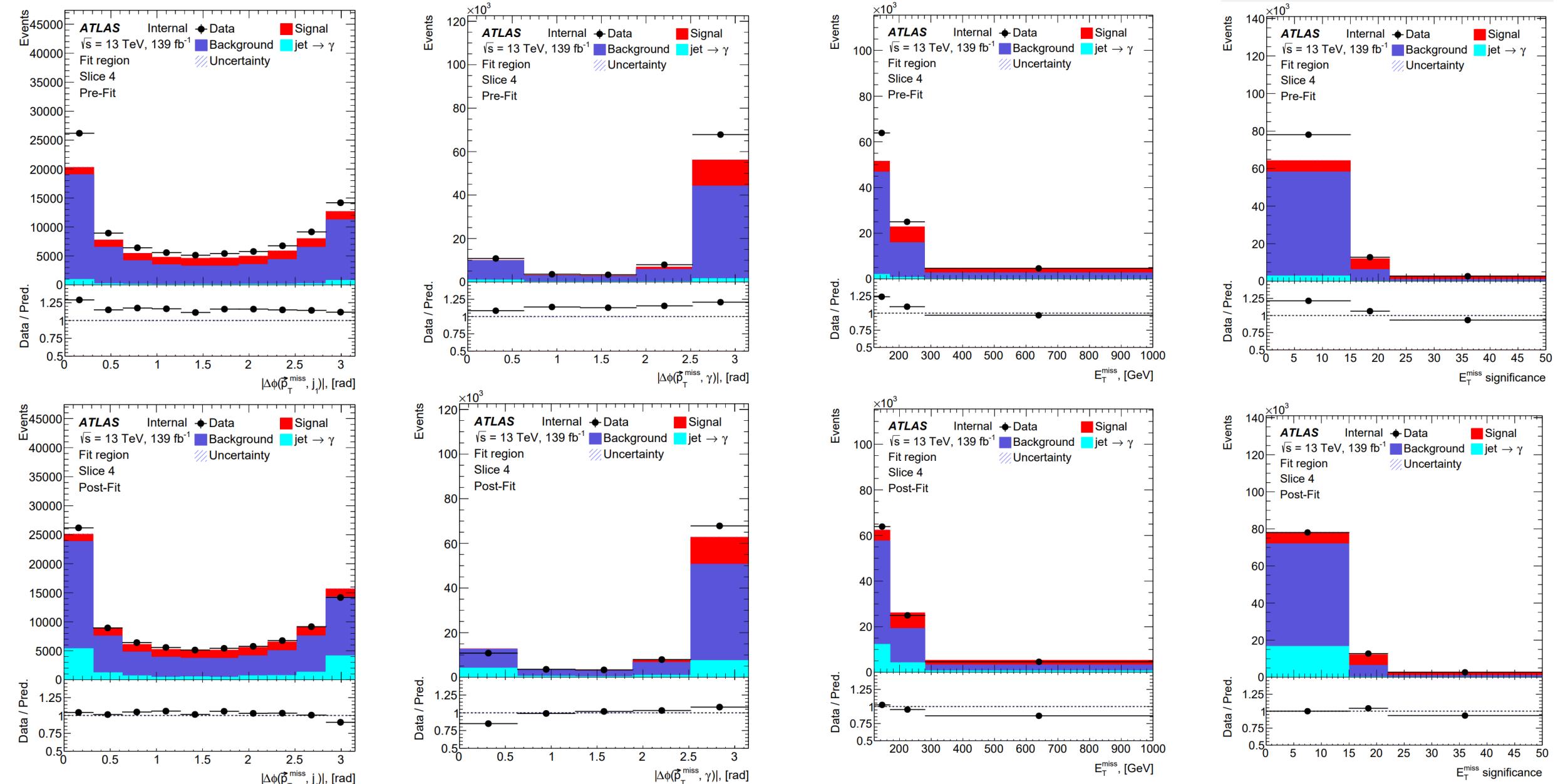
# Fit process. Slice 2



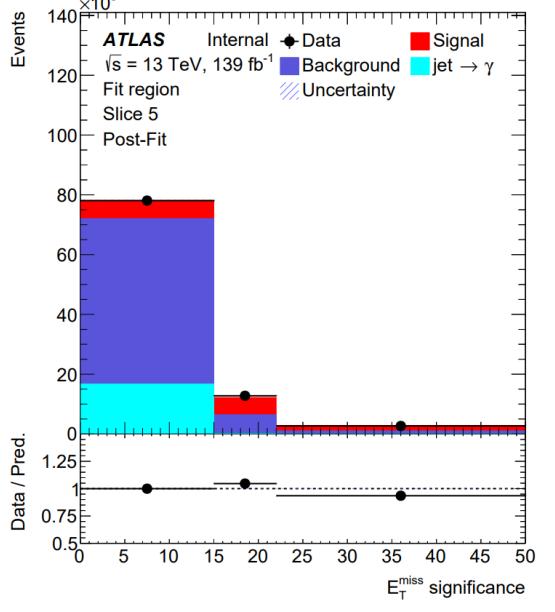
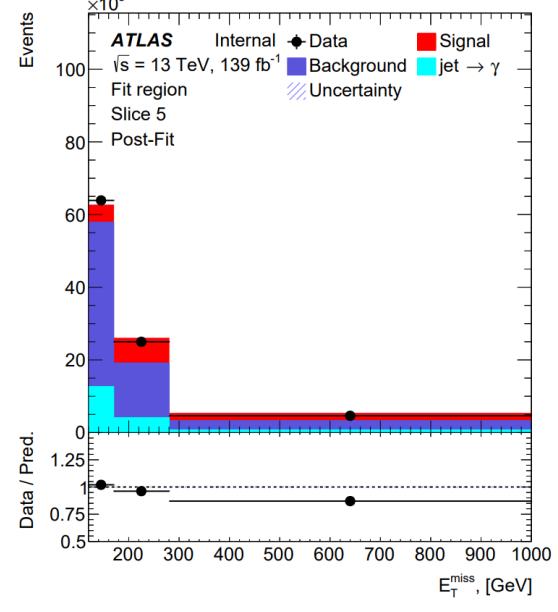
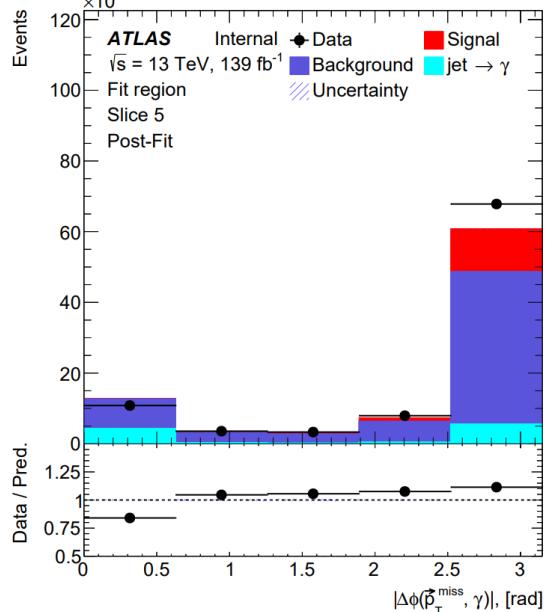
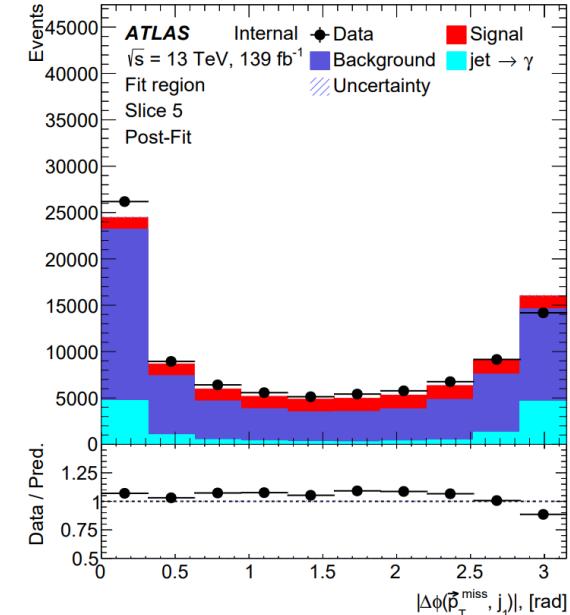
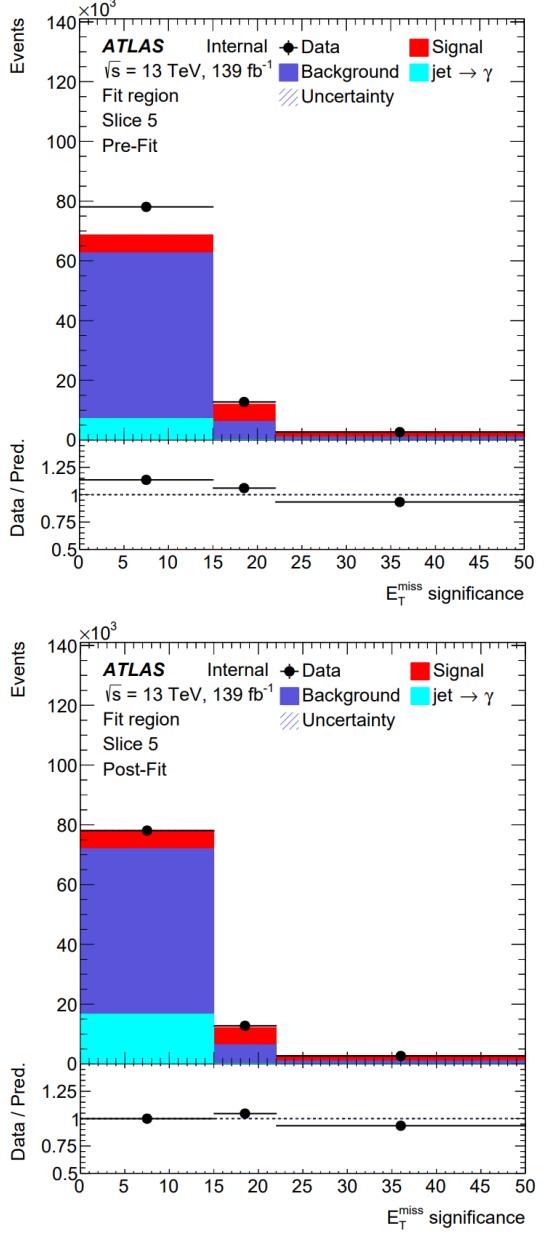
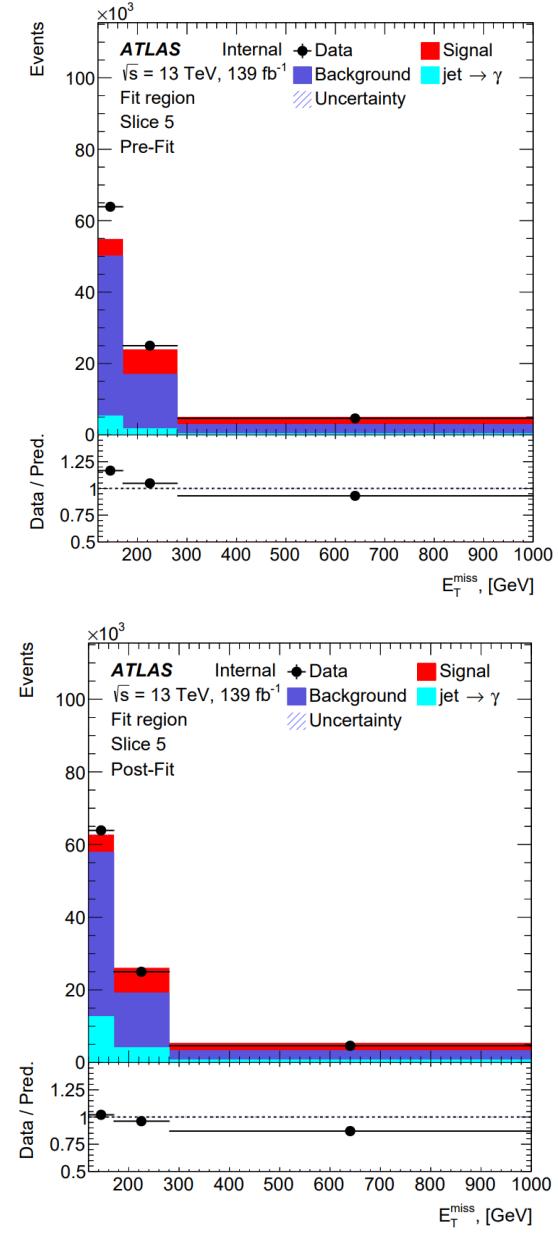
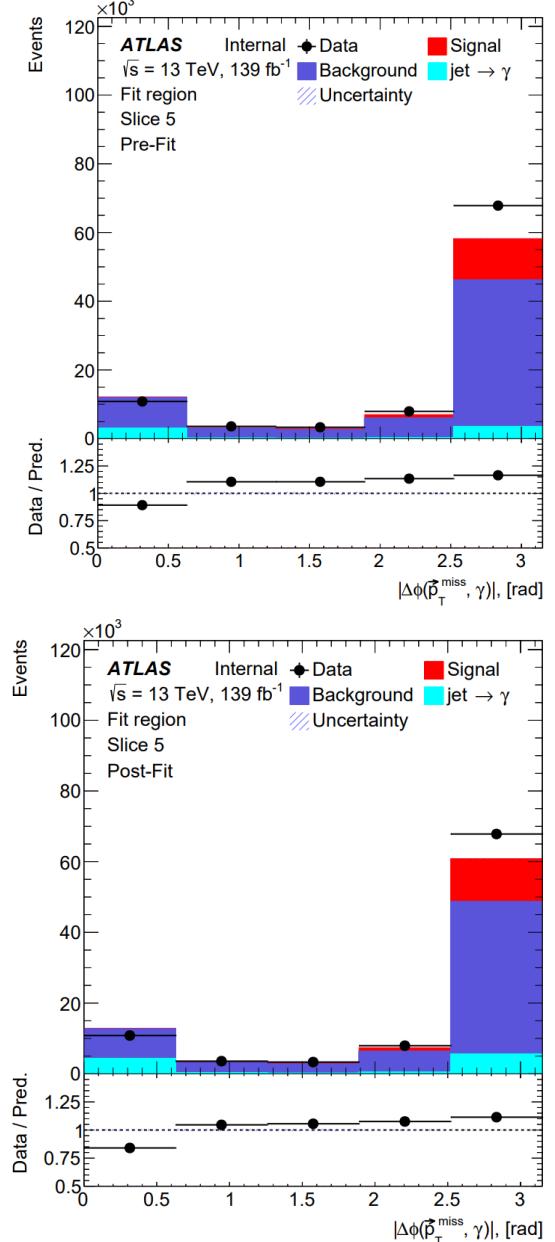
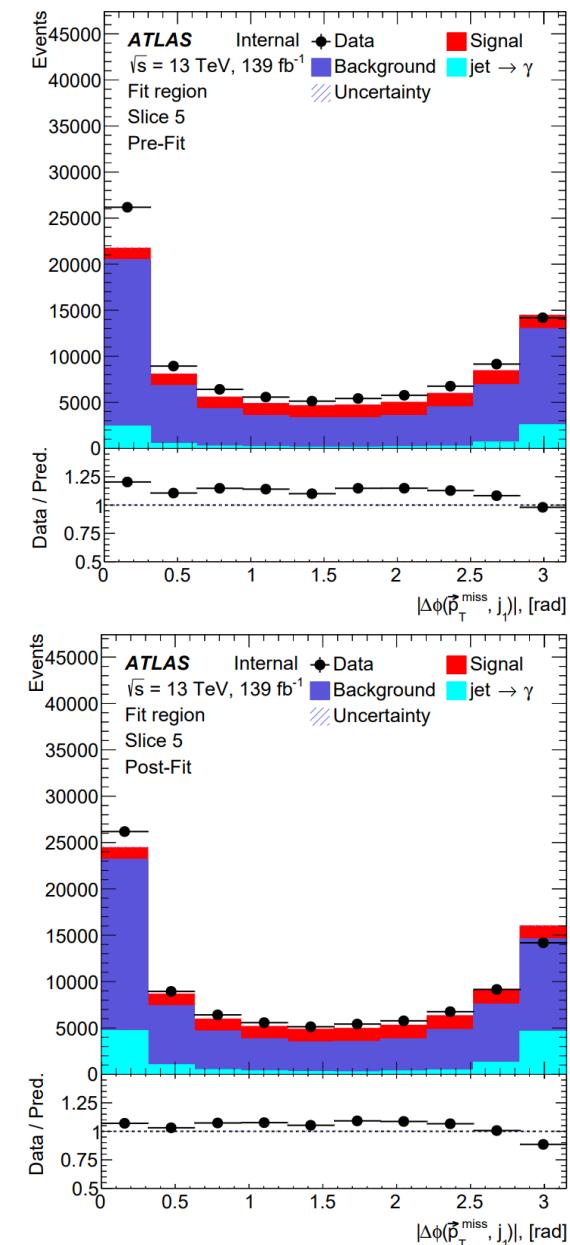
# Fit process. Slice 3



# Fit process. Slice 4



# Fit process. Slice 5



# The results of the fit

- Events in FR:

Data	Background (excl. $jet \rightarrow \gamma$ )	Signal
$93513 \pm 306$	$62568 \pm 146$	$13742 \pm 9$

- Events in CR1  
for each slice:

Slice	Data	Background (excl. $jet \rightarrow \gamma$ )	Signal (Sherpa)	Signal (MadGraph)
1	$4572 \pm 68$	$72 \pm 5$	$20.7 \pm 0.4$	$27 \pm 2$
2	$3776 \pm 61$	$47 \pm 4$	$18.4 \pm 0.3$	$20 \pm 2$
3	$3642 \pm 60$	$74 \pm 4$	$20.1 \pm 0.3$	$26 \pm 2$
4	$2916 \pm 54$	$41 \pm 3$	$21.0 \pm 0.3$	$27 \pm 2$
5	$7672 \pm 88$	$234 \pm 6$	$128.1 \pm 0.8$	$153 \pm 5$

- Events in CR2  
for each slice:

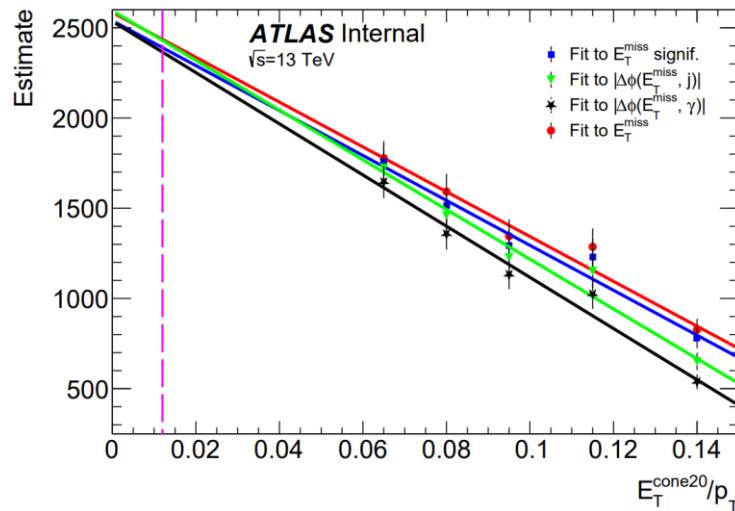
Slice	Data	Background (excl. $jet \rightarrow \gamma$ )	Signal (Sherpa)	Signal (MadGraph)
1	$463 \pm 22$	$8.4 \pm 0.9$	$10.1 \pm 0.3$	$16.7 \pm 1.3$
2	$337 \pm 18$	$8 \pm 3$	$9.3 \pm 0.3$	$12.7 \pm 1.2$
3	$286 \pm 17$	$11.6 \pm 0.9$	$9.7 \pm 0.2$	$15.5 \pm 1.3$
4	$223 \pm 15$	$5.5 \pm 0.9$	$10.9 \pm 0.3$	$18.6 \pm 1.3$
5	$471 \pm 22$	$41 \pm 2$	$67.0 \pm 0.6$	$105 \pm 3$

# The results of the fit

Result of the fit for Z $\gamma$  QCD MadGraph:

Slice	$T_1, E_T^{\text{miss}}$	$T_2, E_T^{\text{miss}}$ sign.	$T_3,  \Delta(E_T^{\text{miss}}, j_1) $	$T_4,  \Delta(E_T^{\text{miss}}, \gamma) $
1	$4.06 \pm 0.08$	$4.01 \pm 0.08$	$3.94 \pm 0.08$	$3.76 \pm 0.07$
2	$4.94 \pm 0.10$	$4.79 \pm 0.09$	$4.61 \pm 0.09$	$4.29 \pm 0.09$
3	$5.20 \pm 0.10$	$4.99 \pm 0.10$	$4.74 \pm 0.10$	$4.73 \pm 0.09$
4	$6.47 \pm 0.13$	$6.19 \pm 0.12$	$5.79 \pm 0.12$	$5.15 \pm 0.11$
5	$2.54 \pm 0.05$	$2.40 \pm 0.05$	$2.00 \pm 0.04$	$1.66 \pm 0.04$

The fit parameter  $T_{(i)}$



Slice	Observed $N_{CR2(i)}^{jet \rightarrow \gamma}$
1	$438 \pm 22$
2	$316 \pm 19$
3	$259 \pm 17$
4	$199 \pm 15$
5	$325 \pm 22$

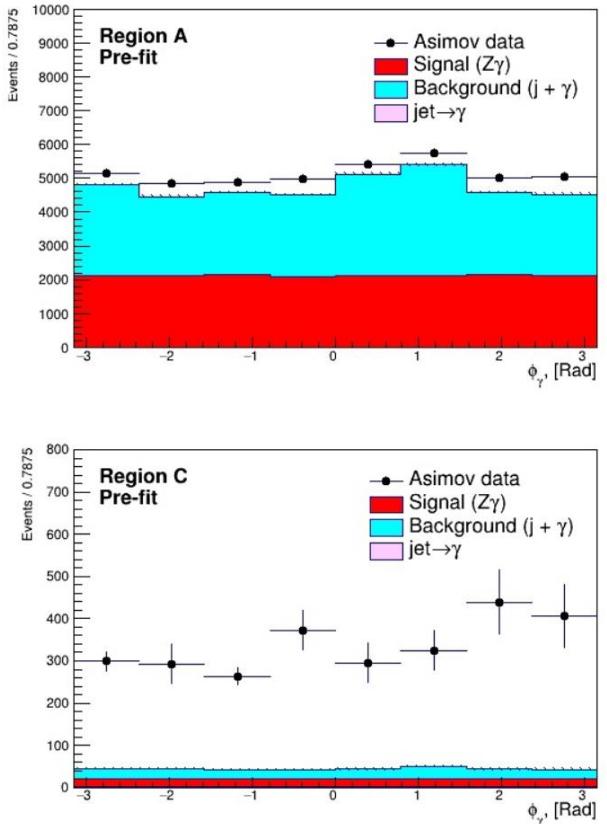
Observed  $jet \rightarrow \gamma$  events in the CR2

Slice	$N_{SR(i)}^{jet \rightarrow \gamma}, E_T^{\text{miss}}$	$N_{SR(i)}^{jet \rightarrow \gamma}, E_T^{\text{miss}}$ sign.	$N_{SR(i)}^{jet \rightarrow \gamma},  \Delta(E_T^{\text{miss}}, j_1) $	$N_{SR(i)}^{jet \rightarrow \gamma},  \Delta(E_T^{\text{miss}}, \gamma) $
1	$1777 \pm 94$	$1756 \pm 93$	$1723 \pm 92$	$1645 \pm 87$
2	$1562 \pm 97$	$1515 \pm 94$	$1459 \pm 91$	$1357 \pm 84$
3	$1345 \pm 92$	$1293 \pm 88$	$1228 \pm 84$	$1132 \pm 78$
4	$1286 \pm 100$	$1231 \pm 96$	$1152 \pm 90$	$1024 \pm 80$
5	$827 \pm 58$	$781 \pm 55$	$651 \pm 46$	$538 \pm 39$

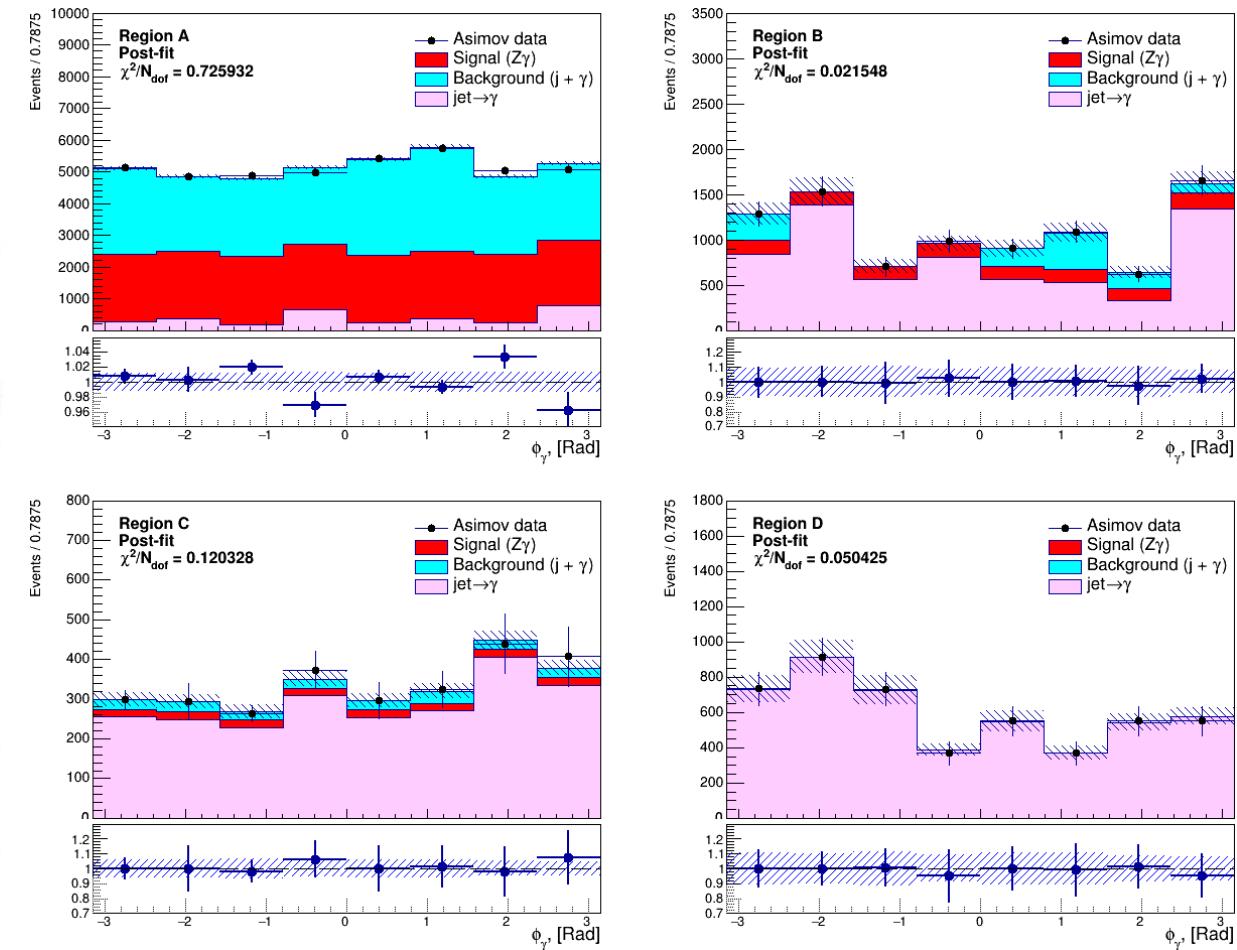
$jet \rightarrow \gamma$  events in the SR for each slice

# The results of the fit

Pre-fit for  $\phi_\gamma$

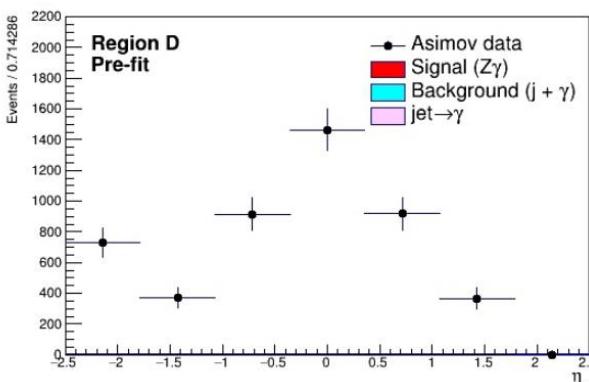
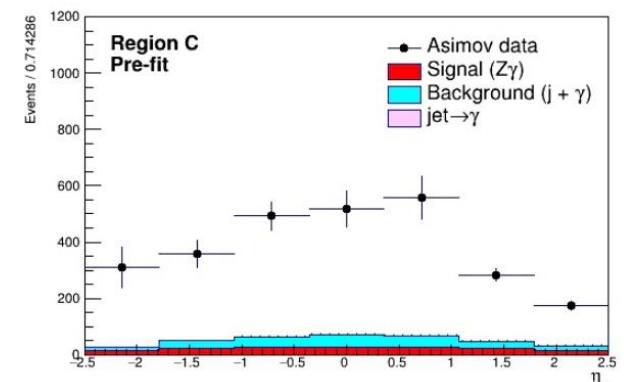
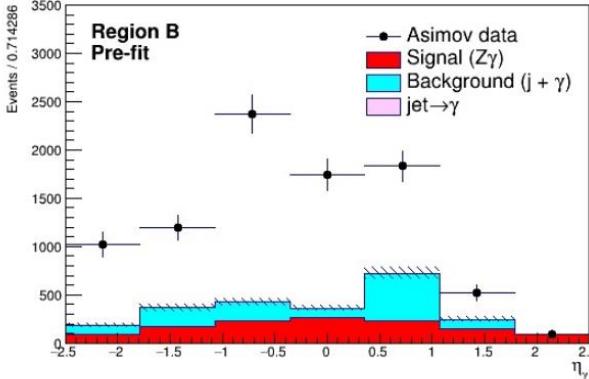
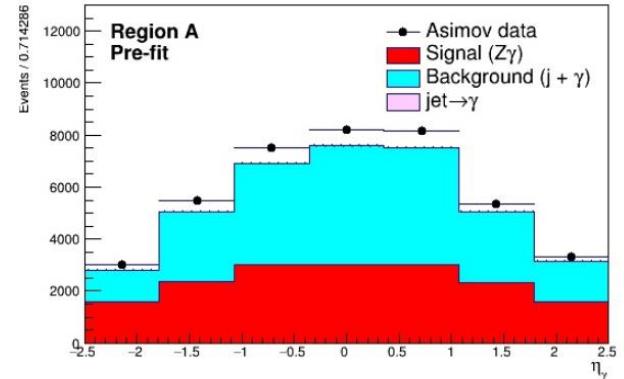


Post-fit for  $\phi_\gamma$



# The results of the fit

Pre-fit for  $\eta_\gamma$



Post-fit for  $\eta_\gamma$

