



# Hydrodynamic flow in heavy-ion collisions at RHIC and LHC

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and Astrophysics

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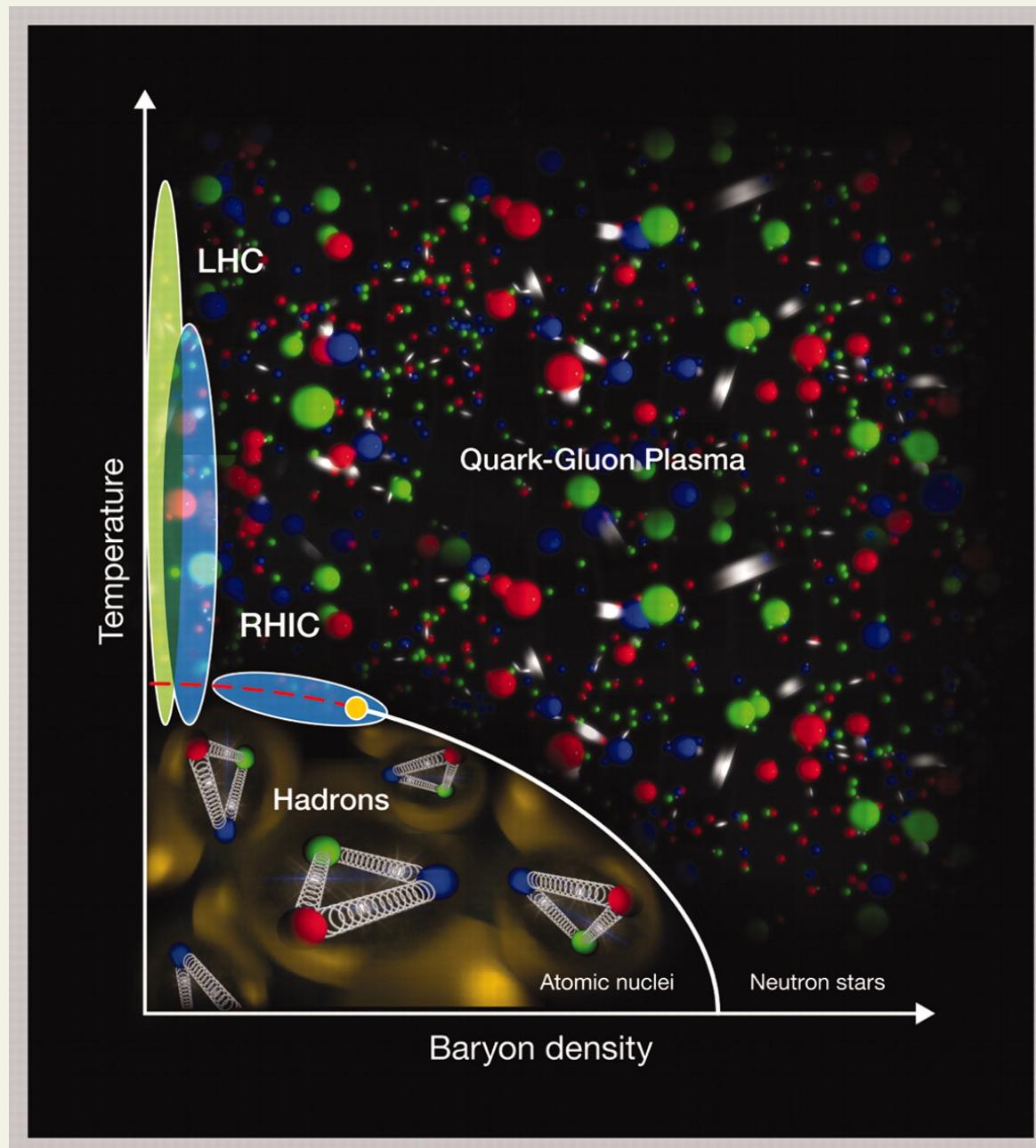
The speaker has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 665778 via the National Science Center, Poland, under grant Polonez DEC-2015/19/P/ST2/03333

# Strongly interacting matter

- interaction between constituents QCD, not QED
- matter in condensed matter physics sense
- so many particles that thermodynamical concepts
  - temperature
  - pressure
  - etc.

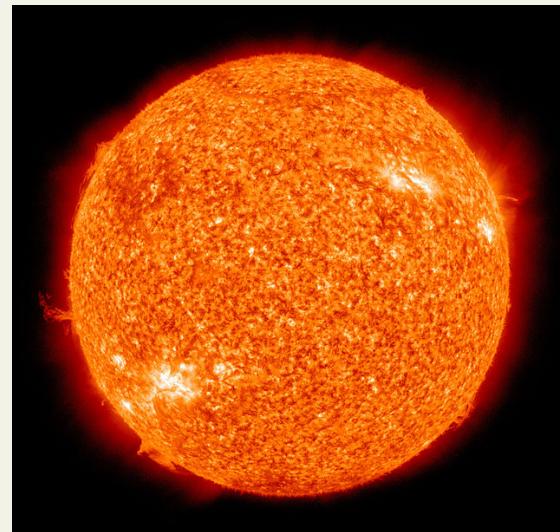
apply

# Phase diagram of strongly interacting matter



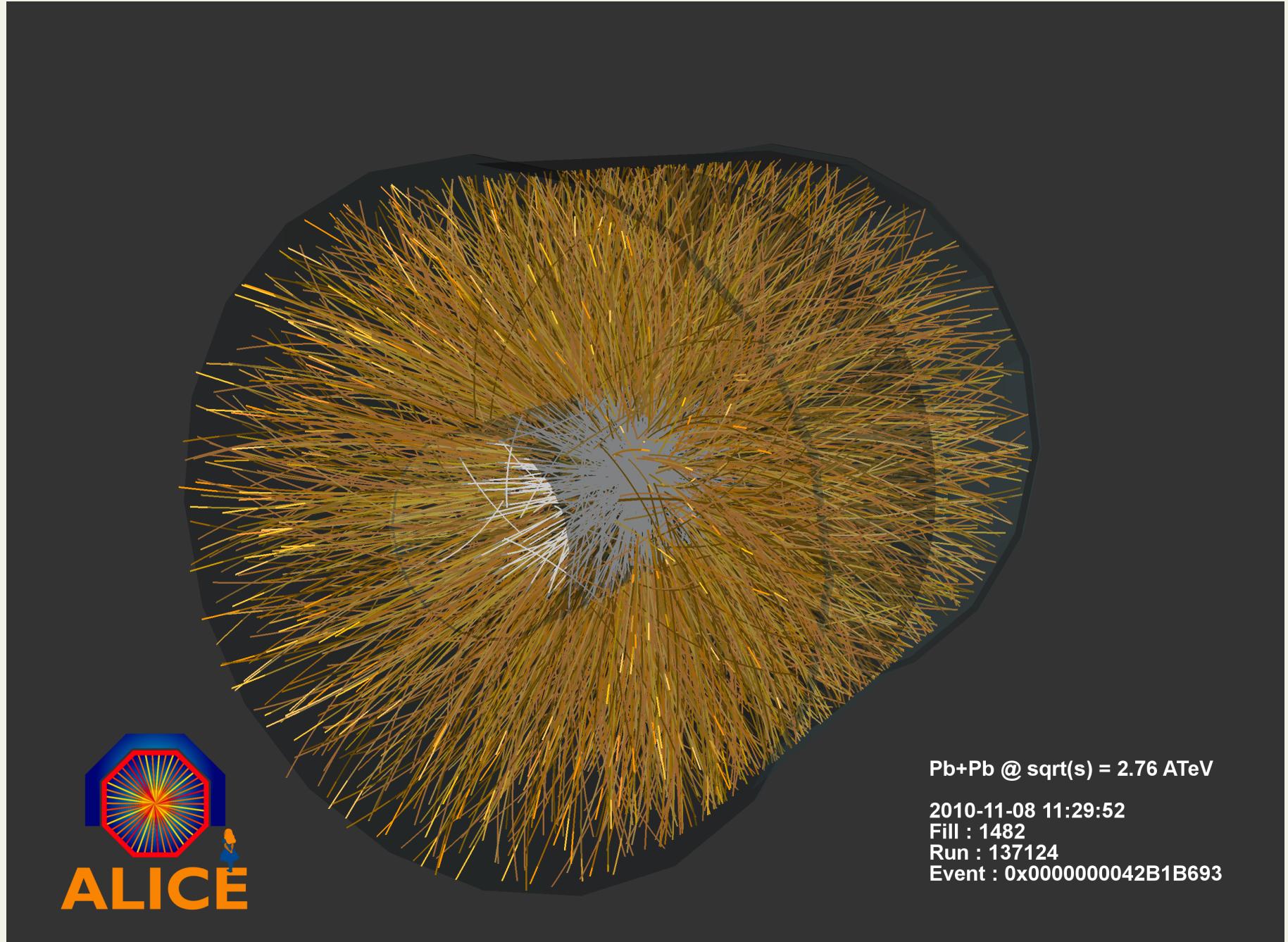
**Transition temperature from hadrons to QGP**  $\sim 2 \cdot 10^{12}$  K,  $\sim 160$  MeV

- **temperature on the surface of the Sun**  $\sim 5800$  K
- **temperature in the core of the Sun**  $\sim 1.6 \cdot 10^7$  K



# Heavy-ion collision

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# Hydrodynamics

**local conservation of energy, momentum and baryon number:**

$$\partial_\mu T^{\mu\nu}(x) = 0 \quad \text{and} \quad \partial_\mu N^\mu(x) = 0$$

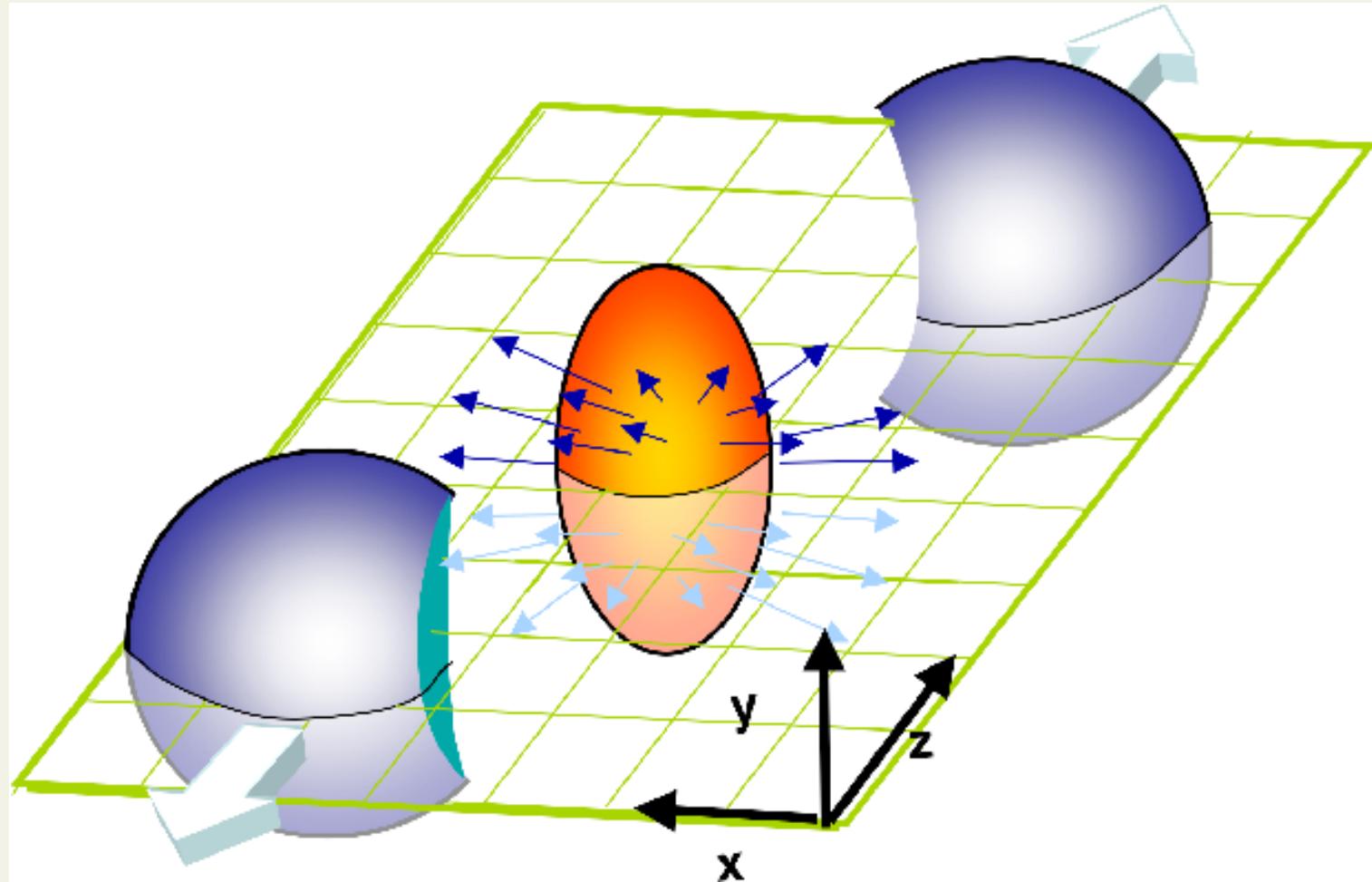
$$\begin{aligned} T^{\mu\nu} &= (\epsilon + P)u^\mu u^\nu - (P + \Pi)g^{\mu\nu} + \pi^{\mu\nu} \\ N^\mu &= nu^\mu + \nu^\mu \end{aligned}$$

**local, macroscopic variables:** **energy density**  $\epsilon(x)$   
**pressure**  $P(x)$   
**flow velocity**  $u^\mu(x)$

**matter characterized by:** **equation of state**  $P = P(T, \{\mu_i\})$   
**transport coefficients**  $\eta = \eta(T, \{\mu_i\})$   
 $\zeta = \zeta(T, \{\mu_i\})$   
 $\kappa = \kappa(T, \{\mu_i\})$

**Unknowns:** initial state, final state

# Elliptic flow $v_2$

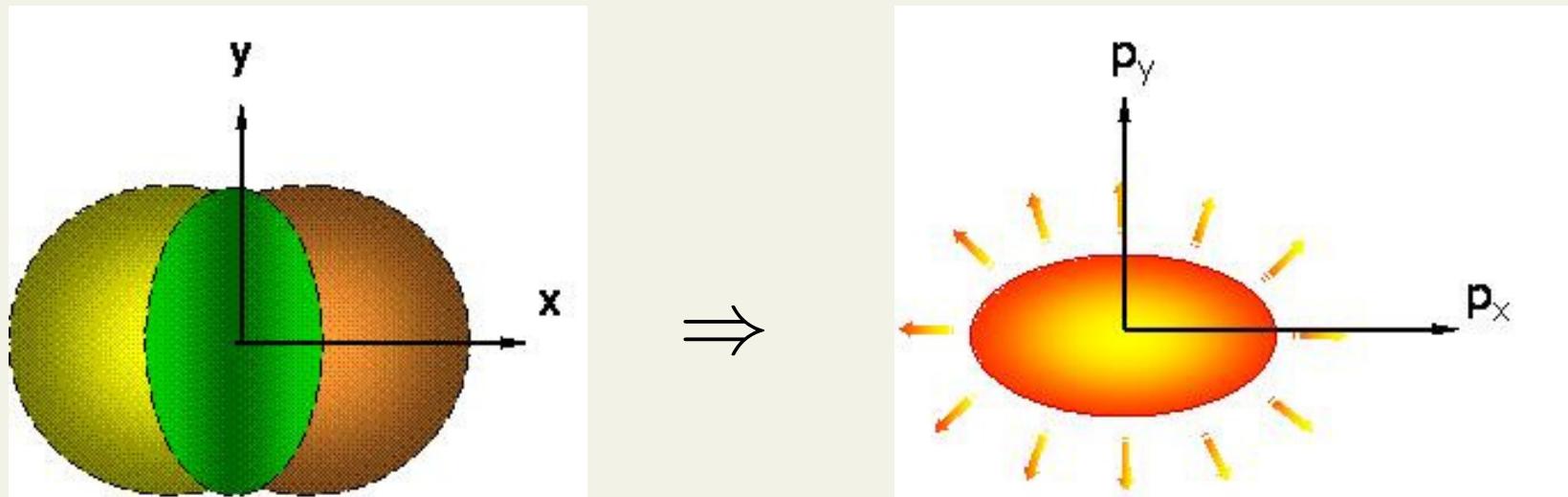


# Elliptic flow $v_2$

spatial anisotropy

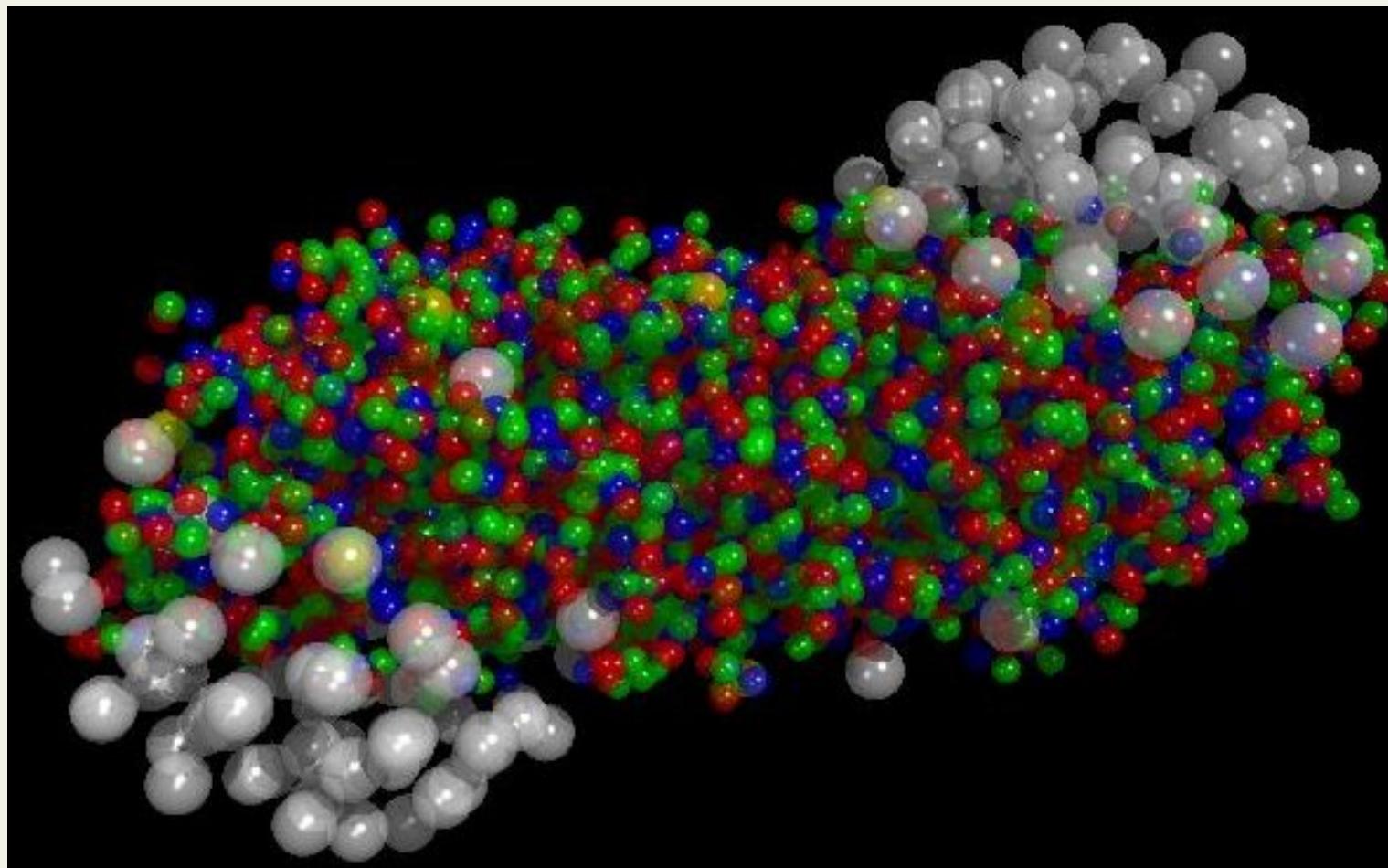


final azimuthal momentum anisotropy



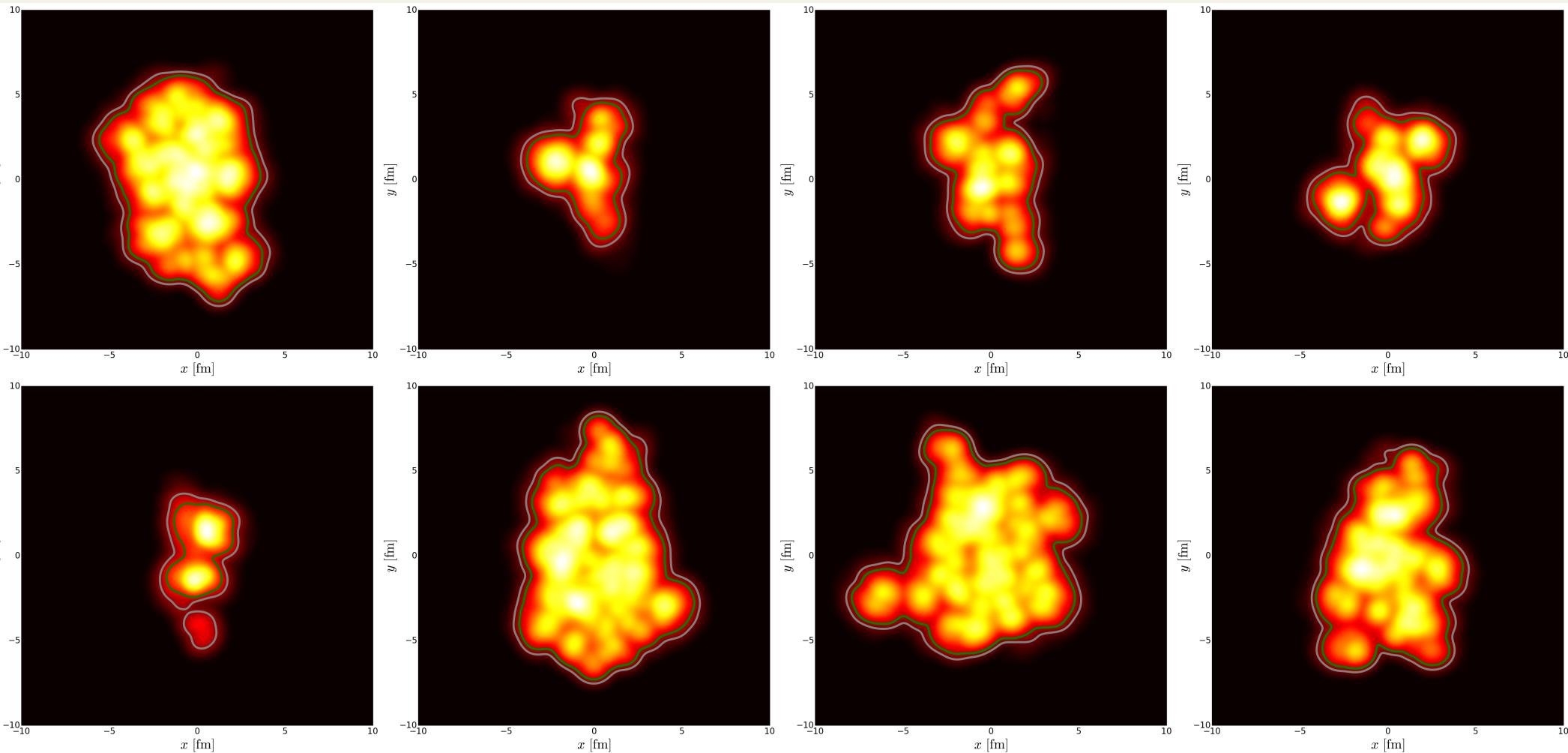
- Anisotropy in coordinate space + rescattering  
⇒ Anisotropy in momentum space
- pressure gradients convert spatial anisotropy to momentum anisotropy

sensitive to speed of sound  $c_s^2 = \partial p / \partial e$  and shear viscosity  $\eta$



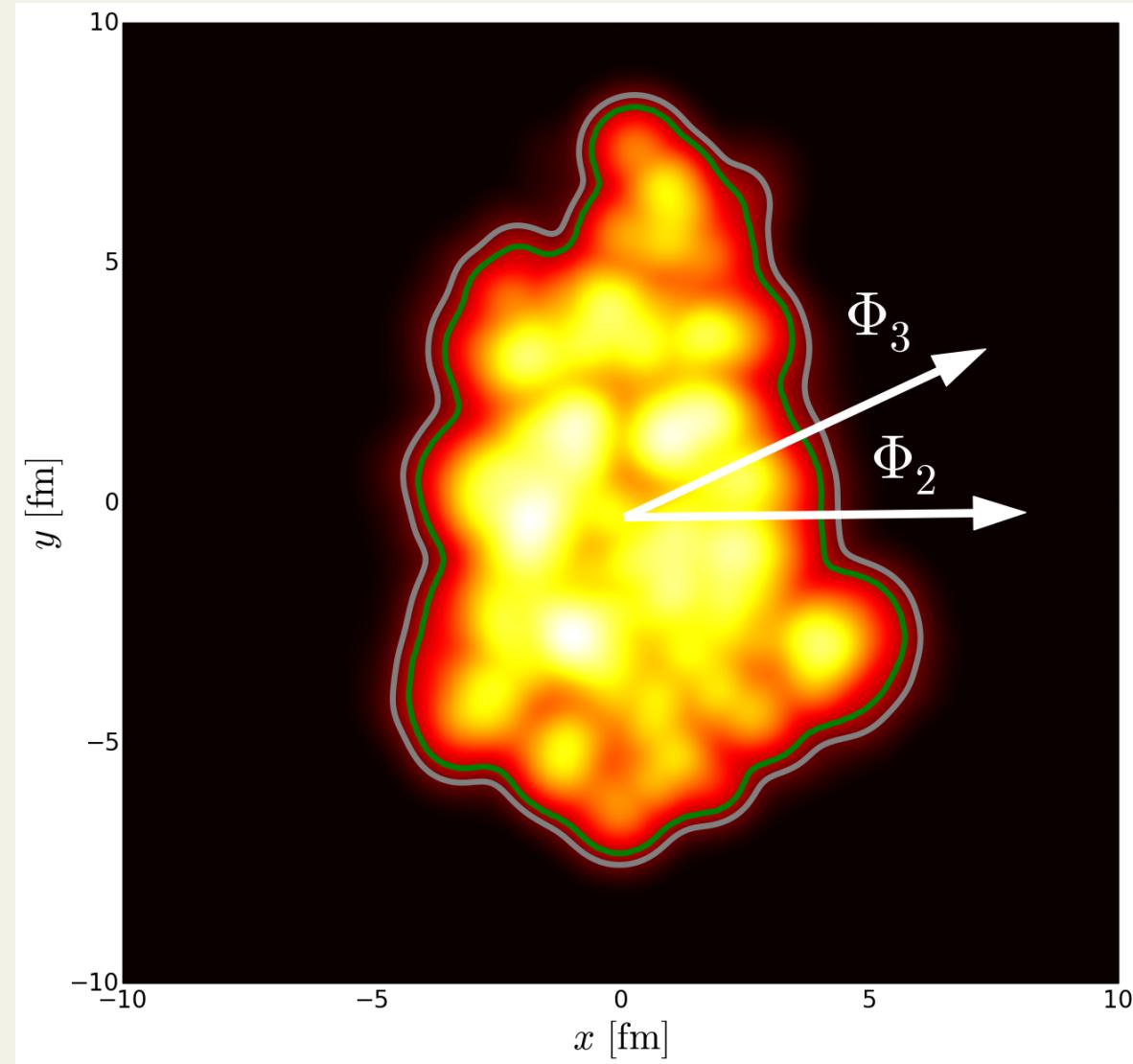
# Initial state fluctuates

temperature profiles in transverse plane



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# Characterising initial state



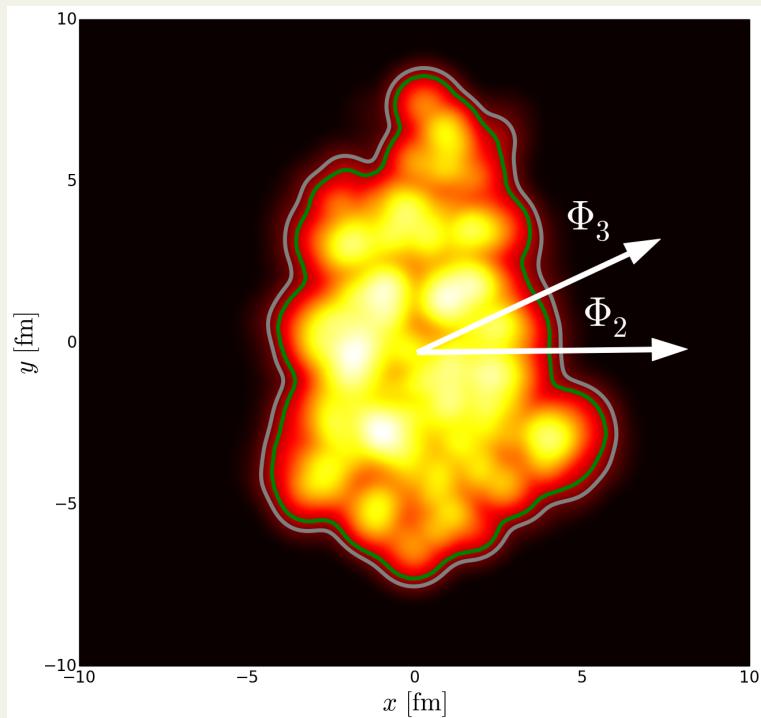
Shape of the initial density quantified by eccentricities:

$$\epsilon_n e^{in\Phi_n} = -\frac{\{r^n e^{in\phi}\}}{\{r^n\}}$$

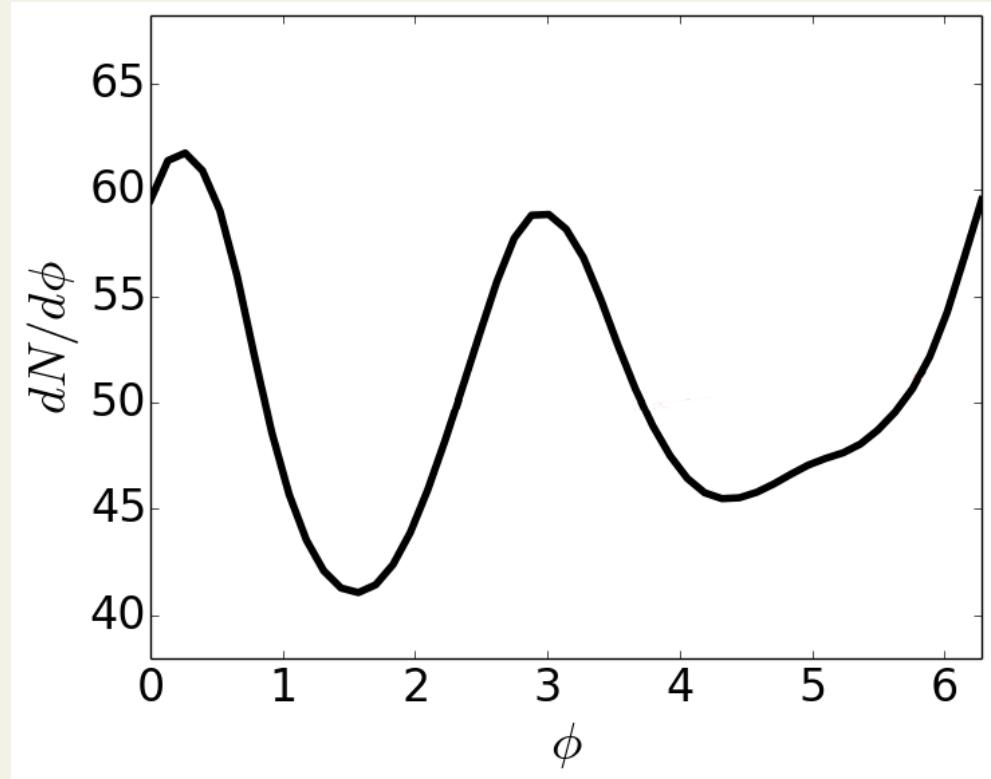
$$\{\dots\} = \int dx dy e(x, y, \tau_0)(\dots)$$

$\epsilon_n$  eccentricity  
 $\Phi_n$  “participant plane” angle

# From fluid to distribution



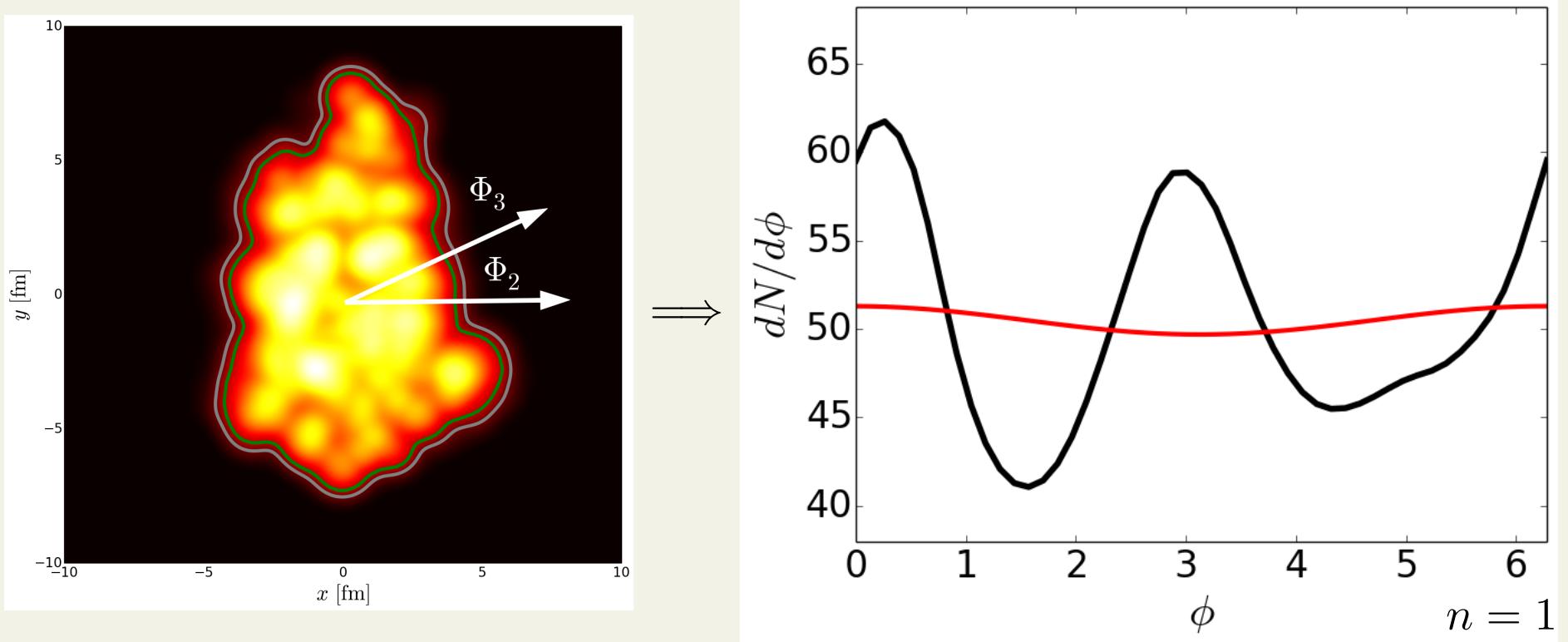
$\Rightarrow$



$\epsilon_n, \Psi_n \implies v_n, \Phi_n$

$$\frac{dN}{dyd\phi} = \frac{dN}{dy} \left[ 1 + \sum_n 2v_n \cos(n(\phi - \Psi_n)) \right]$$

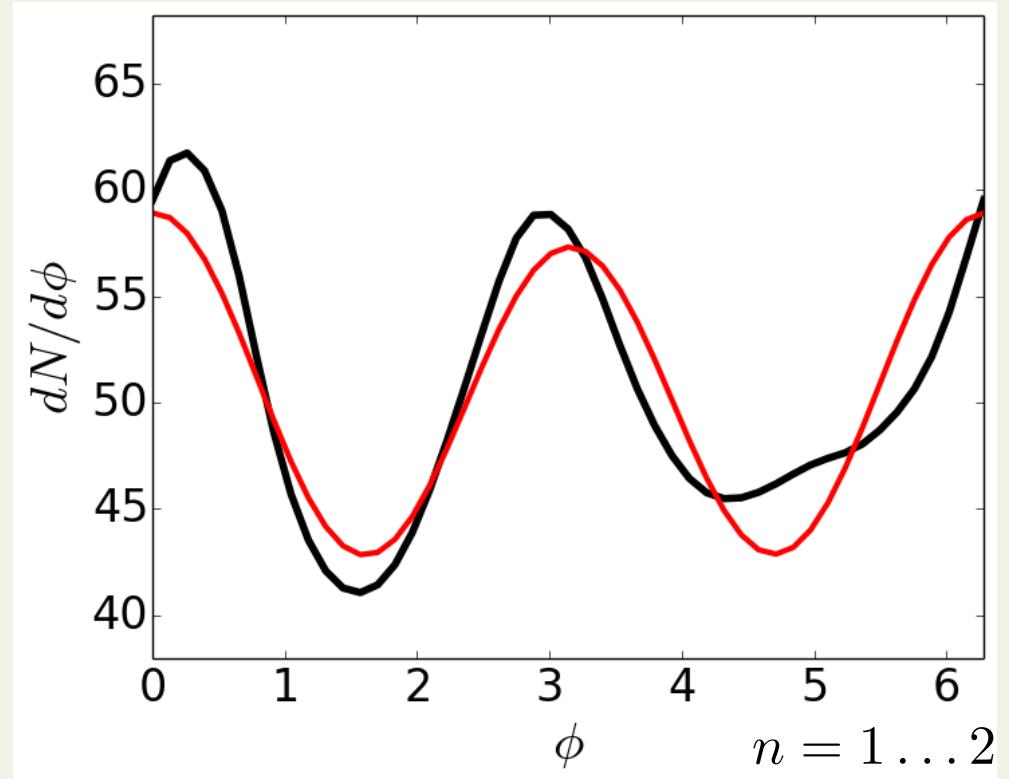
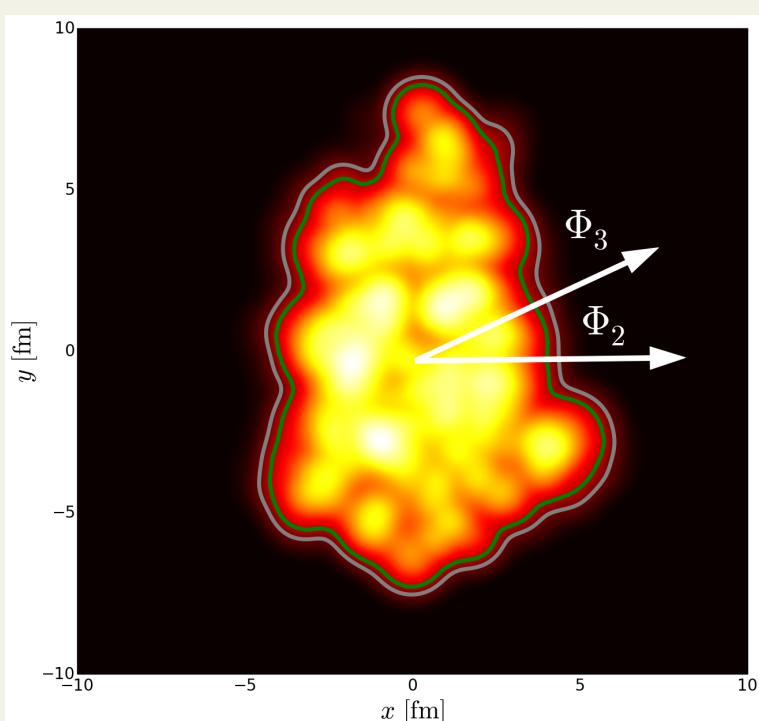
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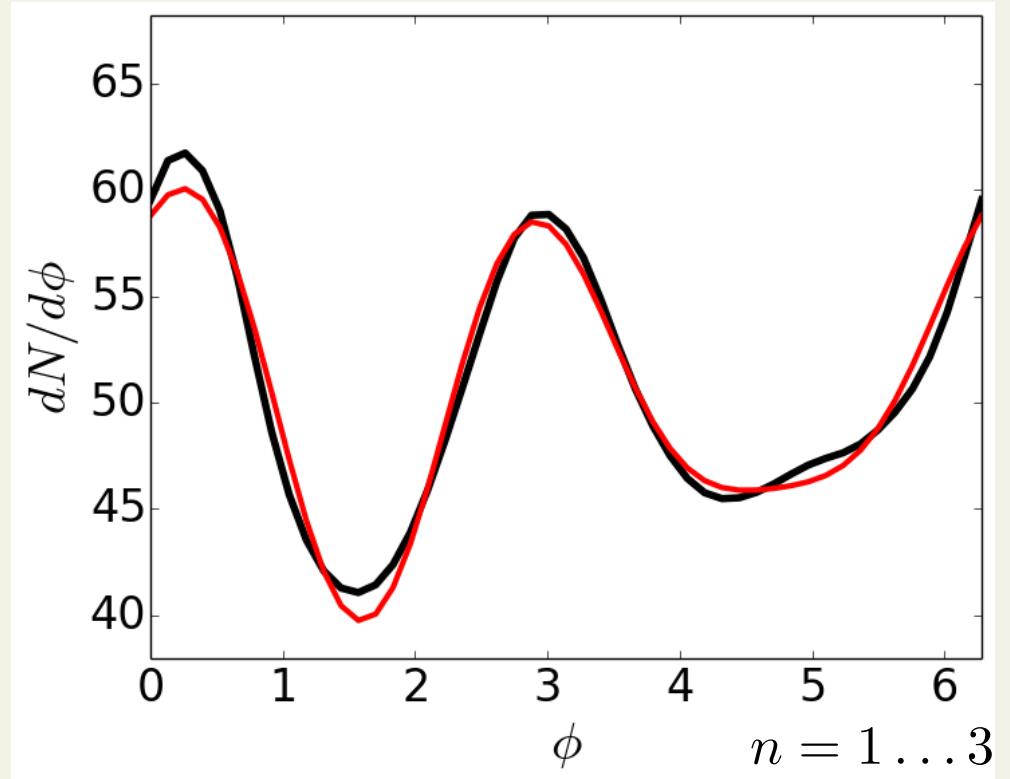
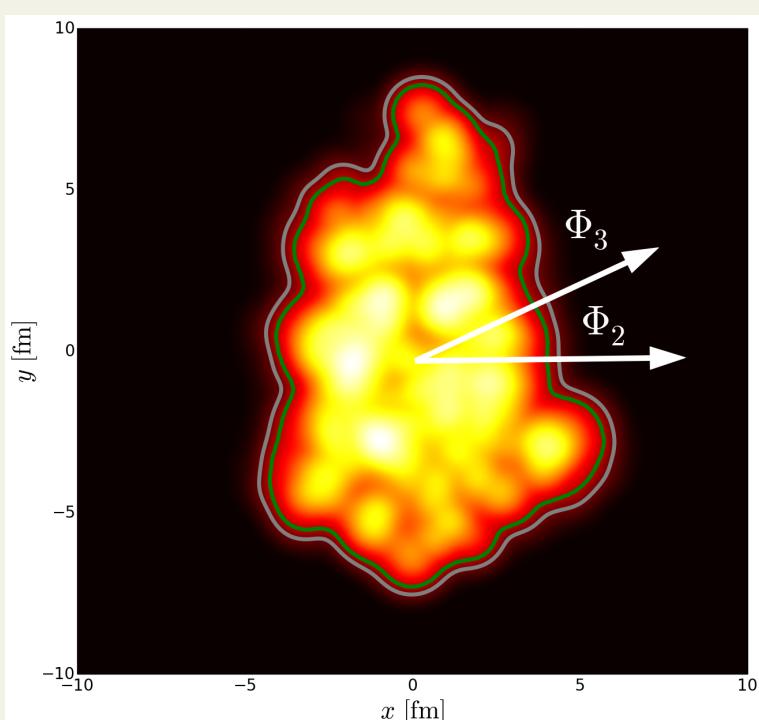
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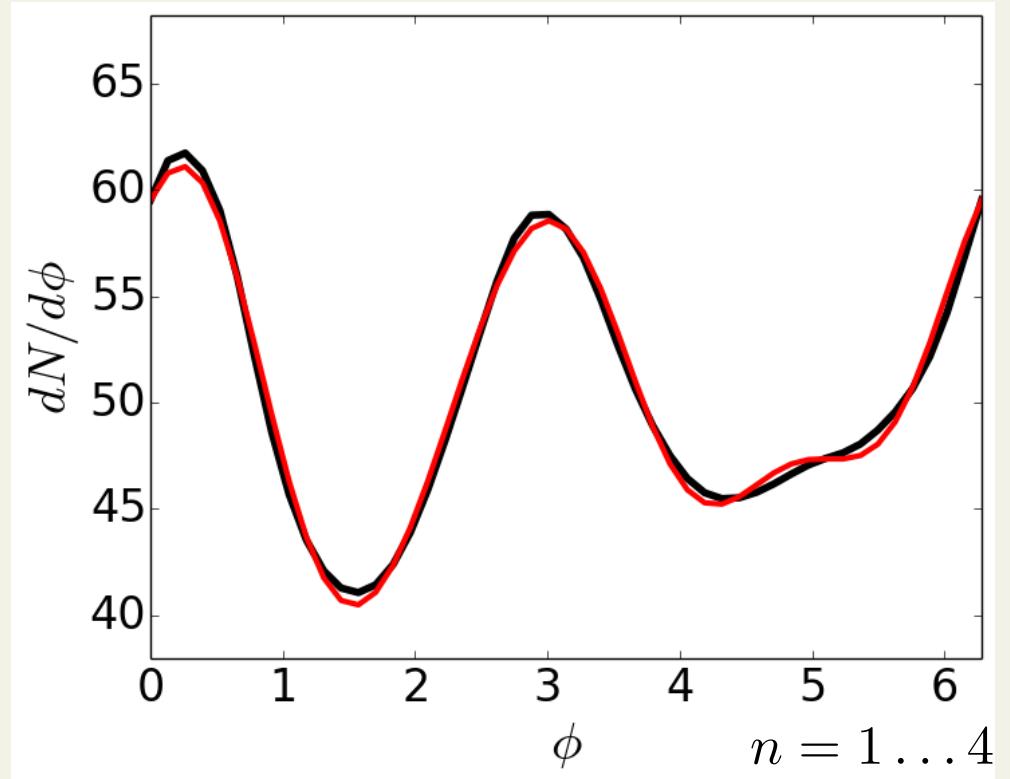
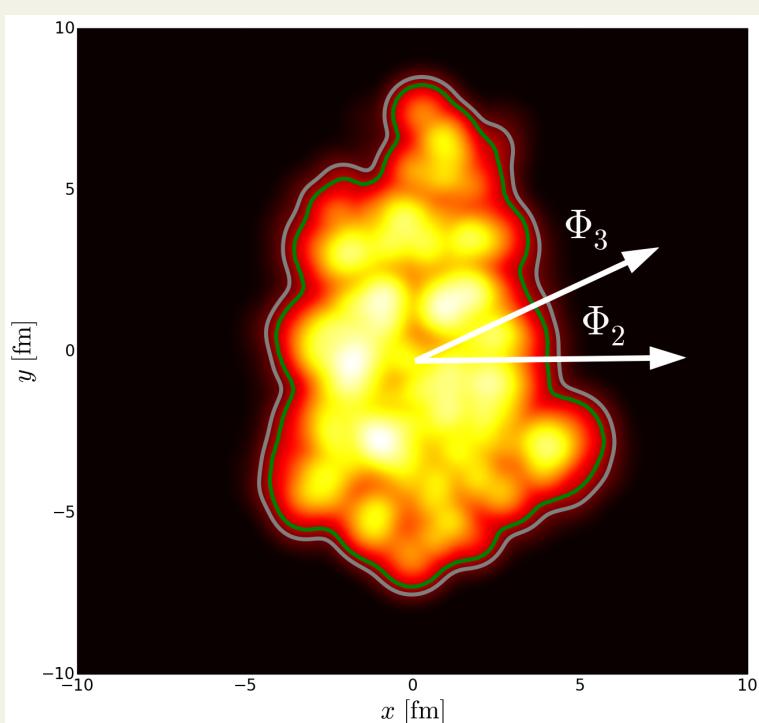
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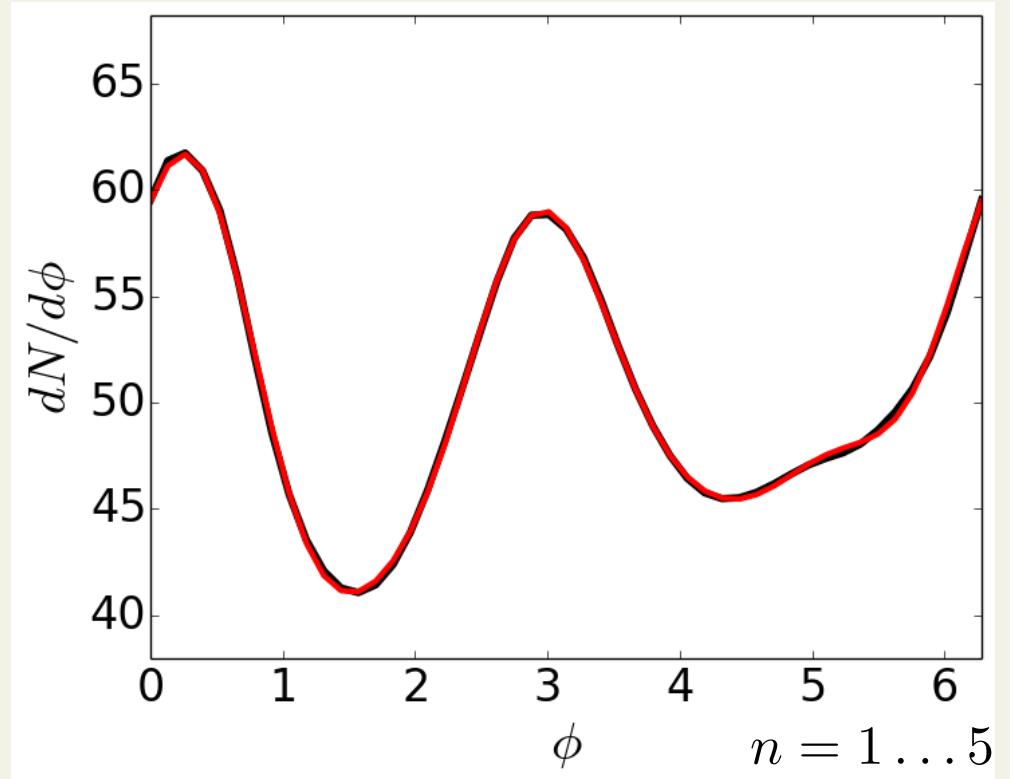
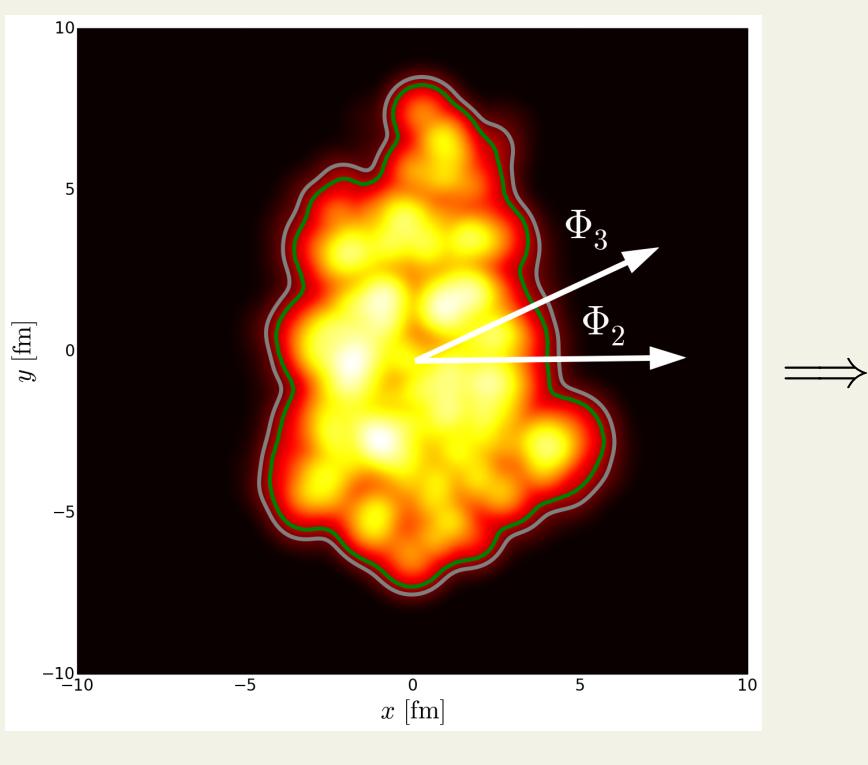
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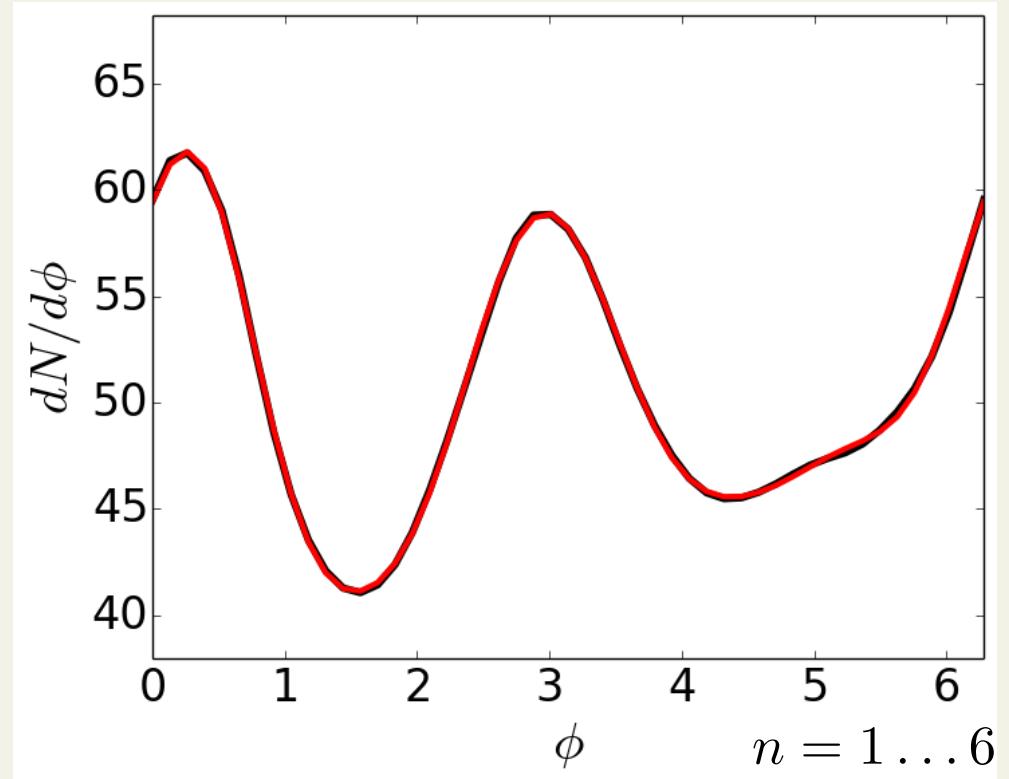
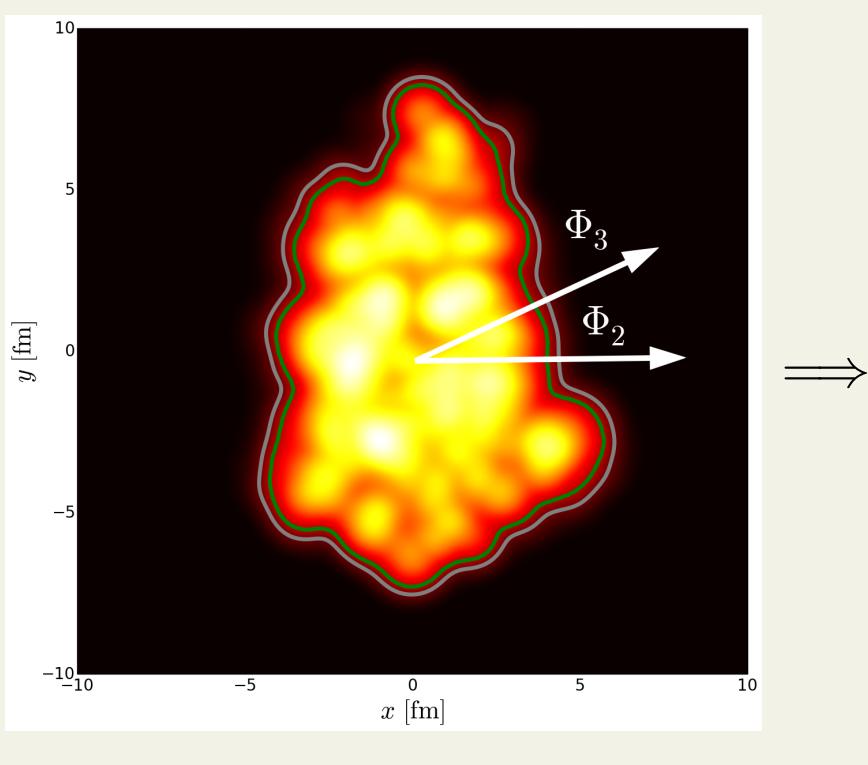
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# From fluid to distribution

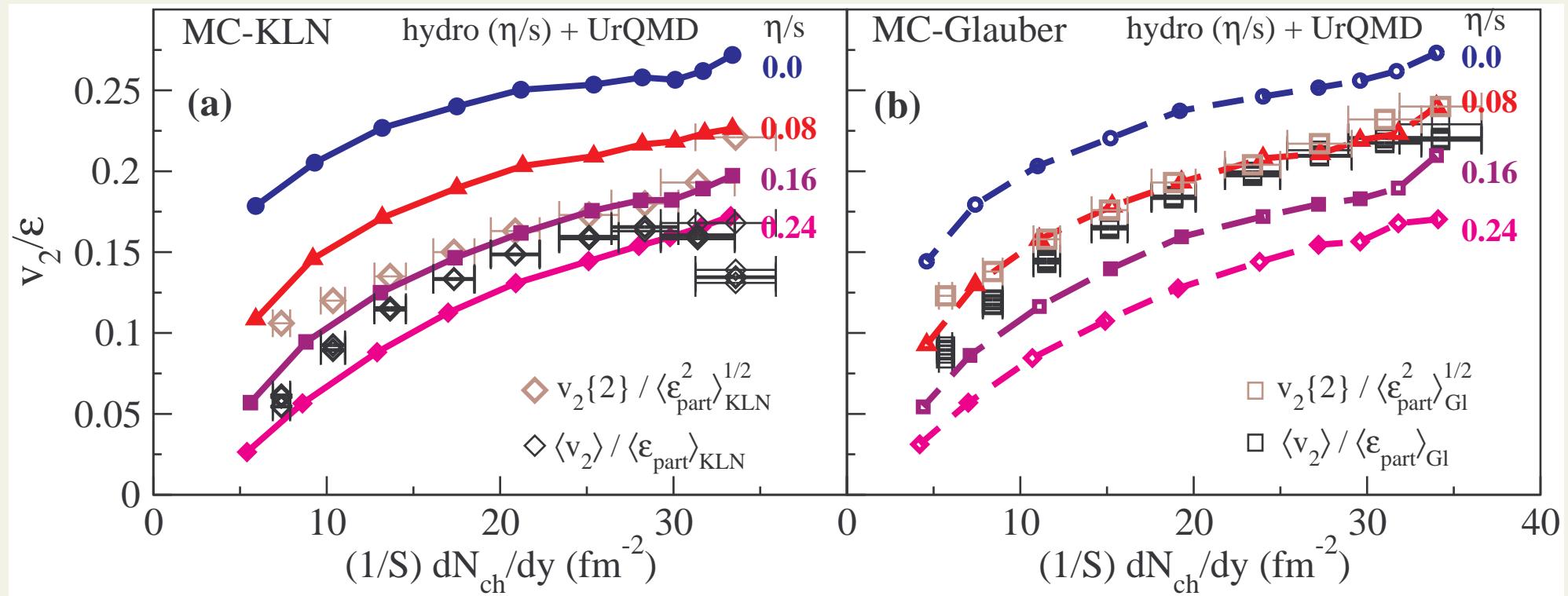


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# $\eta/s$ from $v_2$

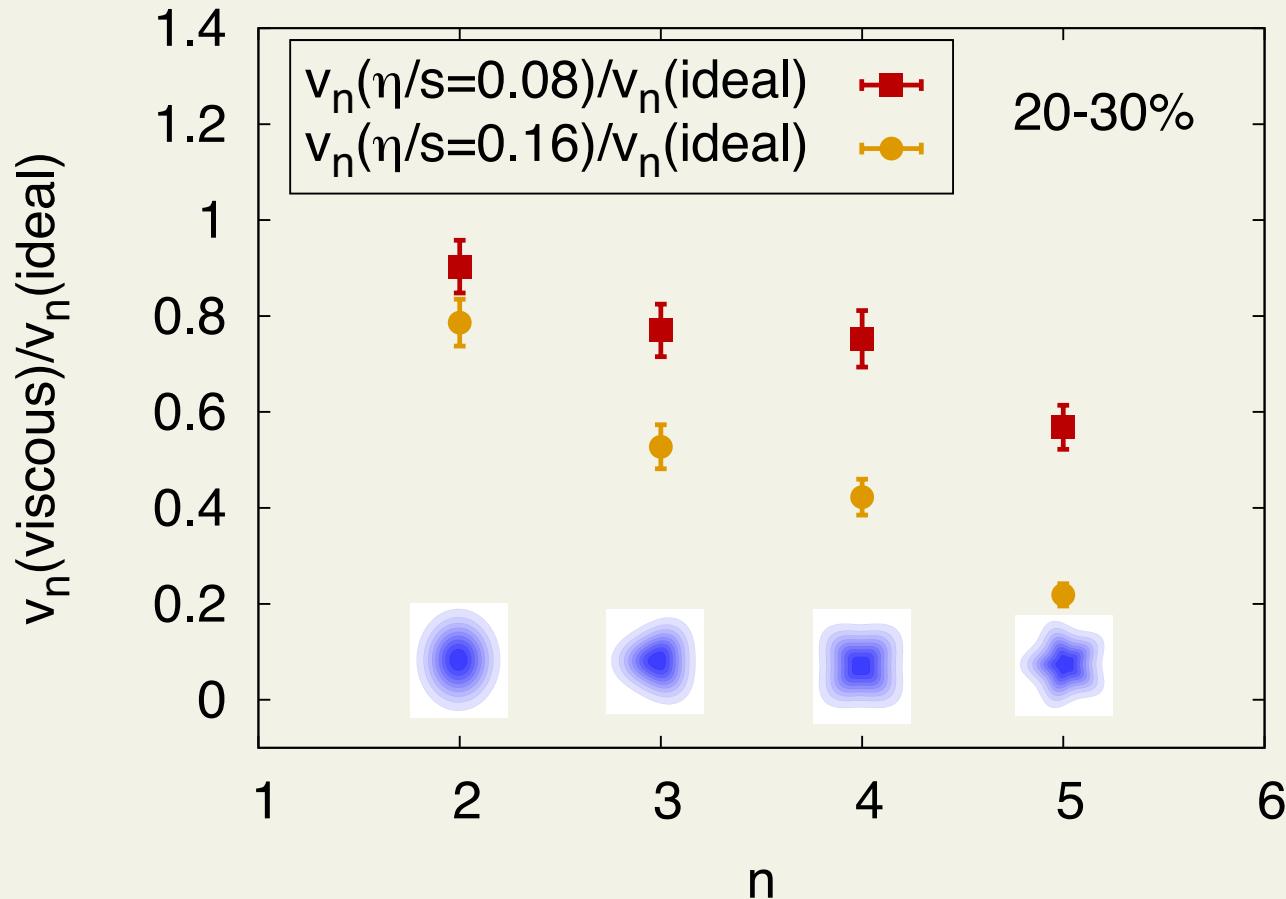
Shen et al. J.Phys.G38:124045,2011



- **MC-Glauber initialization:**  $\eta/s = 0.08$
- **MC-KLN initialization:**  $\eta/s = 0.2$

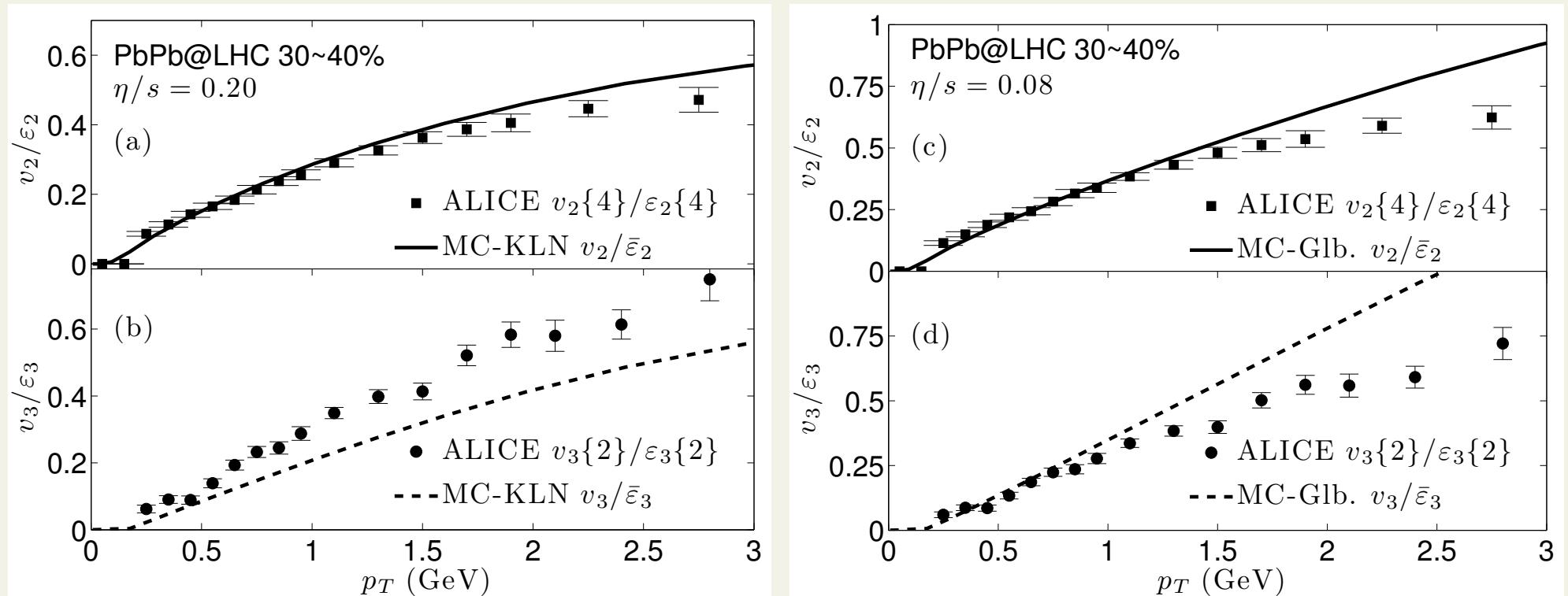
# Sensitivity to $\eta/s$

Schenke et al. Phys.Rev.C85:024901,2012



- higher coefficients are suppressed more by dissipation

Qiu et al. Phys.Lett.B707:151,2012



- models can be distinguished
- MC-Glauber slightly favoured

# Distributions of $v_n$ event-by-event

Scale out the average

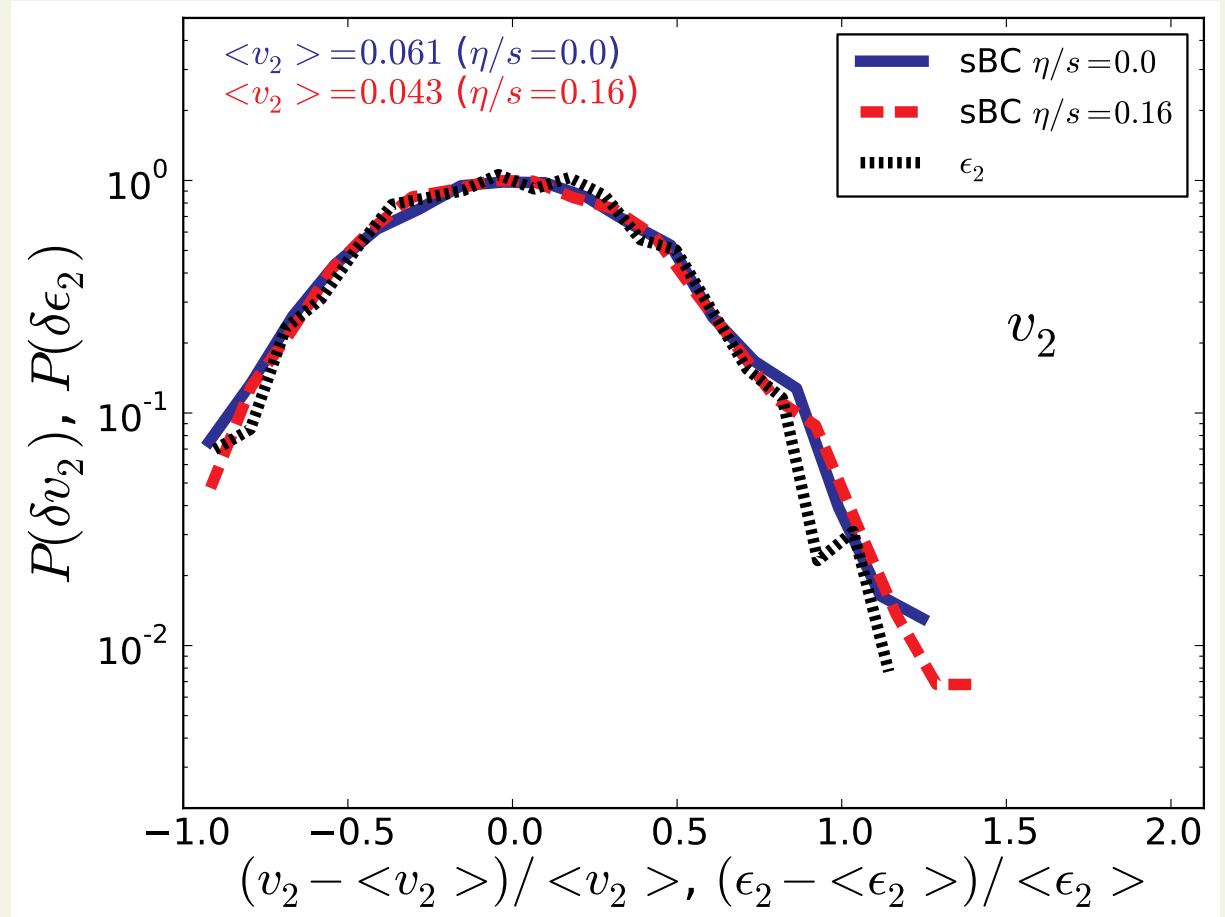
$$\delta v_2 = \frac{v_2 - \langle v_2 \rangle}{\langle v_2 \rangle}$$



$$P(\delta v_2) = P(\delta \epsilon_2)$$

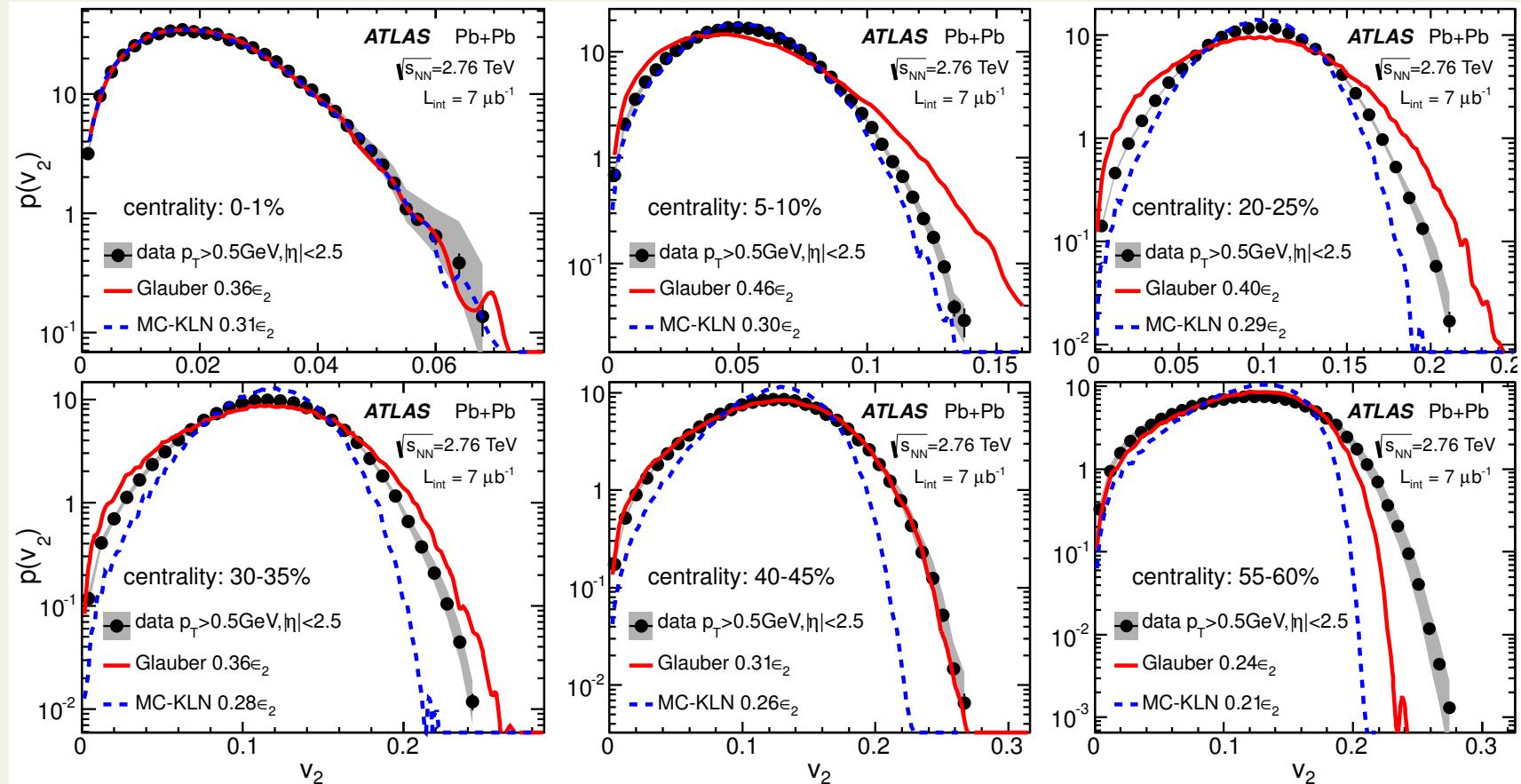
independent of viscosity

Niemi et al. Phys.Rev.C87,054901,2013



# Flow fluctuations

Aad et al. [ATLAS Collaboration] JHEP 1311:183,2013



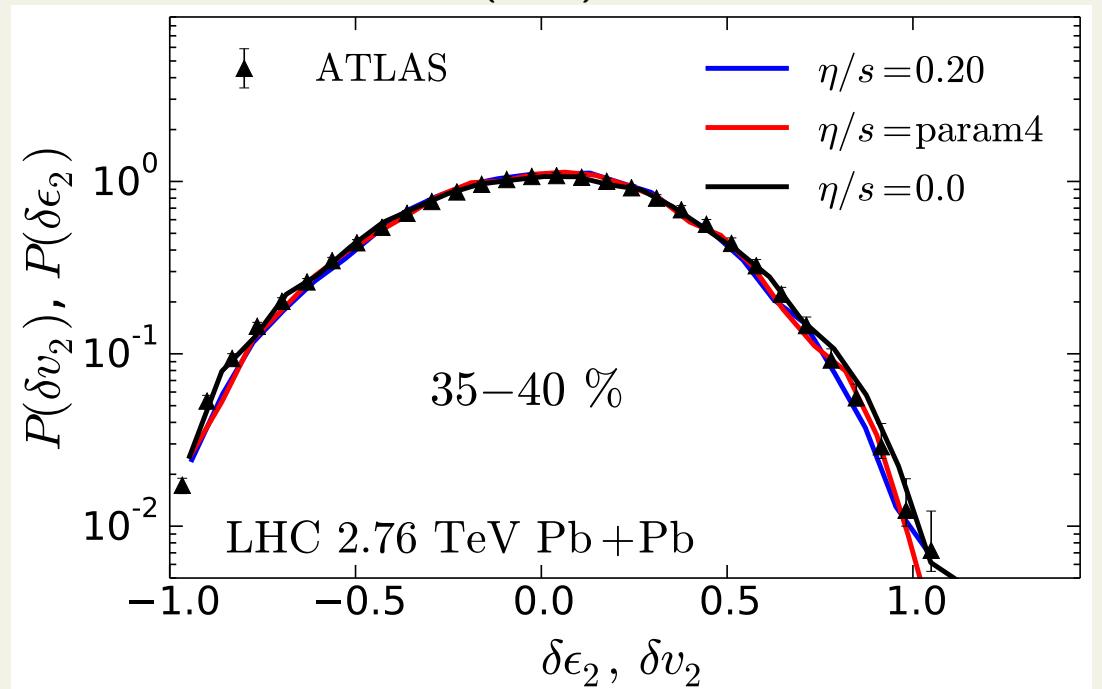
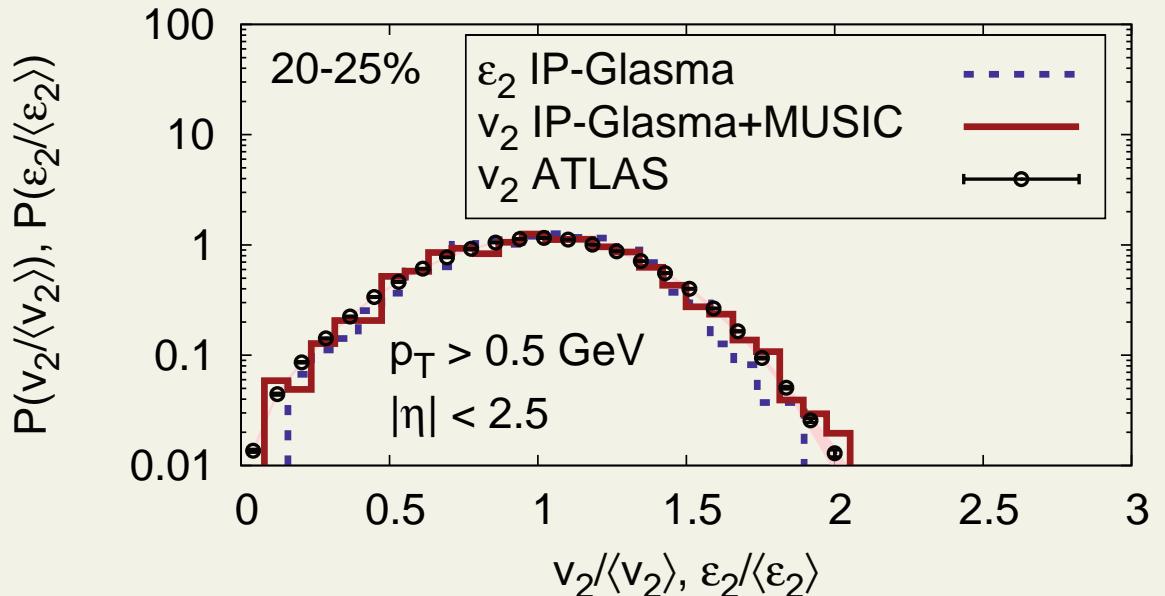
- $P(v_2)$  compared to MC-Glauber and MC-KLN  $P(\epsilon_2)$
- MC-Glauber initialization: too wide
- MC-KLN initialization: too narrow

- IP-Glasma  
(Color Glass + Yang-Mills)

and

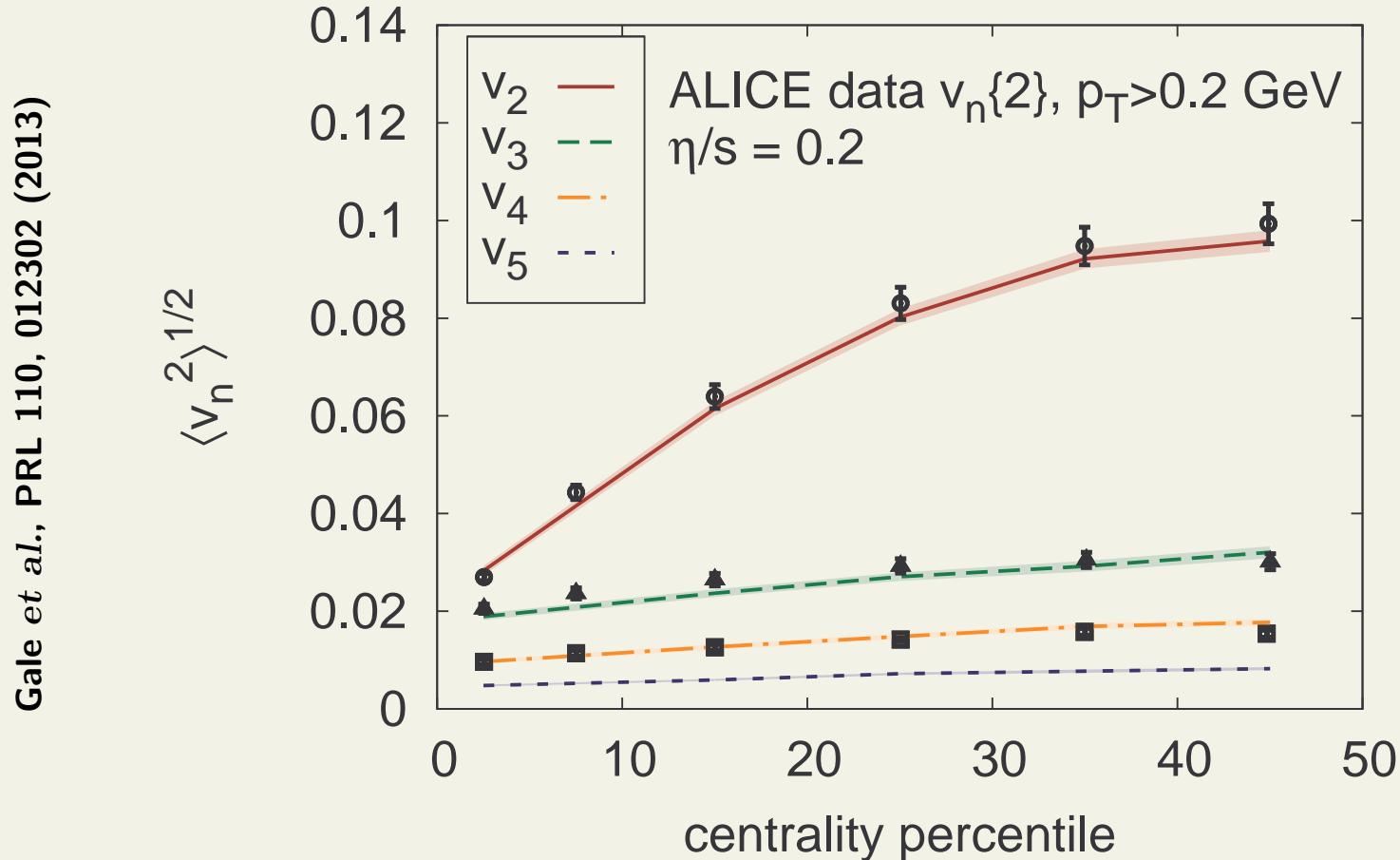
- EKRT  
(pQCD + saturation)

initial states work



# State of the art

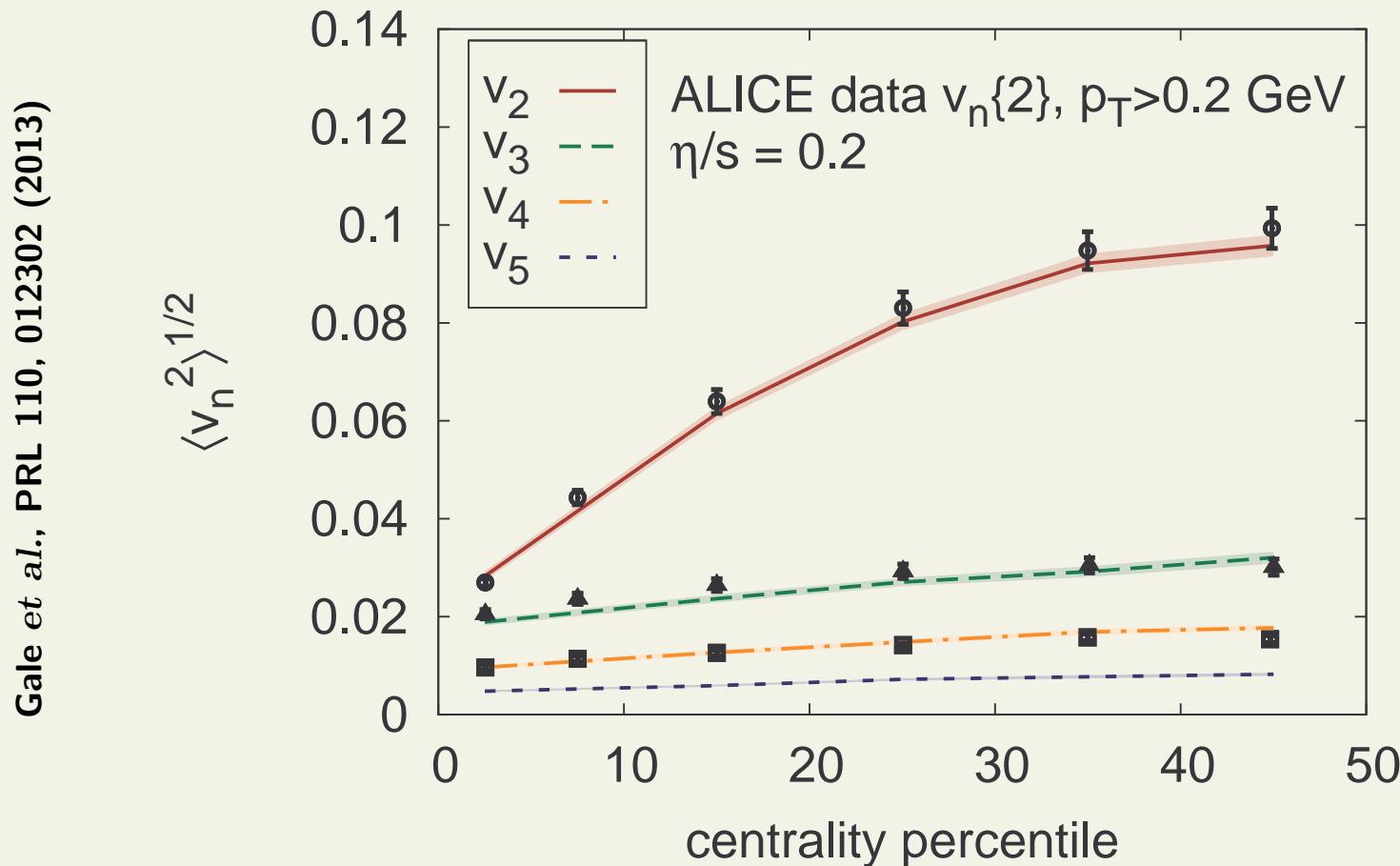
- IP-Glasma initial state: Color Glass plus Yang-Mills evolution



- $\eta/s = 0.2$  favoured

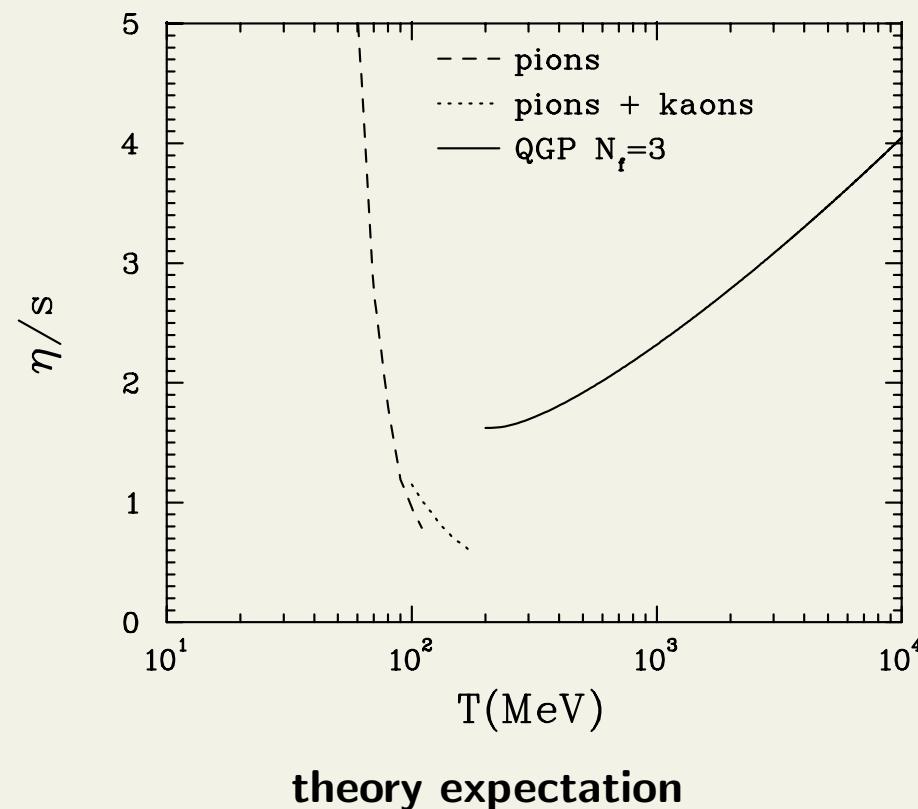
# State of the art

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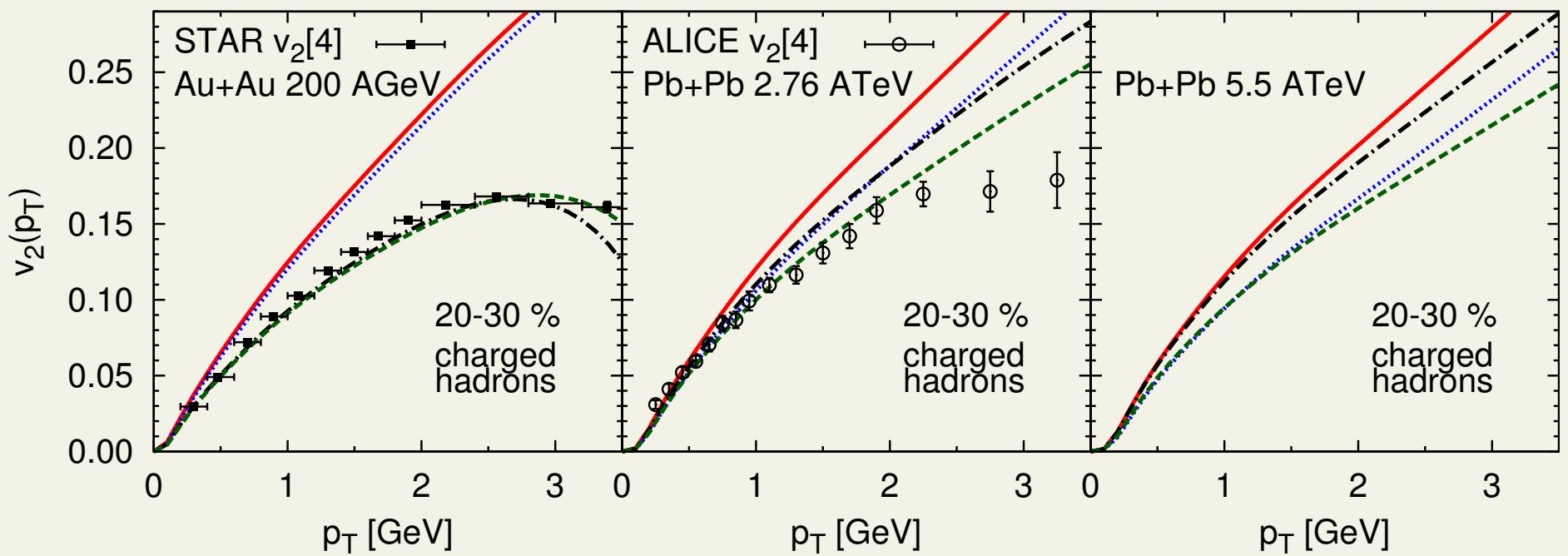
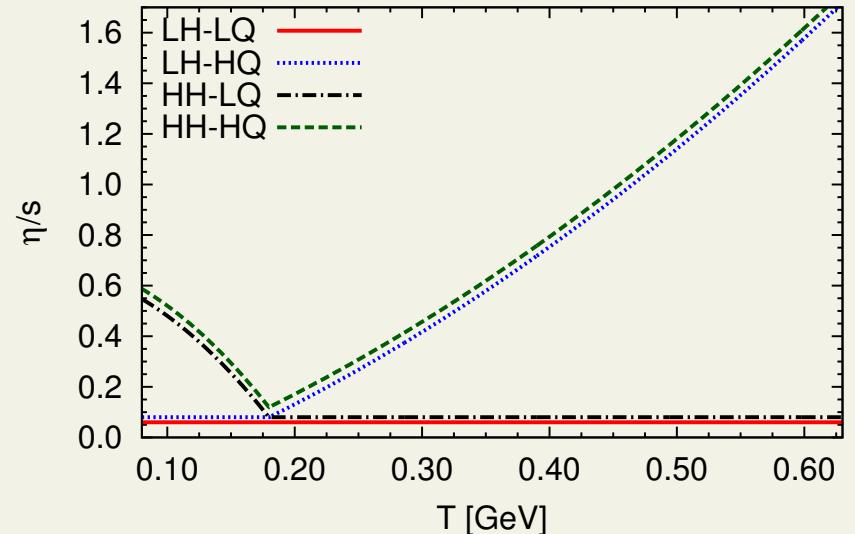
- $\eta/s = 0.2$  favoured at LHC
- $\eta/s = 0.12$  favoured at RHIC

$$\eta/s = \text{const.} \rightarrow (\eta/s)(T)$$



# sensitivity to $(\eta/s)(T)$

- parametrizations of  $(\eta/s)(T)$   
 L="low", H="high"  
 H="hadronic", Q="qgp"



- weak dependence on QGP  $\eta/s$  at RHIC
- increasing sensitivity to QGP  $\eta/s$  with collision energy at LHC
- sensitive to minimum of  $\eta/s$

# Summary

- hydrodynamics can describe the anisotropies of particle emission observed in ultrarelativistic heavy-ion collisions
- the minimum specific shear viscosity of matter formed in these collisions is very low,  $\eta/s \lesssim 2.5/(4\pi)$
- temperature dependence of  $\eta/s$  is to be determined



This talk consisted of 100% recycled electrons