



# Hadronic decays of excited bottomonium states at Belle and Belle II

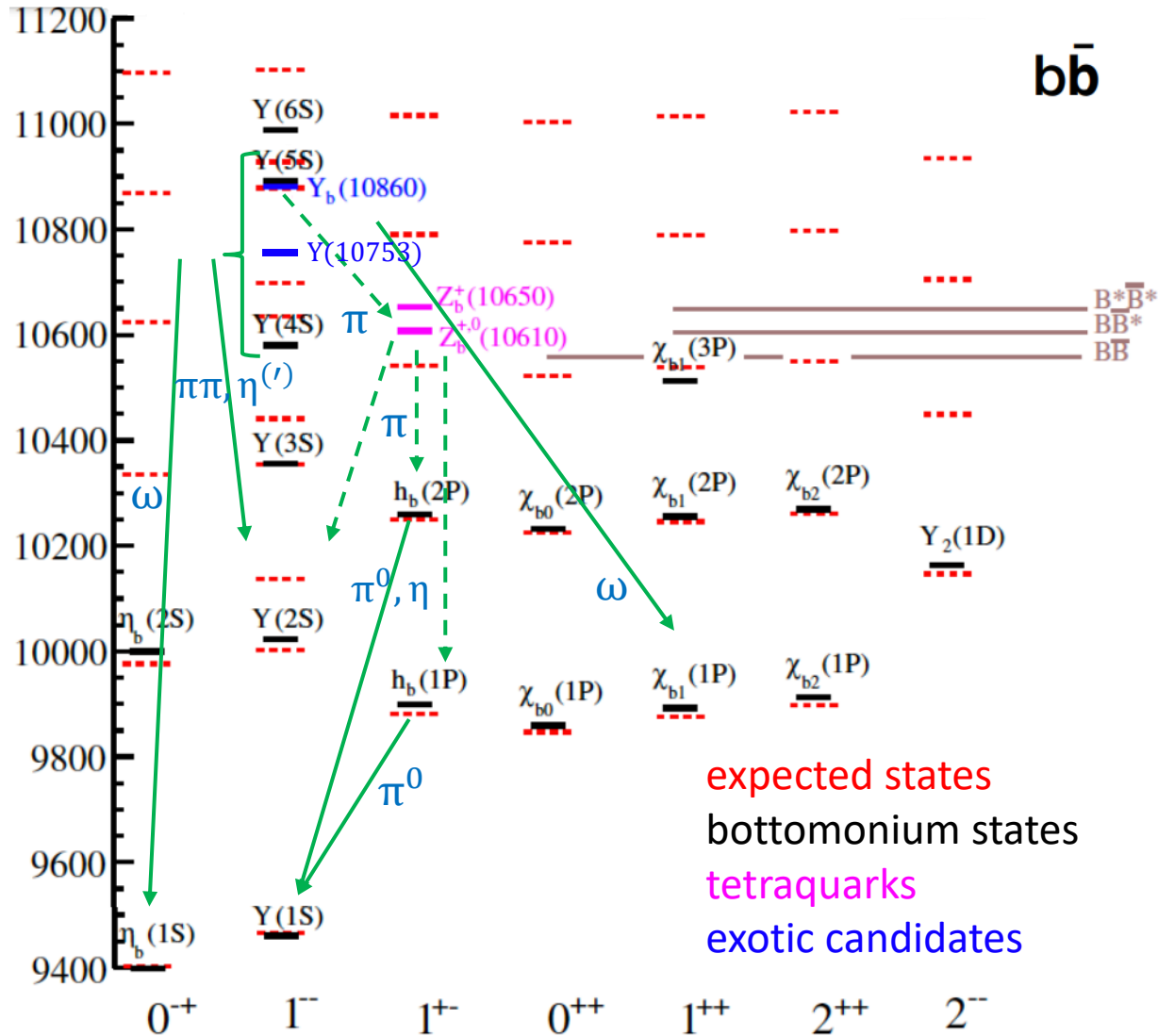
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EVGENIY KOVALENKO

BINP

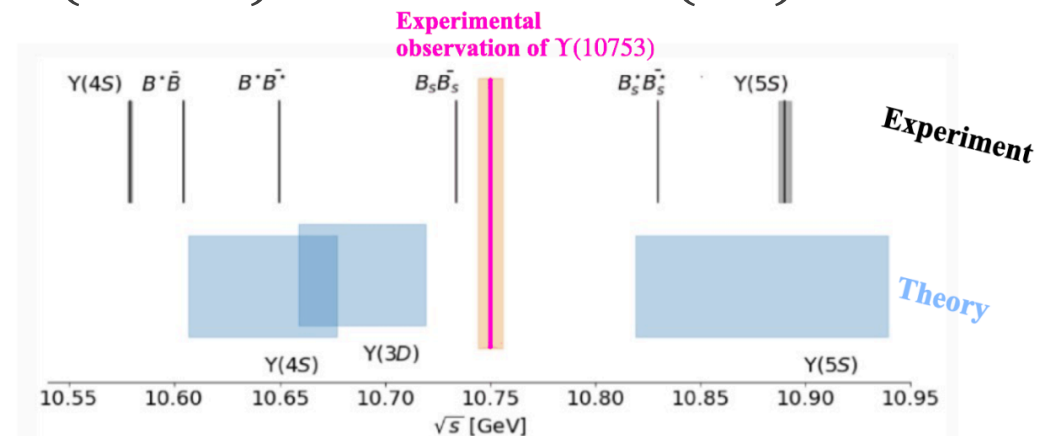
OCTOBER 24<sup>th</sup>, ICPPA2024

# Bottomonium family

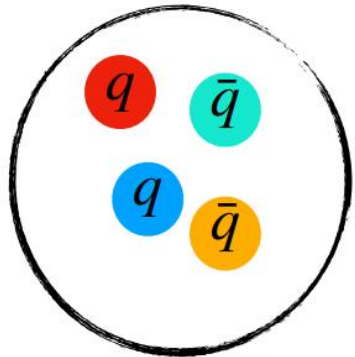


Bound state of  $b\bar{b}$

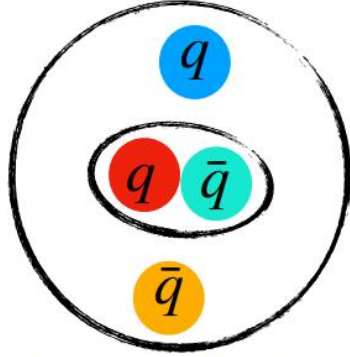
- Properties below  $B\bar{B}$  threshold are as expected
- Above  $B\bar{B}$  - anomalous rate of  $\pi\pi, \eta^{(\prime)}$  transitions
- Tetraquarks  $Z_b(10610, 10650)$  ( $T_{b\bar{b}1}$ ) observed in  $\pi\pi$  transitions, with  $I^G(J^{PC}) = 1^+(1^{+-})$
- $Y(10753)$  is observed -  $Y(3D)$  or exotic?



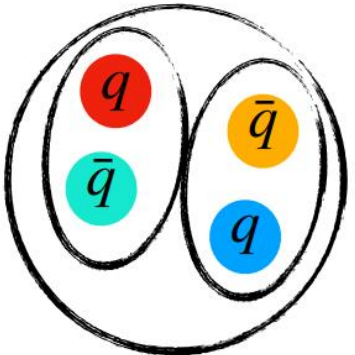
# Structure above $B\bar{B}$ threshold



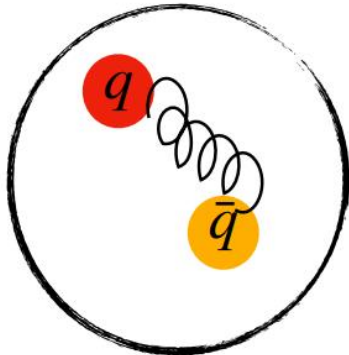
tetraquark



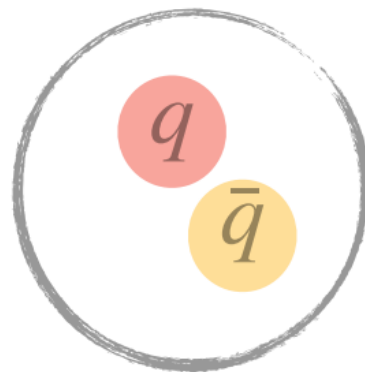
hadro-quarkonium



hadronic molecule



hybrid



conventional  
meson

Including S-D state mixing

- Unexpected states observed also in charmonium (X(3872), Y(4260))
- No definite interpretations
- Better understanding is needed

# Belle and Belle II experiments

Conducted at KEKB/SuperKEKB colliders, Japan

- Asymmetric  $e^+e^-$  colliders
- Center-of-Mass energy mostly at 10.58 GeV ( $Y(4S)$ )

## KEKB

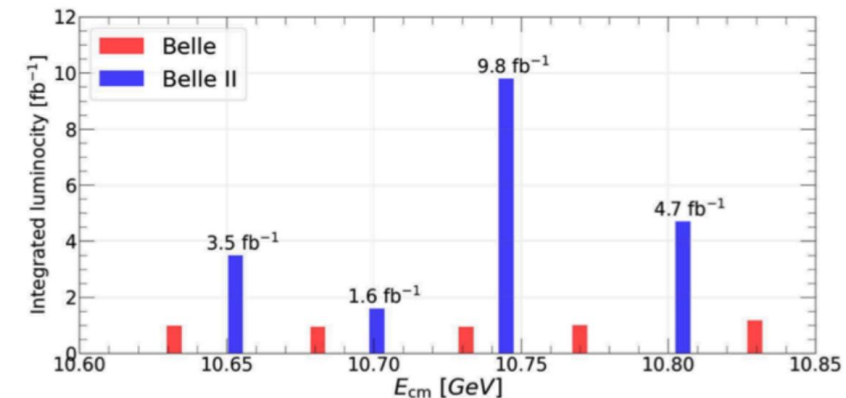
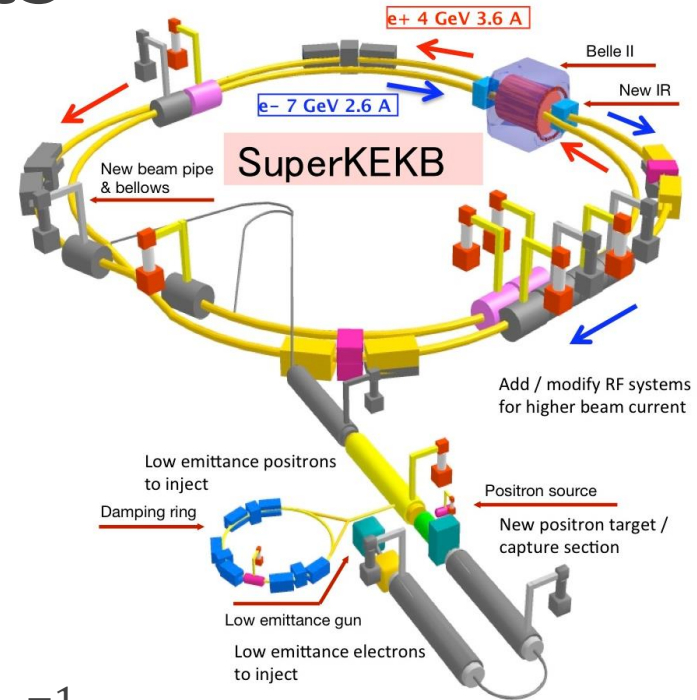
1999-2010

- $e^+(3.5 \text{ GeV}) e^-(8 \text{ GeV})$
- $L_{peak} = 2.1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- $\int L dt = \begin{cases} 711 \text{ fb}^{-1} \text{ at } Y(4S) \\ 21 \text{ fb}^{-1} \text{ scan data} \\ 121 \text{ fb}^{-1} \text{ at } Y(5S) \end{cases}$

## SuperKEKB

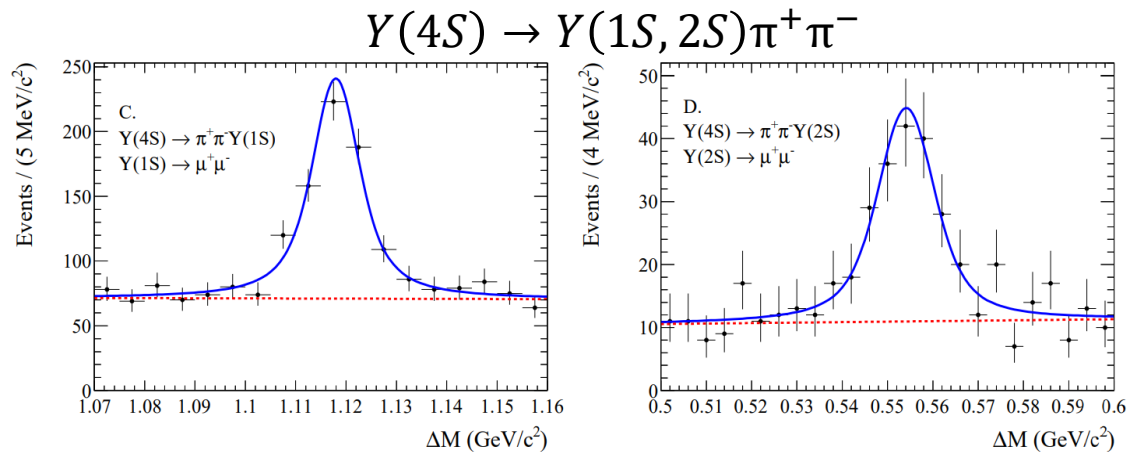
2018-current

- $e^+(4 \text{ GeV}) e^-(7 \text{ GeV})$
- $L_{peak} = 4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- $L_{target} = 6 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$
- $\int L dt = \begin{cases} > 430 \text{ fb}^{-1} \text{ at } Y(4S) \\ 20 \text{ fb}^{-1} \text{ at } Y(10753) \end{cases}$
- Target  $\int L dt \sim 50 \text{ ab}^{-1}$



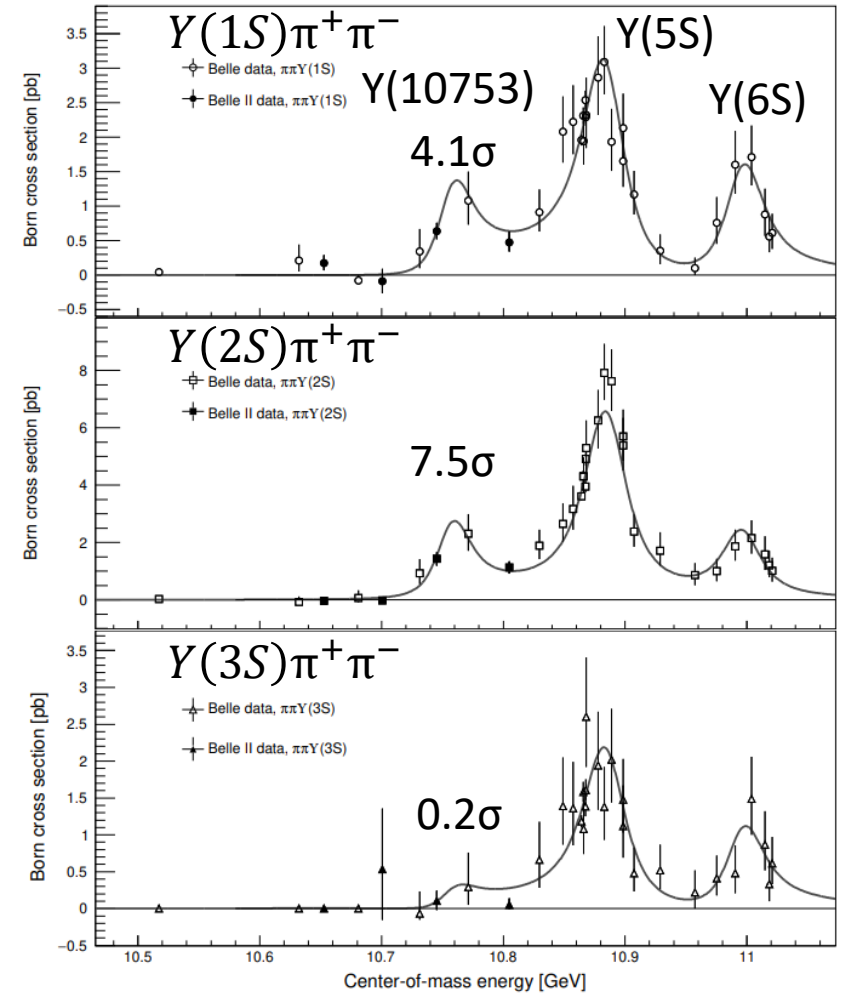
# $Y(4S, 10753, 5S) \rightarrow Y(1S, 2S, 3S)\pi^+\pi^-$

- $Y(4S)$ : compatible with  $b\bar{b}$
- $Y(10753)$ : resonance confirmed, no intermediate  $Z_b$ , structure - ?
- $Y(5S)$ : intermediate  $Z_b$  was discovered  
Non- $Z_b$  rate still **does not support  $b\bar{b}$  (x100)**



$M(\mu\mu\pi\pi) - M(\mu\mu)$  distribution at  $Y(4S)$

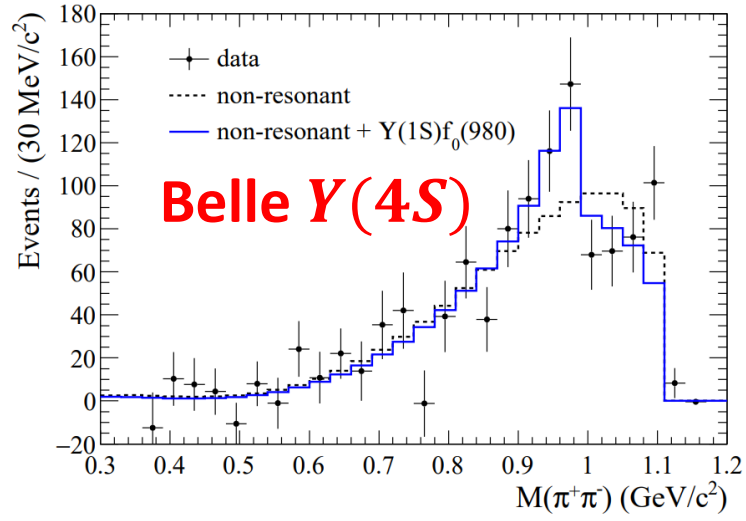
PRD 96 (2017) 5, 052005



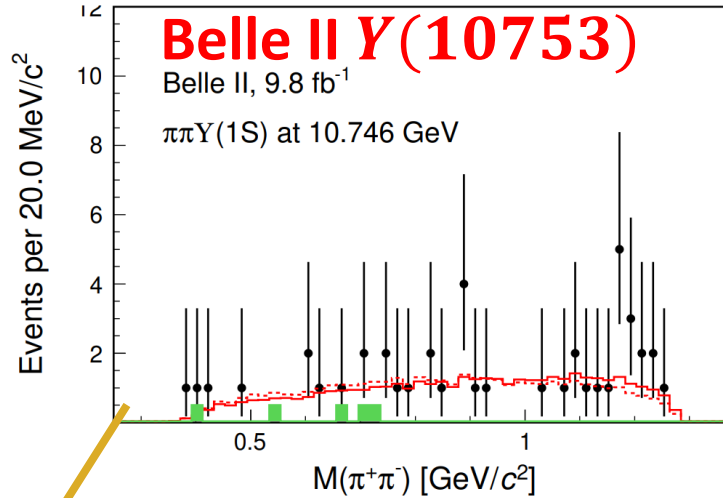
Cross section dependence above  $Y(4S)$

JHEP 07 (2024) 116

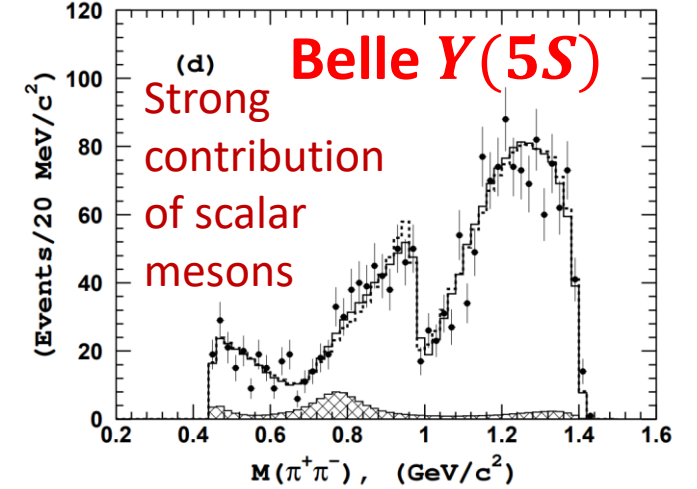
# Di-pion mass spectrum for $Y(1S)\pi^+\pi^-$



PRD 96 (2017) 5, 052005

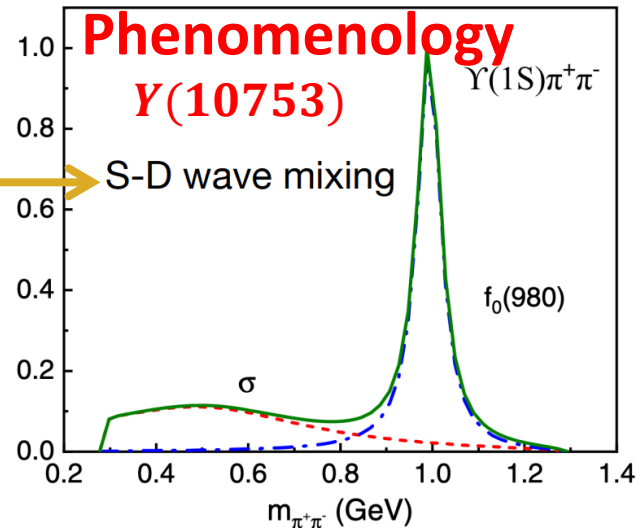


JHEP 07 (2024) 116

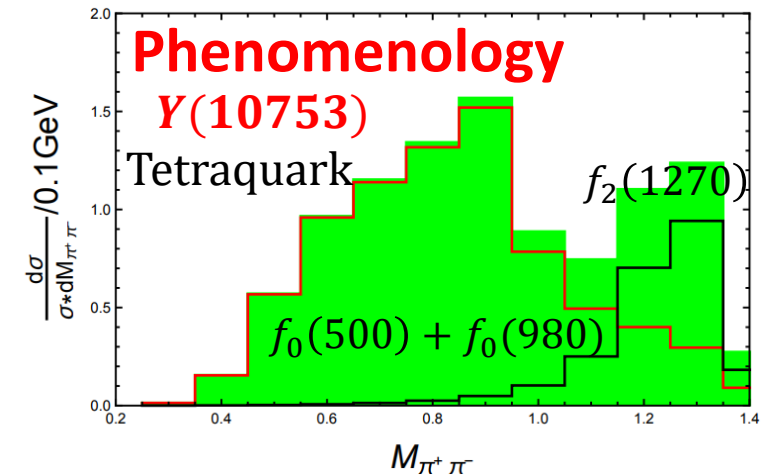


PRD 91 (2015) 7, 072003

- $Y(4S)$ : indication of  $f_0(980)$
- $Y(10753)$ : no  $f_0(980)$ , **no sign of S-D mixing**, compatible with tetraquark?
- $Y(5S)$ :  $Z_b$ ,  $f_0(980)$ ,  $(\pi^+\pi^-)_D$  wave



PRD 105 (2022) 7, 074007



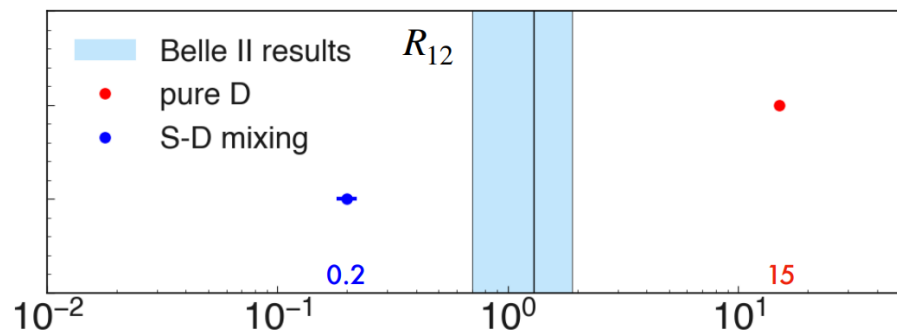
PLB 802 (2020) 135217



# $Y(10753, 5S) \rightarrow \chi_{bJ}(1P)\omega$

■  $Y(10753)$  : observed ( $J = 1, 2$ )

$$R_{12} = \frac{\Gamma_{ee} \times B[Y(10753) \rightarrow \chi_{b1}(1P)\omega]}{\Gamma_{ee} \times B[Y(10753) \rightarrow \chi_{b2}(1P)\omega]} = 1.3 \pm 0.6$$



PRD 104, 034036 (2021)

PLB 2014.09.043

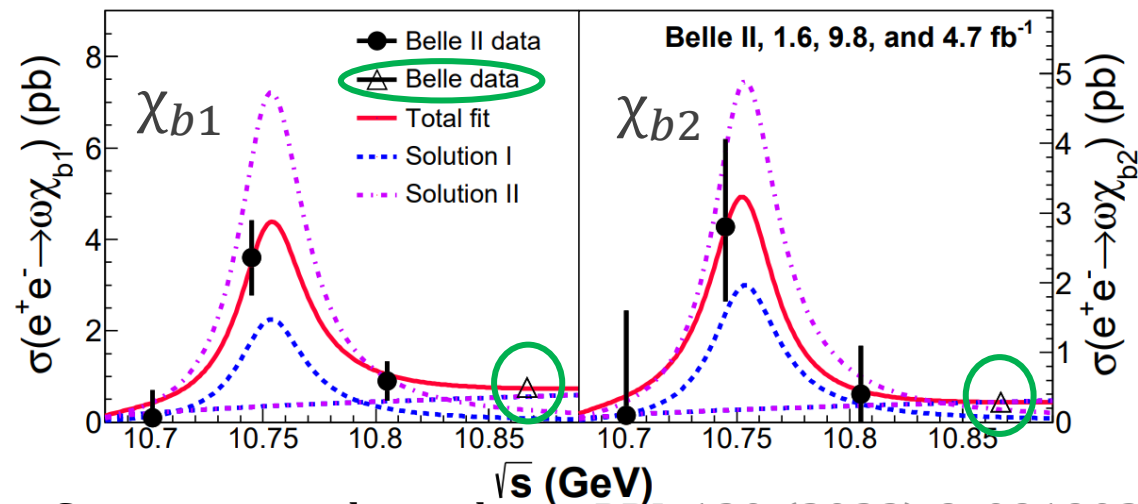
Does not support pure 3D,  $1.8\sigma$  discrepancy from S-D mixing

■  $Y(5S)$  : observed ( $J = 1, 2$ )

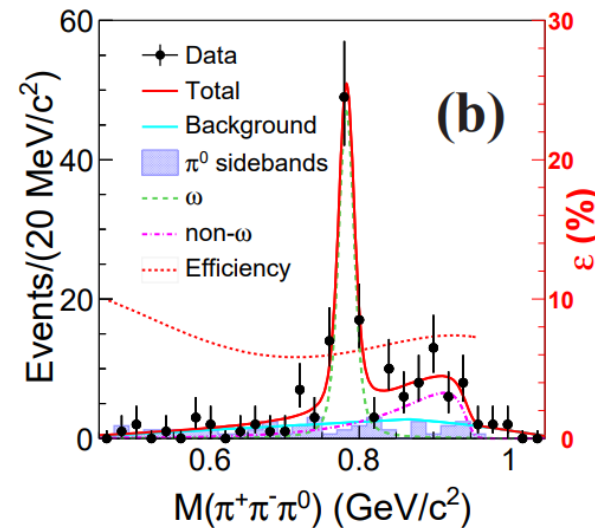
$$R_{12} = 2.6 \pm 1.1 \quad (0.63 \text{ is expected for } b\bar{b} 5S)$$

$$\frac{\sigma[e^+e^- \rightarrow \chi_{b1}(1P)\omega]}{\sigma[e^+e^- \rightarrow Y(1S)\pi^+\pi^-]} \approx \begin{cases} 5.6 \text{ at } Y(10753) \\ 0.3 \text{ at } Y(5S) \end{cases}$$

Different structure? Tail from  $Y(10753)$ ?



Cross-section dependence PRL 130 (2023) 9, 091902

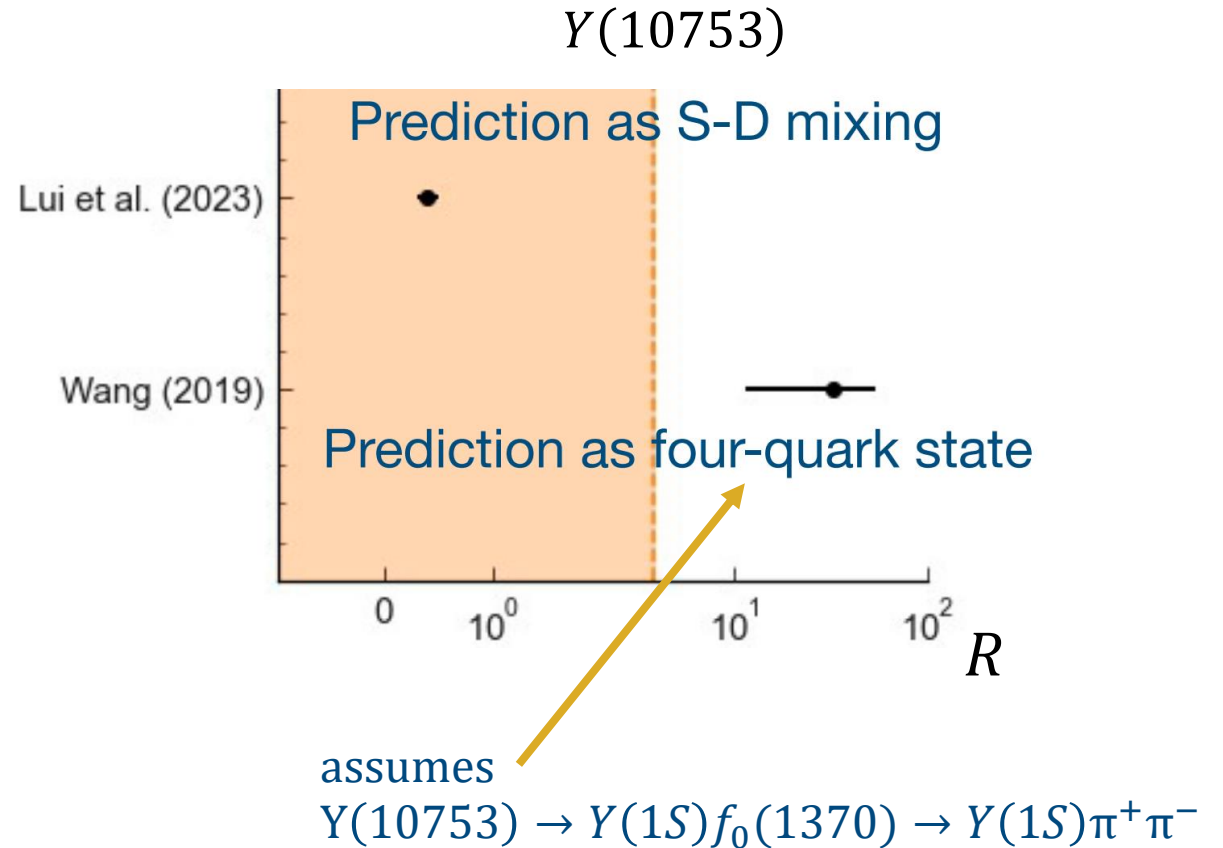


Distribution at  $Y(5S)$  PRL 113 (2014) 14, 142001

# $Y(4S, 10753, 5S) \rightarrow \eta_b(1S)\omega$

- $Y(4S)$  : PRD 102 (2020) 9, 092011  
 $B[Y(4S) \rightarrow \eta_b(1S)\omega] < 1.8 \times 10^{-4}$   
 $R = \frac{\sigma(e^+e^- \rightarrow \eta_b(1S)\omega)}{\sigma(e^+e^- \rightarrow Y(1S)\pi^+\pi^-)} < 2.2$
- $Y(10753)$  : PRD 109 (2024) 7, 072013  
 $\sigma(e^+e^- \rightarrow \eta_b(1S)\omega) < 2.5 \text{ pb}$   
 $R < 1.25$
- $Y(5S)$  : PRD 102 (2020) 9, 092011  
 $B[Y(5S) \rightarrow \eta_b(1S)\omega] < 1.3 \times 10^{-3}$   
 $B[Y(5S) \rightarrow \eta_b(2S)\omega] < 5.6 \times 10^{-3}$   
 $R < 0.25$

Does not support tetraquark?





# $Y(4S, 5S) \rightarrow Y(1S, 2S)\eta^{(\prime)}$

## ■ $Y(4S)$ :

$$B[Y(4S) \rightarrow Y(1S)\eta] = (1.70 \pm 0.23 \pm 0.08) \times 10^{-4}$$

$$B[Y(4S) \rightarrow Y(1S)\eta'] = (3.43 \pm 0.88 \pm 0.21) \times 10^{-5}$$

$$R_{\eta/\pi\pi} = 2.07 \pm 0.24 \text{ (1/}m_b\text{ suppression for pure } b\bar{b}\text{)}$$

$$R_{\eta'/\eta} = 0.20 \pm 0.06 \text{ (}\approx 5\text{ for pure } b\bar{b}\text{)}$$

## ■ $Y(5S)$ :

$$B[Y(5S) \rightarrow Y(1S)\eta] = (8.5 \pm 1.7) \times 10^{-4}$$

$$B[Y(5S) \rightarrow Y(1S)\eta'] < 6.9 \times 10^{-5}$$

$$R_{\eta/\pi\pi} = 0.19 \pm 0.04 \text{ (1/}m_b\text{ suppression for pure } b\bar{b}\text{)}$$

$$R_{\eta'/\eta} < 0.09 \text{ (}\approx 13\text{ for pure } b\bar{b}\text{)}$$

$$B[Y(5S) \rightarrow Y(2S)\eta] = (4.1 \pm 0.6) \times 10^{-4}$$

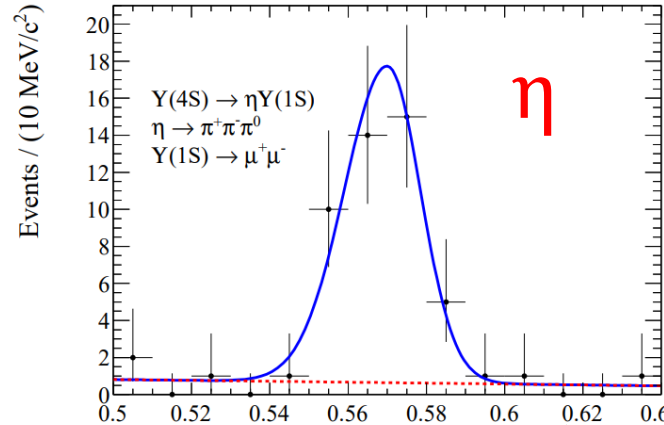
$$R_{\eta/\pi\pi}(2S) = 0.51 \pm 0.06 \text{ (1/}m_b\text{ suppression for pure } b\bar{b}\text{)}$$

Does not support pure  $b\bar{b}$

Could be explained by admixture of additional pair of light quarks

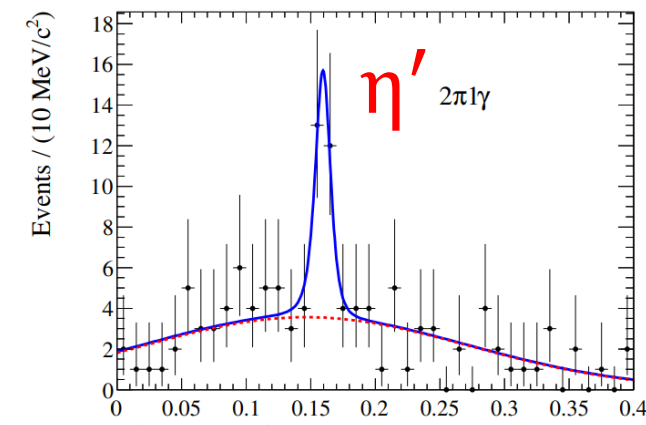
Or by B-meson loops

## Belle $Y(4S)$



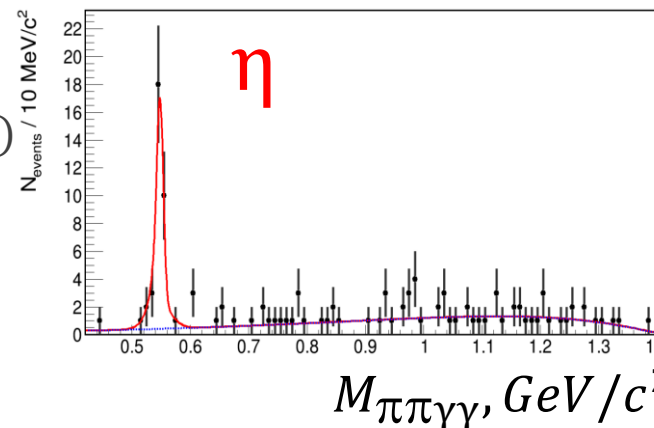
$$\Delta M_{\eta^{(\prime)}} = M(Y(4S)) - M(Y(1S)) - M(\eta^{(\prime)}), GeV/c^2$$

PRD 96 (2017) 5, 052005



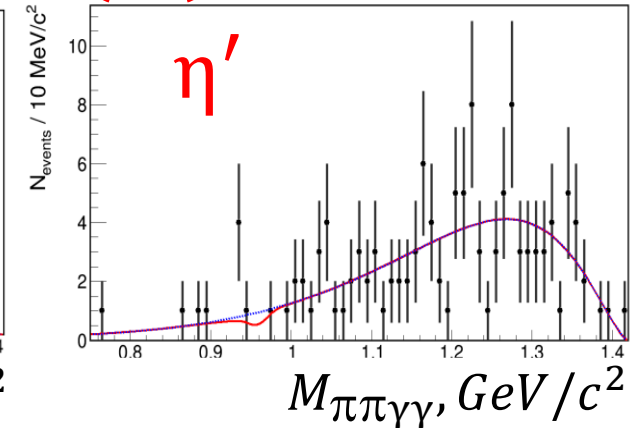
PRL 121 (2018) 6, 062001

## Belle $Y(5S)$



$M_{\pi\pi\pi\gamma\gamma}, GeV/c^2$

PRD 104 (2021) 11, 112006



$M_{\pi\pi\pi\gamma\gamma}, GeV/c^2$

# $h_b(1P, 2P) \rightarrow Y(1S)\eta(\pi^0)$

- Enhanced production in  $Y(5S) \rightarrow h_b(1P, 2P)\pi^+\pi^-$

$$\frac{\Gamma_{ann}[h_b(2P)]/\Gamma_{ann}[h_b(1P)]}{\Gamma_{ann}[\chi_{b1}(2P)]/\Gamma_{ann}[\chi_{b1}(1P)]} = 0.24^{+0.47}_{-0.24} \quad (1 \text{ is expected})$$

[arxiv:2407.03783](https://arxiv.org/abs/2407.03783)

- Contradiction gets stronger with expected

$$B(h_b(2P) \rightarrow Y(1S)\eta) \sim O(10\%) \quad \text{PRD 86 (2012) 094013}$$

- First evidence of  $h_b(2P) \rightarrow Y(1S)\eta$ :

$$B(h_b(2P) \rightarrow Y(1S)\eta) = (7.1^{+3.7}_{-3.2} \pm 0.8) \times 10^{-3}$$

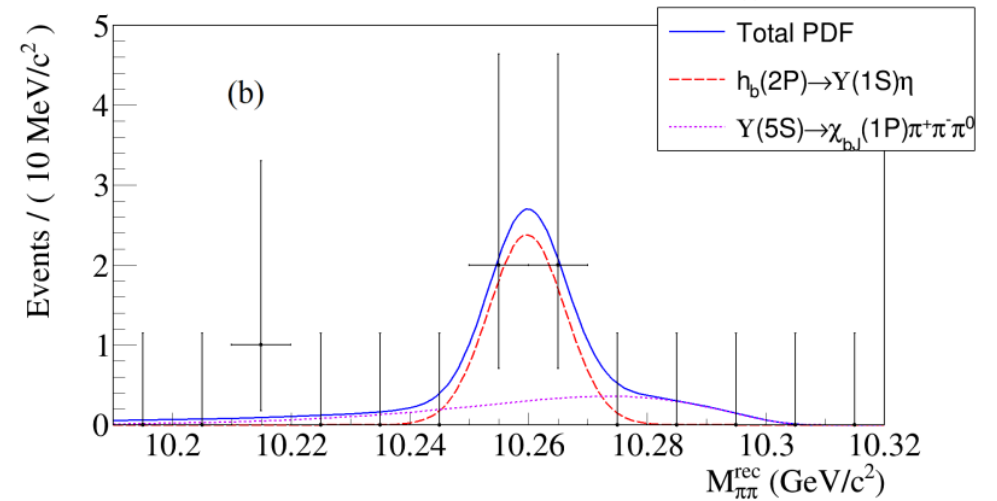
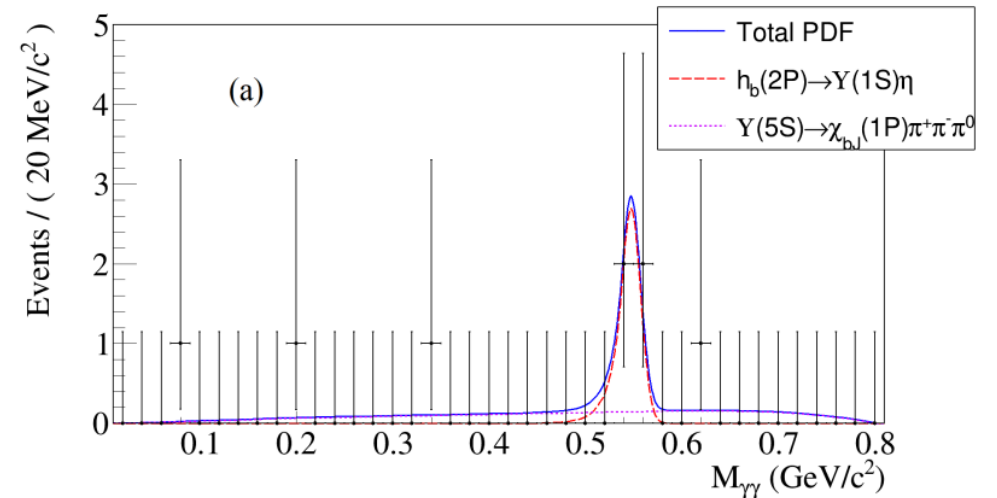
$$\frac{\Gamma[h_b(2P) \rightarrow Y(1S)\eta]}{\Gamma[Y(3S) \rightarrow h_b(1P)\pi^0]} = 30^{+20}_{-18} \pm 10 \quad (140 - 320 \text{ is expected})$$

[PRD 84 \(2011\) 091101](https://arxiv.org/abs/2407.03783)

- Also set upper limits:

$$B(h_b(1P) \rightarrow Y(1S)\pi^0) < 1.8 \times 10^{-3}$$

$$B(h_b(2P) \rightarrow Y(1S)\pi^0) < 1.8 \times 10^{-3}$$



[arxiv:2407.03783](https://arxiv.org/abs/2407.03783)

# Conclusion

- Hadronic transitions between bottomonium states provides important information on its structure
- There are signs that states  $Y(4S, 10753, 5S)$  above  $B\bar{B}$  threshold might not be pure conventional  $b\bar{b}$
- No clear explanation
- Additional efforts are required at this range of energies
  - $e^+e^- \rightarrow Y(1S)K^+K^-$
  - $e^+e^- \rightarrow Y(1S, 2S)\eta^{(\prime)}$
  - Additional data taking around  $Y(10753, 5S)$  energies

# BACKUP

$$Y(10753,5S) \rightarrow [Y(1S, 2S, 3S)/h_b(1P, 2P)]\pi^+\pi^-$$

