

Multilayer SND (Scattering & Neutrino Detector) optimization for statistical analysis of tau-neutrino events using detector response

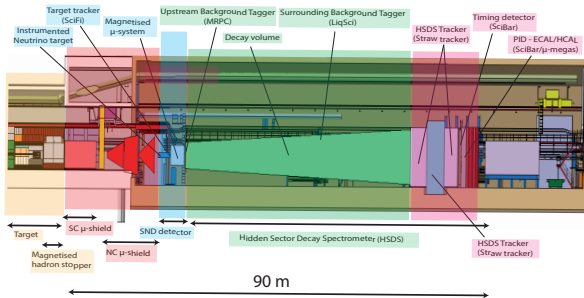
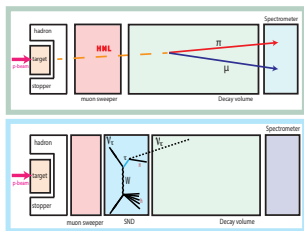
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23/10/2024

Search for Hidden Particles (SHiP)

- ▶ **SHiP** is a recently approved intensity-frontier experiment aiming to search for hidden particles with mass up to $O(10)$ GeV and extremely weak couplings, down to 10^{-10} .
- ▶ FIP decay search in background-free environment and LDM scattering
- ▶ Rich program at the Scattering & Neutrino Detector (SND): search for Light Dark Matter (LDM) & neutrino interaction physics with unique access to τ neutrino
 - ▶ Original Proposal (2013): Developed for new cavern ECN4
 - ▶ Refined Proposal (2023): Adaptation to existing ECN3 facility



SHiP experimental techniques: Decay & Scattering

Sensitivity is determined by three key factors:

- **Yields** (protons on target)
- **Acceptance** (including lifetime and angular acceptance)
- **Background level**

An exhaustive search require "model-independent" detector configuration, which should enable:

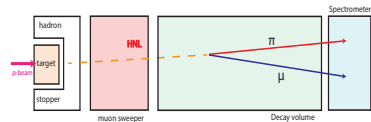
- Comprehensive reconstruction and identification of both fully and partially reconstructible modes
- Sensitivity to partially reconstructed modes
 - Distinguish between different models.
 - Assess the compatibility of the observed signal with theoretical predictions.

► 4×10^{19} protons on target per year currently available in the SPS

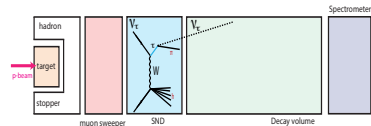
- $\sim 2 \times 10^{17}$ charmed hadrons (> 10 times the yield at HL-LHC)
- $\sim 2 \times 10^{12}$ beauty hadrons
- $\sim 2 \times 10^{15}$ tau leptons
- $\mathcal{O}(10^{20})$ photons above 100 MeV
- 3500 $\nu_\tau + \bar{\nu}_\tau$ per year, and $2 \times 10^5 \nu_e + \bar{\nu}_e / 7 \times 10^5 \nu_\mu + \bar{\nu}_\mu$ regardless of target design

Physics model	Final state
SUSY neutralino	$\ell^\pm \pi^\mp, \ell^\pm K^\mp, \ell^\pm \rho^\mp, \ell^+ \ell^- \nu$
Dark photons	$\ell^+ \ell^-, 2\pi, 3\pi, 4\pi, KK, q\bar{q}, D\bar{D}$
Dark scalars	$\ell\ell, \pi\pi, KK, q\bar{q}, D\bar{D}, GG$
ALP (fermion coupling)	$\ell^+ \ell^-, 3\pi, \eta\pi\pi, q\bar{q}$
HSDS ALP (gluon coupling)	$\pi\pi\gamma, 3\pi, \eta\pi\pi, \gamma\gamma$
HNL	$\ell^+ \ell^- \nu, \pi l, \rho l, \pi^0 \nu, q\bar{q}' l$
Axino	$\ell^+ \ell^- \nu$
ALP (photon coupling)	$\gamma\gamma$
SUSY sgoldstino	$\gamma\gamma, \ell^+ \ell^-, 2\pi, 2K$
LDM	electron, proton, hadronic shower
SND	τ^\pm
Neutrino-induced charm production (ν_e, ν_μ, ν_τ)	$D_s^\pm, D^\pm, D^0, \bar{D}^0, \Lambda_c^+, \bar{\Lambda}_c^-$

Visible decay to SM particles

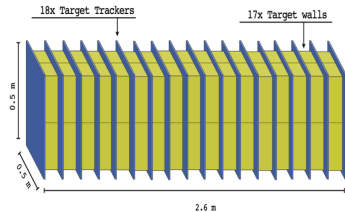
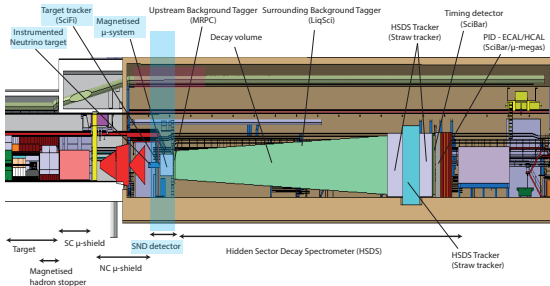
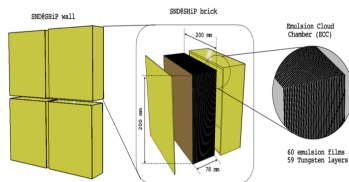


Scattering off atomic electrons and nuclei



Scattering & Neutrino Detector (SND)

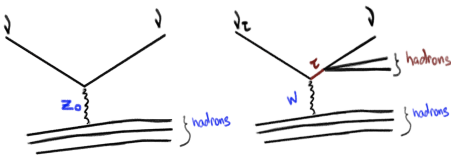
- ▶ Original design based on **nuclear emulsions**: DONuT / OPERA / **SND@LHC**
- ▶ Emulsion Cloud Chamber (ECC) bricks
- ▶ Target Tracker (TT): 18 layers of SciFi
- ▶ μ spectrometer: Drift tubes (4 stations)
 - ▶ Air core dipole magnet: 1 T



The task

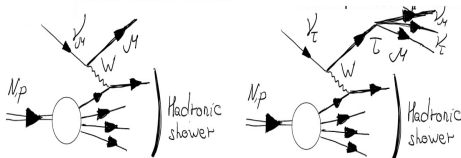
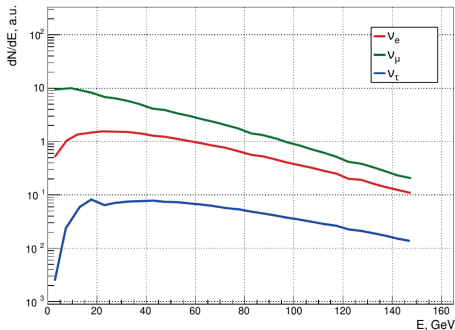
► We need to classify the two signals from these processes:

- **NCDIS** $\nu_\mu \rightarrow \text{hadrons}$
- **CCDIS** $\nu_\mu \rightarrow \mu + \text{hadrons}$
- **CCDIS** $\nu_\tau \rightarrow \tau + \text{hadrons}$
(hadronic & leptonic τ decay modes)



Neutrino spectra were taken from the SHiP experiment and used as a GENIE input. Detector response was performed using Geant4.

SHiP ν_e, ν_μ, ν_τ



Detector concept

► Absorber:

- Material: Fe (5 cm, 2 cm)
- Magnetic field: 1.7 Tesla along the y-axis

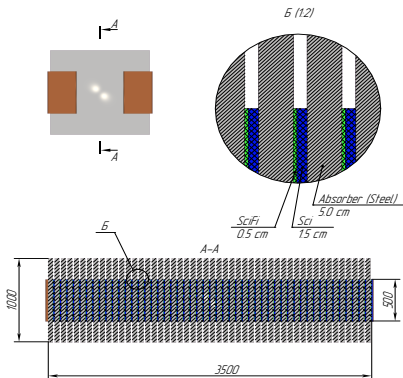
► Tracker:

- Fibres: \varnothing 250 μ m SciFi

► Scintillator:

- Endep Scint layers

1 (3) cm \times 1 (3) cm \times 1.5 cm
(xyz) (Poly)

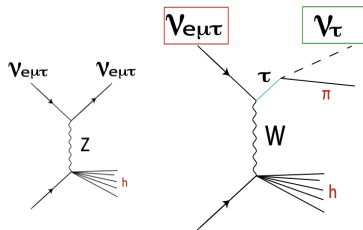
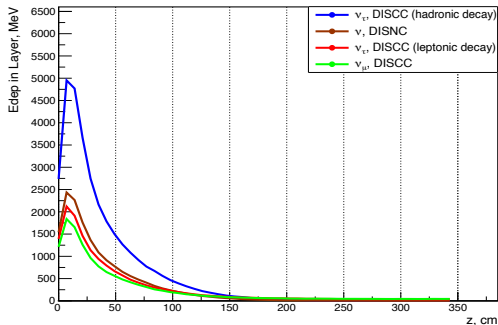


#	Name	Quantity
1	Magnetic absorber (GO Steel)	50
2	Sci	50
3	SciFi	50
4	Current Coil	2

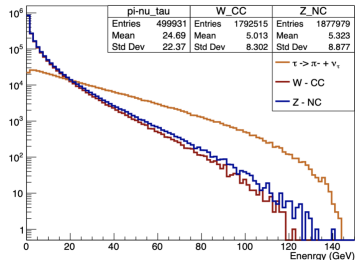
Longitudinal shower profile for CCDIS ν_τ & NCDIS ν_μ

- ▶ **Charged current (hadronic decay):**
 - ▶ Hadrons from τ decay are more energetic.
- ▶ **Neutral current and charged current (leptonic decay):**
 - ▶ Hadrons initiated by Z slightly energetic than hadrons from W .

Energy deposit, 50 layers: Absorber(Fe, 5. cm) x SciFi(Poly, 0.5 cm) x Sci(Poly, 1.5 cm)

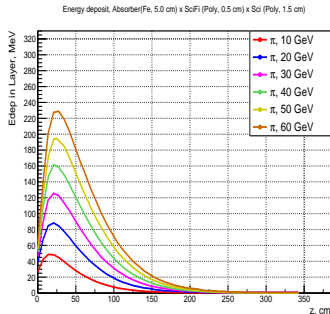
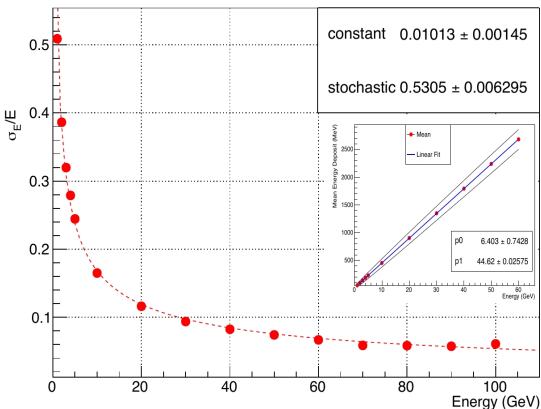


Charged hadron energy



Energy resolution

- ▶ **Incoming particles:** π , e
- ▶ **Particles momentum range:** **1-100 GeV/c**

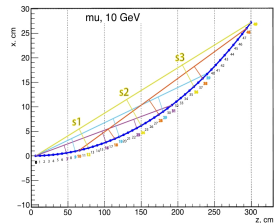
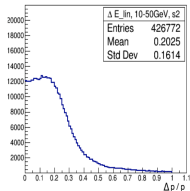
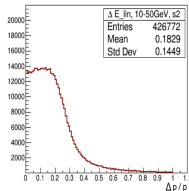
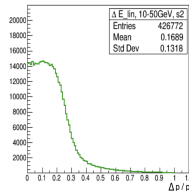


- ▶ for electrons: $\frac{\sigma_E}{E} \sim \frac{33\%}{\sqrt{E}}$
- ▶ for pions : $\frac{\sigma_E}{E} \sim \frac{53\%}{\sqrt{E}}$

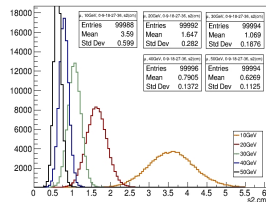
Energy deposit collected in Scint layers

Particle (muon) momentum reconstruction

- ▶ We determine **sagitta** to use the dependences of these parameters on the kinetic energy of the muon
- ▶ The trajectory parameters, **S1, S2, S3** are calculated as "distances from a point to a line"
- ▶ If the functions $p = f(s)$ for a limited range of **10-30 GeV** are used, the most accurate determination of the muon momentum of $\sim 12\%$ is obtained
- ▶ If the functions $p = f(s)$ for **10-50 GeV** are used, a determination of the muon momentum with an accuracy of $\sim 14-15\%$ is obtained


 $\Delta p/p$ s2, in2, 10-50GeV, 0-2-4-6-8

 $\Delta p/p$ s2, in2, 10-50GeV, 0-3-6-9-12

 $\Delta p/p$ s2, in2, 10-50GeV, 0-4-8-12-16


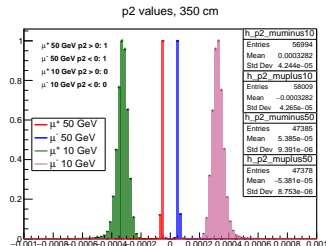
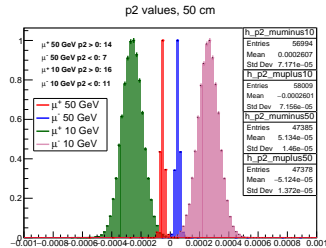
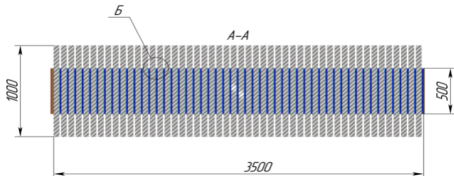
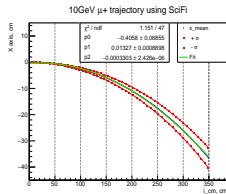
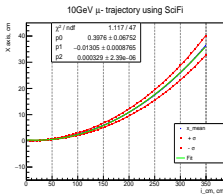
0-9-18-27-36, s2, 10, 20, 30, 40, 50GeV



Particle (muon) charge reconstruction

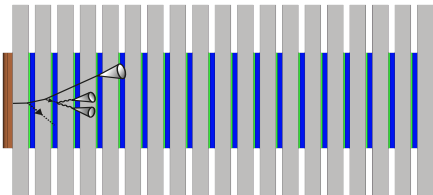
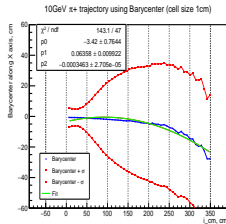
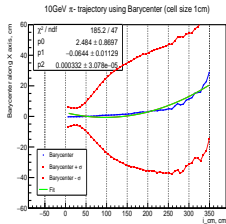
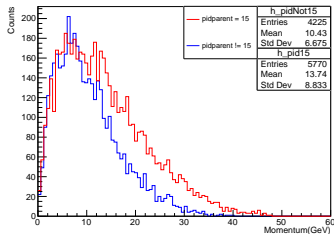
- Determine charge: the sign of the fitted **parabolic coefficient p2** to decide whether the muon is

- μ^+ : $p_2 < 0$
- μ^- : $p_2 > 0$

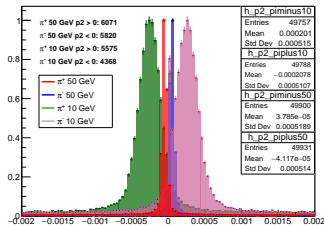


Particle (pion) momentum reconstruction

- ▶ Based on the **fastest hadron track charge**, determine whether the tau neutrino is ν_τ or $\bar{\nu}_\tau$
- ▶ Momentum reconstruction for **hadrons** using SciFi information in process
- ▶ Trajectory for **hadrons** using only Scint layers information

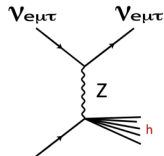
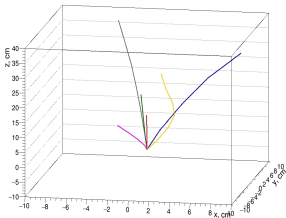
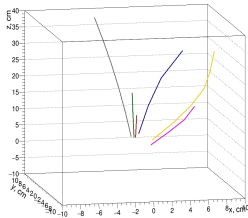
Fastest Hadrons from 50 GeV ν_τ 

p2 values, 25 cm

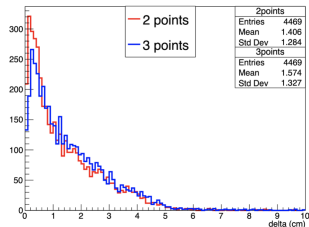


Neutrino vertex reconstruction

- ▶ **To reconstruct the vertex**, we extrapolate our tracks by a linear function
- ▶ Each track segment is crossed in pairs, then the average sum of the distance to the center of the segment that connects the crossed lines is taken
- ▶ In the actual configuration of the detector there is **no zero point**, there are only track points starting from **$z=5\text{cm}$**

SHiP, ν_e NC hadron cluster tracksSHiP, ν_e NC hadron cluster tracks

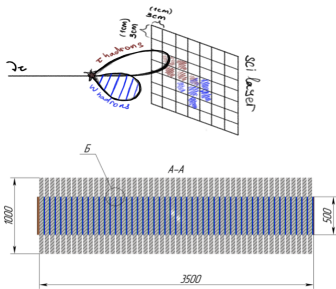
Accuracy of neutrino vertex reconstruction (DISNC)



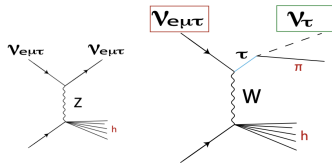
Conclusion: vertex reconstruction accuracy using SciFi layers $\sim 0.1\text{ cm}$

CCDIS ν_τ (hadronic decay) & NCDIS ν_μ

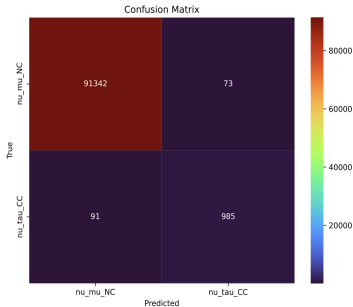
- ▶ **16 Scint layers** (out of 50 layers)
 - ▶ Energy deposition
 - ▶ Energy of hadron cluster
 - ▶ Shower CoG in XY plane
 - ▶ Shower width in XY plane
- ▶ **in total: 81 parameter**



Parameters describing close parts (layers) of the detector are correlated

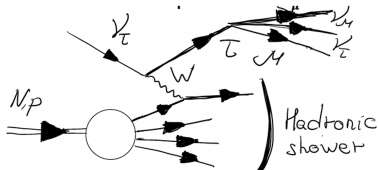
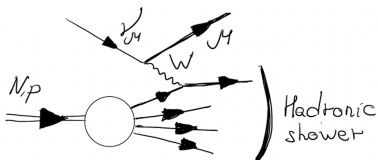


The less diagonal the matrix, the better the classification



CCDIS ν_τ (leptonic decay) & CCDIS ν_μ

Reasonable cuts on the data



- ▶ Non-trivial problem due to:
 - ▶ High-imbalance of the classes (300:1);
 - ▶ overlapping feature distributions.
- ▶ The cut on the angle btw P_μ and P_{hadr} should be applied:

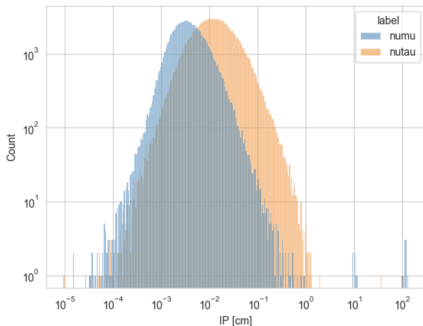
$$\alpha < \arctan \frac{\text{Det. transverse length} / 2}{\text{Det. longitudinal length} / 2} \simeq 10 \text{ degr.} \quad \text{— rejects 70\% of the data}$$

- ▶ removing low-energy nucleons from the nucleus fragmentation: fully absorbed in the passive material
- ▶ In case of using Impact parameter (IP) of muons w.r.t. to the interaction point:
 - ▶ $IP > 0.1 \text{ cm}$ (resolution is 0.1 cm) & $IP < 0.6 \text{ cm}$ (remove outliers)

Impact parameter (IP) of muons w.r.t. to the interaction point

- ▶ Multiple scattering of muon/tau also contributes into IP.
- ▶ Resolution of the vertex reconstruction is not sufficient to use IP as a parameter in the classification.

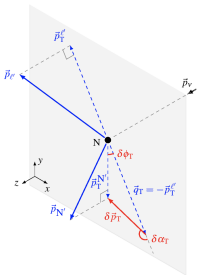
- ▶ Simulation (5 cm of the passive material). Extrapolation of first 3 points back to the $z = 0$ cm.



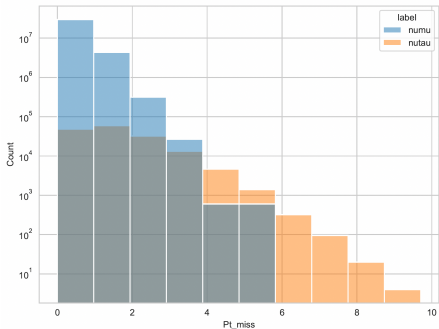
$$IP_{\max}^{\text{nutau}} - IP_{\max}^{\text{numu}} \simeq 0.007 \text{ cm}$$

Crucial parameter

- Difference in missing transverse momentum distribution is mostly caused by the neutrinos that carried away momentum.



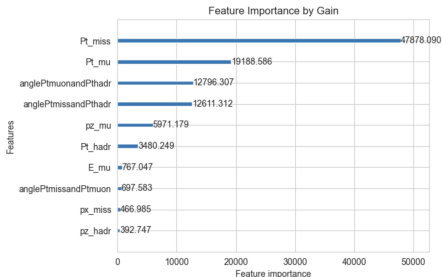
Cut on the missing P_T is possible but rejects most of the nutau events as well → BDT.



<https://arxiv.org/pdf/1512.05748>

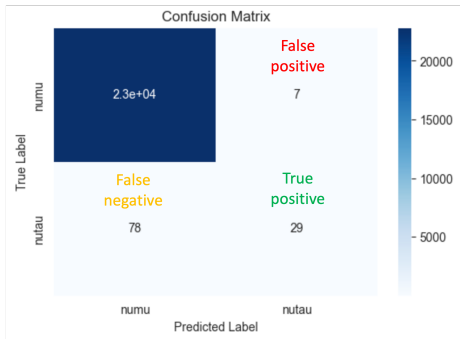
Classification setup of BDT classifier (Lightgbm based)

- ▶ Training on 80%, validation on 20% of the data.
- ▶ Data is weighted to consider the imbalance of the dataset ($w = 1./300$ weights for nutau events instead of $w = 300$. for numu).
- ▶ 18 kinematic parameters used as features (momenta and energies of muons and hadronic showers, and angles btw momenta in the transverse plane).
- ▶ Muon momenta and hadronic shower energies are smeared according to the detector resolution.
- ▶ Optimization of hyperparameters of BDT using Optuna.



Results. Confusion matrix

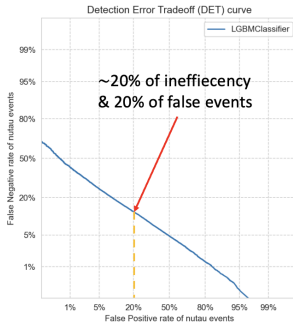
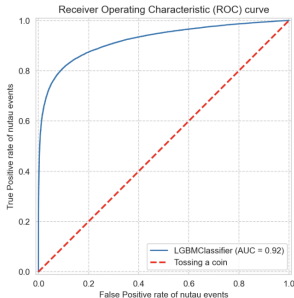
- ▶ Confusion matrix **does not show the performance of the classifier for different discriminator threshold** which is crucial for highly-imbalanced problem.
- ▶ Maximising **True positive (TP)** value.
- ▶ **False negative (FN)** value shows the inefficiency of the classifier (how many nutau were classified incorrectly). Not dangerous for searching for nutau signal.
- ▶ **False positive (FP)** value shows the number of incorrectly classified numu events. Dangerous for searching for nutau signal.



Random test data sampling:
 $TP/(FP + TP) = [0.69, 0.94]$ in 95% CI.

Results. ROC-AUC and DET curves

- ▶ Varying the discriminator threshold from 0 to 1, one can choose the classifier with the required performance.
- ▶ ROC-AUC — tradeoff btw. **TP** and **FP**, DET — tradeoff btw. **FN** (inefficiency) and **FP**.
- ▶ Example: discriminator threshold is chosen with 20% of inefficiency and 20% of false events.

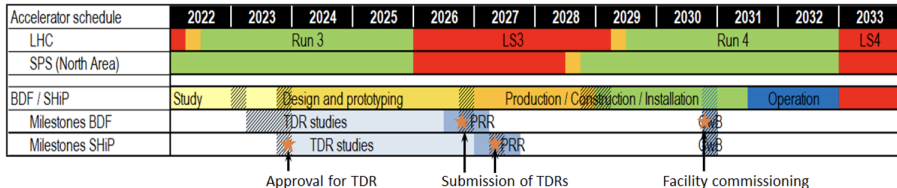


Thank you!

vasilisa.guliaeva@cern.ch

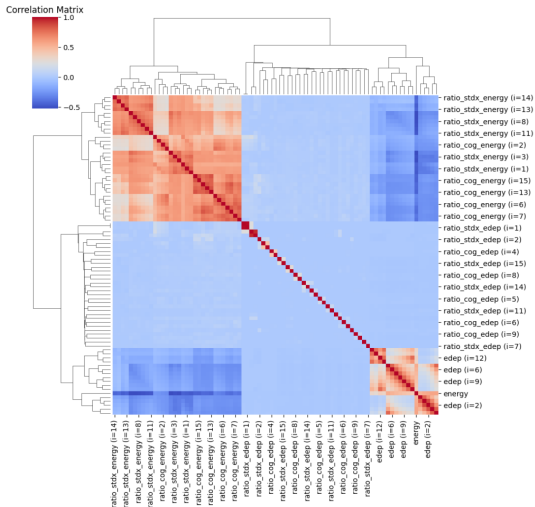
BDF/SHiP preliminary schedule

- ▶ Availability of test beams challenging
- ▶ Important to start data taking > 1 year before **LS4**



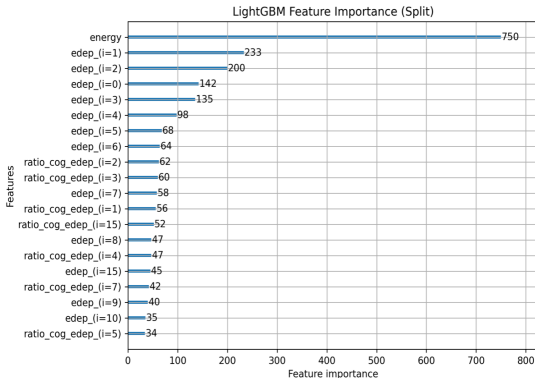
CCDIS ν_τ (hadronic decay) & NCDIS ν_μ

- ▶ **16 Scint layers** (out of 50 layers)
 - ▶ Energy deposition
 - ▶ Energy of hadron cluster
 - ▶ Shower CoG in XY plane
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- ▶ **in total: 81 parameter**

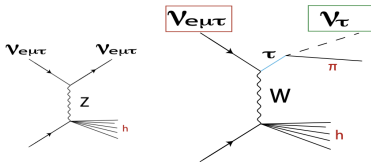
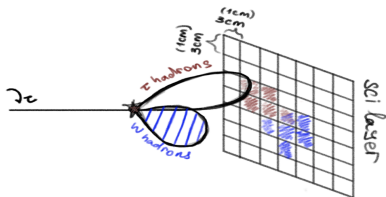


CCDIS ν_τ (hadronic decay) & NCDIS ν_μ

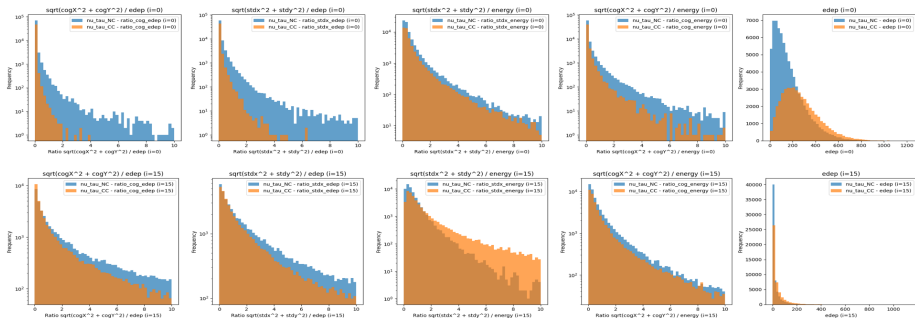
- ▶ Most valuable: energy of hadron cluster, energy deposit in layers;
- ▶ Split measures how often a feature is used to split the data in decision trees during training, which helps assess the feature's importance in making decisions.



CCDIS ν_τ (hadronic decay) & NCDIS ν_μ



► Parameters (example):



Impact parameter (IP) of muons w.r.t. to the interaction point

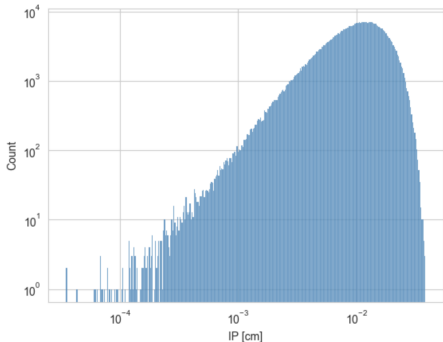
- ▶ The difference btw 2 cases is the path before the decay of tau in the nutau case. IP should be larger in this case:

$$IP = c\gamma\tau \sin(\theta) =$$

$$c\tau \frac{E_\tau}{m_\tau} \sqrt{1 - (p_{\tau,z}/P_\tau)^2}$$

- ▶ Multiple scattering of muon/tau also contributes into IP.

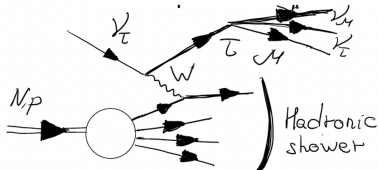
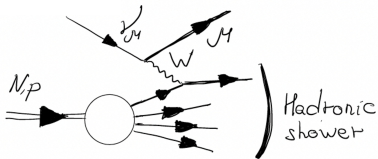
- ▶ Theory. Calculate the contribution into IP of muon due to the tau decay for nutau case for (E_τ, θ_τ) in SHiP case.



$$IP_{\max}^\tau \sim 10^{-2} \text{ cm}$$

CCDIS ν_τ (leptonic decay) & CCDIS ν_μ

- ▶ Non-trivial problem due to:
 - ▶ High-imbalanceness of the classes (300:1);
 - ▶ overlapping feature distributions.



Results. ROC-AUC and DET curves

- ▶ Varying the discriminator threshold from 0 to 1, one can choose the classifier with the required performance.
- ▶ ROC-AUC — tradeoff btw. **TP** and **FP**, DET — tradeoff btw. **FN** (inefficiency) and **FP**.
- ▶ Metrics:
 - ▶ **True positive rate** = $\frac{TP}{\text{Actual positive}}$ ← Maximising
 - ▶ **False positive rate** = $\frac{FP}{\text{Actual negative}}$ ← Dangerous
 - ▶ **False negative rate** = $\frac{FN}{\text{Actual positive}}$ ← Not dangerous

