

Analysis of Λ -hyperon production in carbon-nucleus run



Speaker: Ksenia Alishina

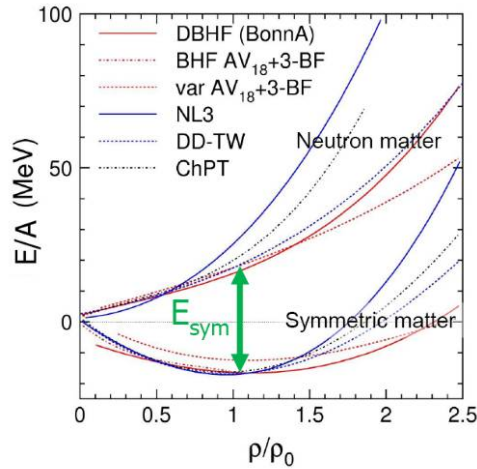
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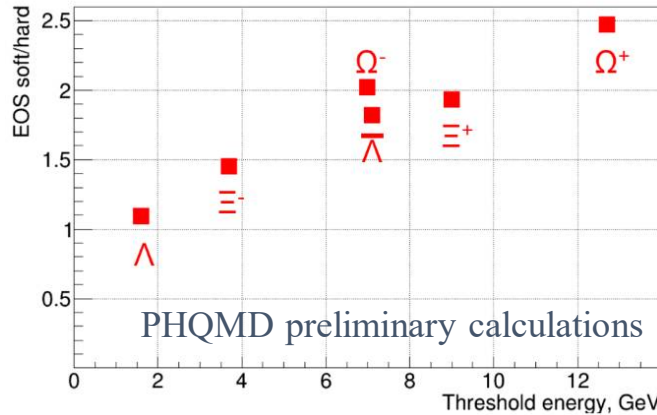
25.10.2024

Physical motivation BM@N experiment

Ch.Fuchs, EPJA 30 (2006) 5

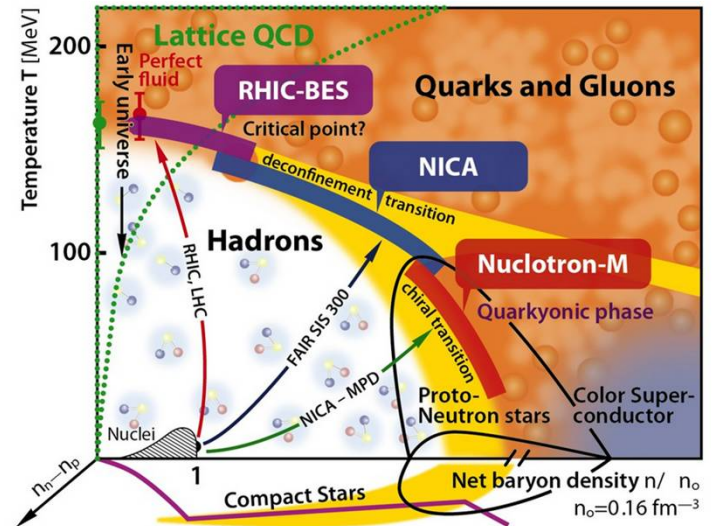
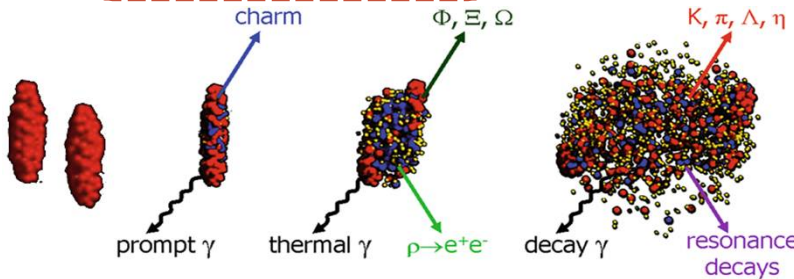
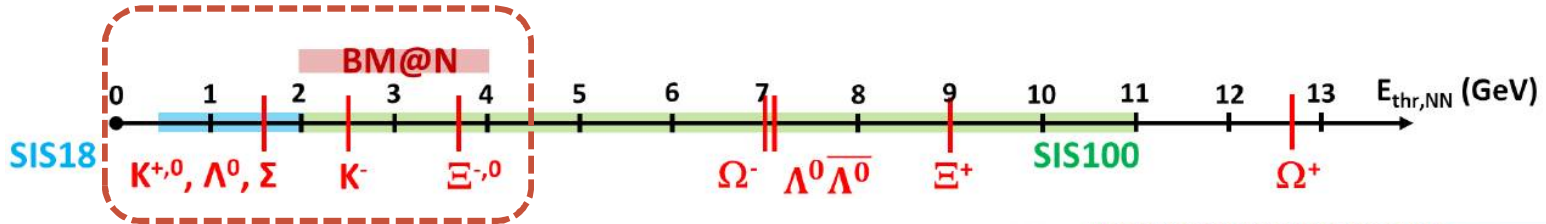


Hyperon yield in 4A GeV Au+Au:
soft EOS (K=240 MeV) / hard EOS (K=350) MeV



EoS study for symmetric matter at $\rho/\rho_0 = 3 - 5$, $\rho_0 = 0.16\text{fm}^{-3}$:

- Elliptical flow of protons, mesons and hyperons;
- Sub-threshold production of strange mesons and hyperons extract nuclear;
- Incompressibility (K_{mn}) from the modeled data;



EoS: The relation between density, pressure, temperature, energy and isospin asymmetry:

$$E_A(\rho, \delta) = E_A(\rho, 0) + E_A(\rho) \delta^2$$

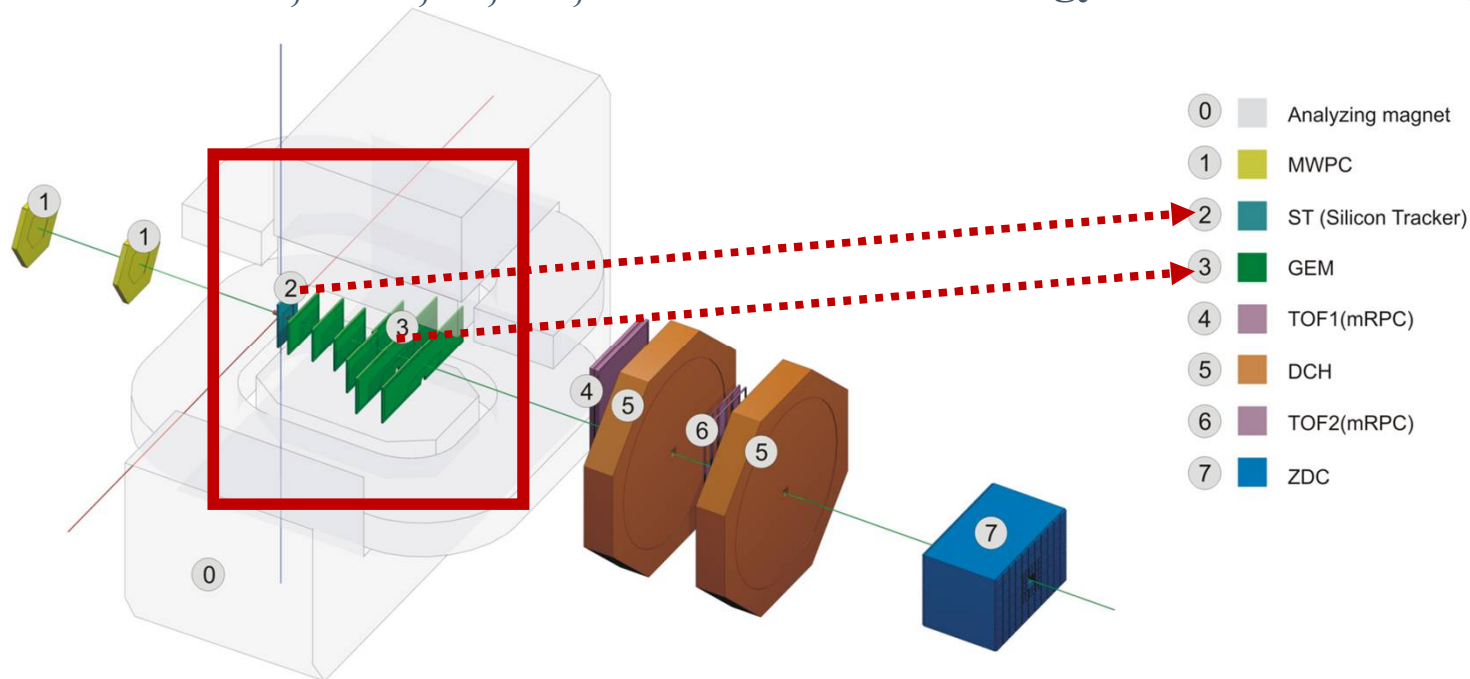
$$\delta = (\rho_n - \rho_p) / \rho$$

Incompressibility of the nucleus: $K_{mn} = 9\rho^2 \frac{\partial^2}{\partial \rho^2} (E/A)|_{\rho=\rho_0}$

Setup scheme

$C + A \rightarrow X$, $A: C, Al, Cu, Pb$

Energy beam = 4.0 AGeV, 4.5 AGeV



Central tracker:

- One plane of a forward Si detector;
- 6 GEM stations:
 - o 5 GEM detectors ($66 \times 41 \text{ cm}^2$);
 - o 2 GEM detectors ($163 \times 45 \text{ cm}^2$);

Gas Electron Multiplier (GEM) system:

To measure momenta of a charged particle;

Event reconstruction in GEM in C+A interaction;

Triggers: BD, BC₁, BC₂, T₀, VETO

Trigger efficiency

The trigger efficiency was evaluated by a convolution of the **GEANT simulation** of the barrel detector response to DCM-QGSM events with reconstructed Λ hyperons and the GEANT simulation of delta electrons.

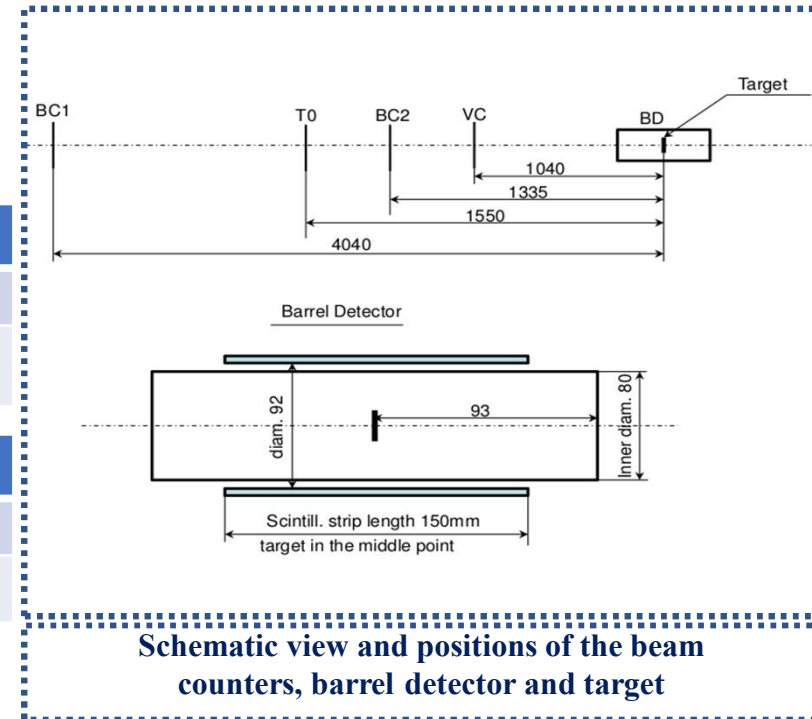
$$\epsilon_{trig} = N_{sim_{\Lambda}}(BD \geq n) / N_{sim_{all\Lambda}}$$

The **systematic errors** in **Table 1** cover:

- 1) Contribution of delta electrons;
- 2) The spread of the trigger efficiencies calculated for different y and p_T bins of the reconstructed Λ -hyperons;
- 3) Change in the trigger efficiency after correction of the simulated track multiplicity in agreement with the experimental data.

Table 1. Trigger efficiency ϵ_{trig}

4 AGeV	C	Al	Cu	Pb
$\epsilon_{trig}(BD \geq 2)$	0.80 ± 0.02	-	-	-
$\epsilon_{trig}(BD \geq 3)$	-	0.87 ± 0.02	0.92 ± 0.02	0.95 ± 0.02
4.5 AGeV	C	Al	Cu	Pb
$\epsilon_{trig}(BD \geq 2)$	0.80 ± 0.02	-	-	-
$\epsilon_{trig}(BD \geq 3)$	-	0.83 ± 0.02	0.91 ± 0.02	0.94 ± 0.02

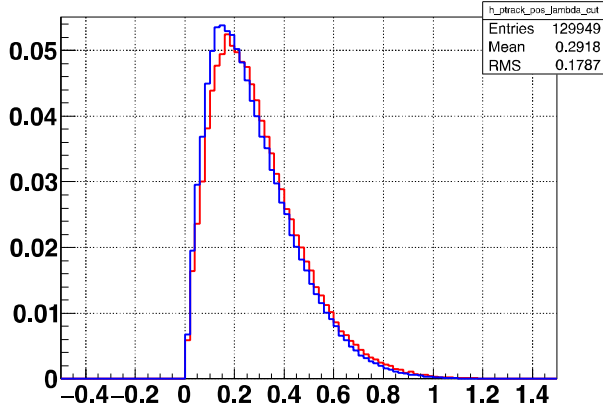


ϵ_{trig} is used for evaluation of production cross section;

Data and Monte - Carlo comparison

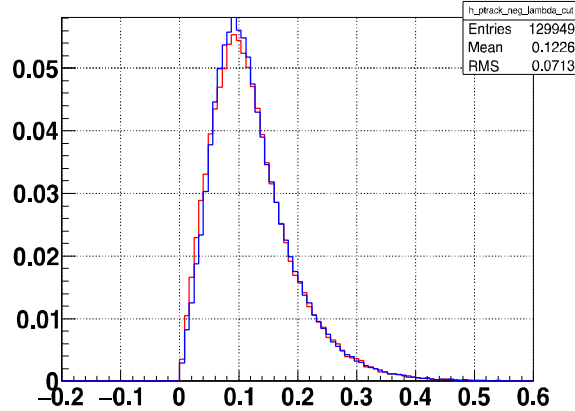
C+Cu interactions at **4.0 AGeV** beam energy

h_ptrack_pos_lambda_cut



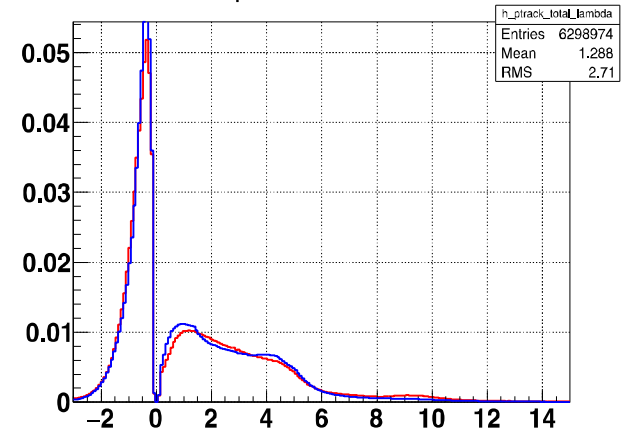
transverse momentum of positive particles ($p_T > 0$, GeV/c)

h_ptrack_neg_lambda_cut



transverse momentum of negative particles ($p_T < 0$, GeV/c)

h_ptrack_total_lambda



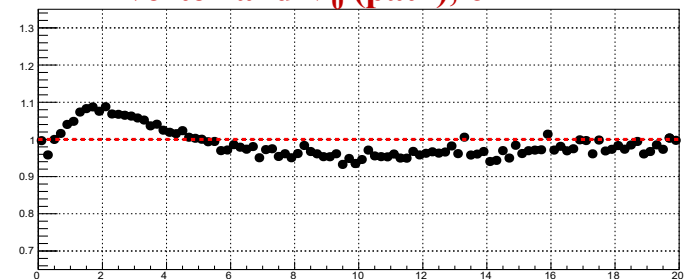
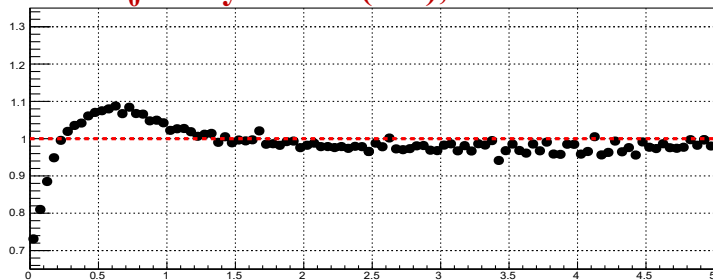
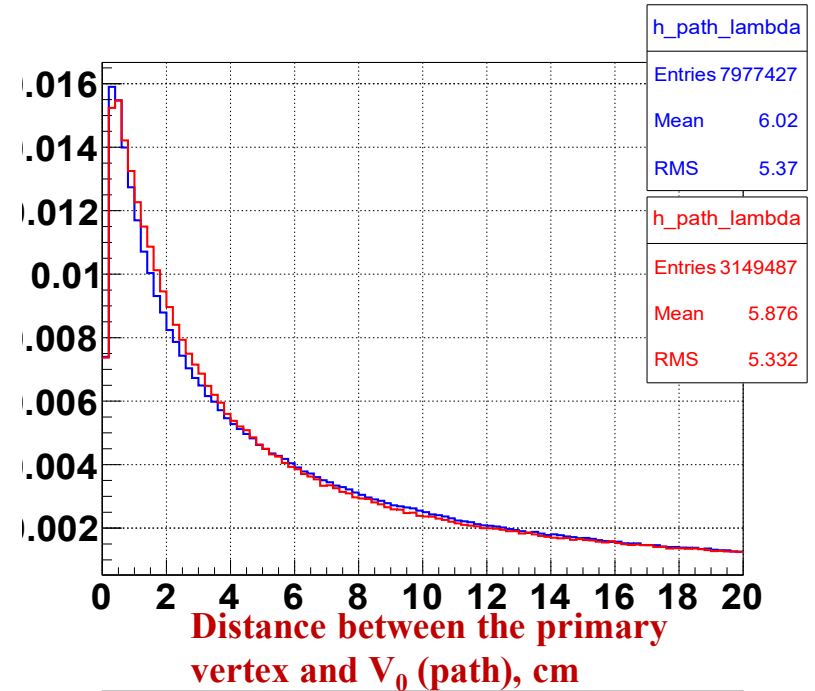
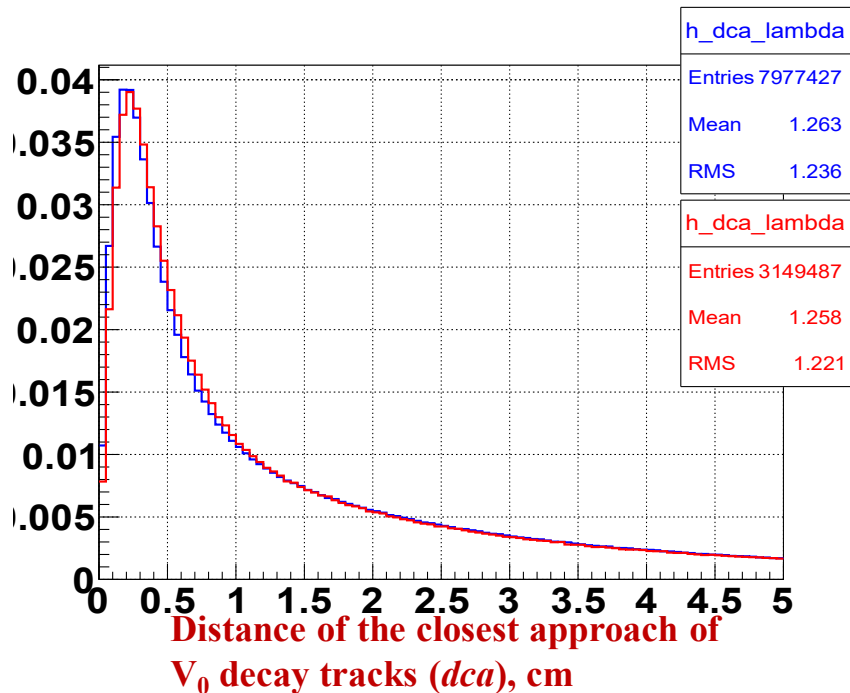
total momentum of negative and positive particles, GeV/c

Blue line - MC, **red line** - data.

Data and Monte-Carlo comparison

Reaction $C+Cu$, energy **4.0** AGeV

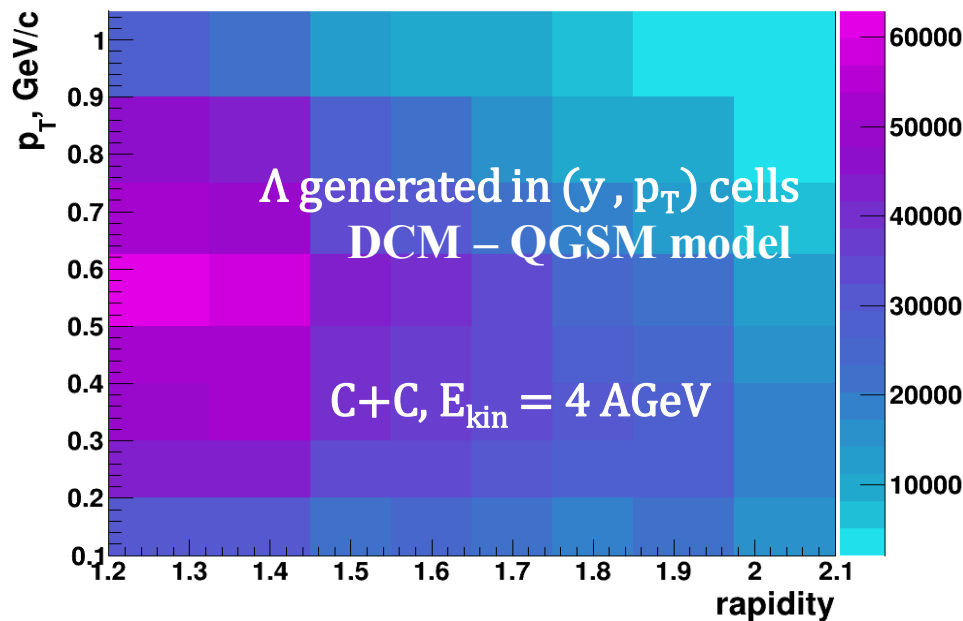
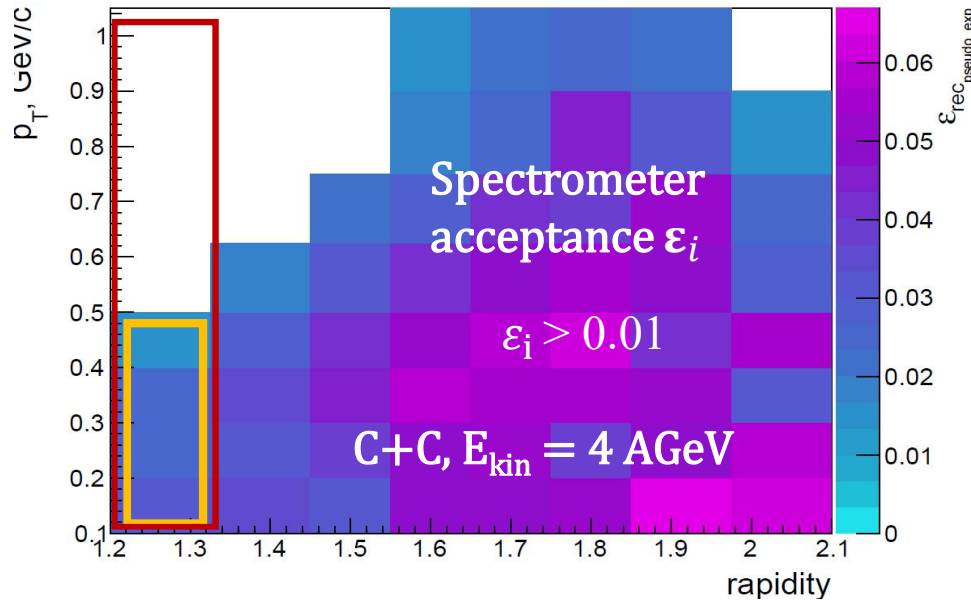
Cuts were applied as follow: $dca < 1.0$, $path > 2.5$



Physical analysis steps

- 1 The experiment accumulated data, but the statistics from the reconstructed selected Λ candidates are not very rich ($N_{\text{DATA}} \sim 5.9 \times 10^5$).
- 2 The high statistic MC data set was generated: ($N_{\text{MC}} \sim 3.8 \times 10^7$). MC were tuned to data and acceptance was evaluated in (y, p_T) cells with good precision.
- 3 Each event was weighted with the acceptance for each cell.
- 4 1D distributions in y or p_T were evaluated as the projections of 2D distributions to the corresponding kinematic variable.

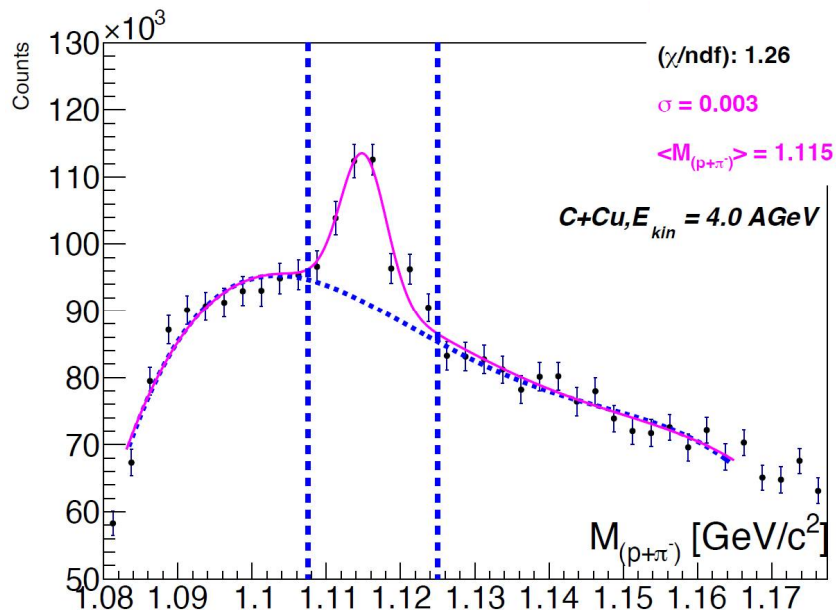
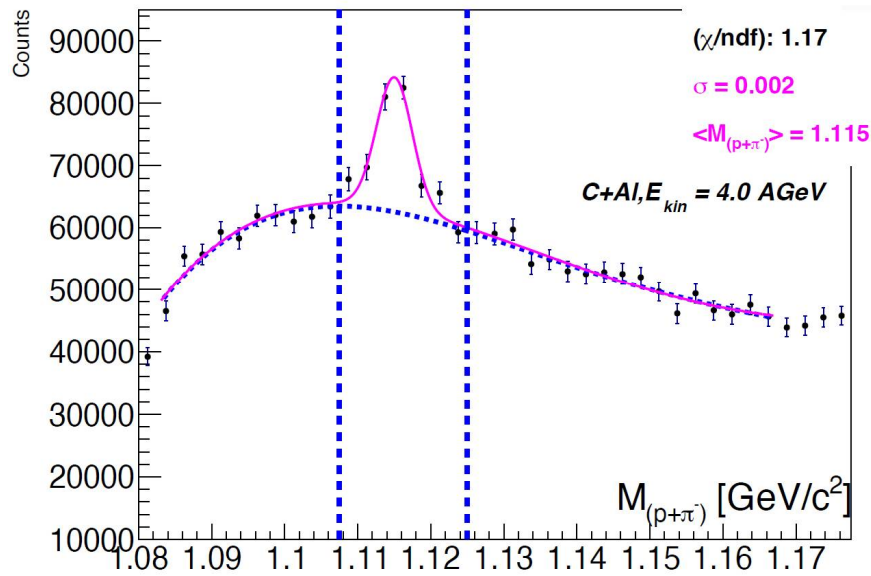
Extrapolation to low acceptance (y, p_T) cells



Extrapolation steps:

- 1 Extrapolation based on the DCM – QGSM model;
- 2 Extrapolation factor is calculated $f_{extr} = N_{all}/N_{con}$, N_{all} – sum of all generated events; N_{con} – sum of generated events in cells with high acceptance;
- 3 f_{extr} - is used for evaluation of production cross section in full kinematic range;

Mass distribution of the Λ (BM@N DATA)



Procedure in DATA $C+A \rightarrow X$

- 1) Split (y, p_T) area in small cells for MC/DATA (8x8);
- 2) **To each event assigned the weight ϵ_i** ;
- 3) Sum the cells by $\sum_{ij} y_{ij}$ and by $\sum_{ij} pT_{ij}$

$0.1 < p_T < 1.05$
and
 $1.2 < y_{lab} < 2.1$

- Λ signal width $\sim 2.0 - 4 \text{ MeV}$;
- **Signal** = hist – Background in **1107.5 - 1125 MeV/c^2** ;

The suppression factors

- The suppression factors of reconstructed events ϵ_{pileup} due to selection **criteria** applied to eliminate beam halo and pile-up events in interactions of the 4.0 and 4.5 AGeV carbon beam with the C, Al, Cu, Pb targets.

Table 2. ϵ_{pileup} suppression factors

Selection	4 AGeV	4.5 AGeV
T0==1	+	+
BC2==1	+	+
Veto==0	+	+
C	0.674±0.034	0.529±0.026
Al	0.740±0.037	0.618±0.031
Cu	0.779±0.039	0.621±0.031
Pb	0.784±0.039	0.686±0.034

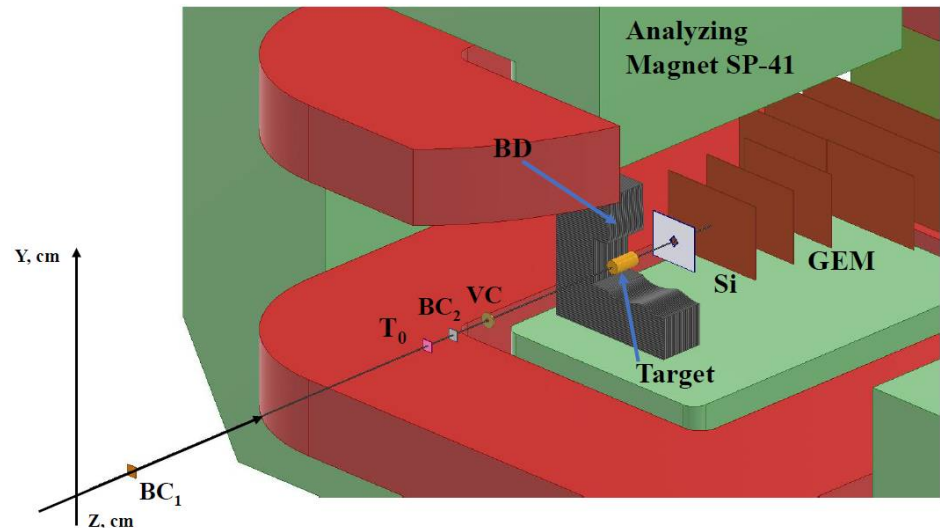
- ϵ_{pileup} is used for evaluation of production cross section;

Number of signals in the start detector: $T_0=1$

Preliminary systematics evaluation:

$$\delta\epsilon_{pileupsys} = \epsilon_{pileup} \cdot \delta\epsilon_{pileup};$$

where $\delta\epsilon_{pileup} = 5\%$



Cross sections $\sigma_{\Lambda}(y/p_T)$ of the Λ

The inclusive cross section σ_{Λ} of Λ hyperon in C+A interactions are calculated in bins of (y, p_T) according to the formula:

$$\sigma_{\Lambda}(p_T) = \frac{[\sum_y N_{rec}^{\Lambda}(y, p_T) / \epsilon_{rec}(y, p_T)]}{[\epsilon_{trig} \cdot \epsilon_{pileup} \cdot L]}$$

$$\sigma_{\Lambda}(y) = \frac{[\sum_{p_T} N_{rec}^{\Lambda}(y, p_T) / \epsilon_{rec}(y, p_T)]}{[\epsilon_{trig} \cdot \epsilon_{pileup} \cdot L]}$$

weighted signal

L is the luminosity, N_{rec}^{Λ} is the number of reconstructed Λ -hyperons,
 ϵ_{rec} is the combined efficiency of the Λ - hyperon reconstruction,
 ϵ_{trig} is the trigger efficiency, ϵ_{pileup} is the suppression factors of reconstructed events.

Table 3. Integrated **luminosities** collected in interactions of the carbon beam of 4.0 and 4.5 AGeV with different targets.

Interactions, target thickness		Integrated luminosity/ 10^{30} cm^{-2}		Integrated luminosity/ 10^{30} cm^{-2}
C+C (9 mm)	4 AGeV	6.06	4.5 AGeV	4.69
C+Al (12 mm)		2.39		3.60
C+Cu (5 mm)		2.00		3.06
C+Pb (10 mm)		0.22		0.84

Yields of the Λ

The Y_Λ of Λ hyperon in C+A interactions are calculated in bins of (y, p_T) cells according to the formula:

$$Y_\Lambda(y, p_T) = \sigma_\Lambda(y, p_T) / \sigma_{inel}$$

σ_{inel} is the cross section for minimum bias inelastic C+A interactions(model).

The cross sections for inelastic C+Al, C+Cu, C+Pb interactions calculated by the formula (DCM-QGSM):

$$\sigma_{inel} = \pi R_0^2 (A_P^{1/3} + A_T^{1/3})^2$$

$R_0 = 1.2$ fm is an effective nucleon radius, A_P and A_T are atomic numbers of the beam and target nucleus [1]. The **uncertainties** for C+Al, C+Cu, C+Pb inelastic cross sections are estimated by formula: $\sigma_{inel} = \pi R_0^2 (A_P^{1/3} + A_T^{1/3} - b)^2$ with $R_0 = 1.46$ fm and $b = 1.21$ [2].

Table 4. Inelastic cross sections σ_{inel} for carbon-nucleus interactions

Interaction	C+C	C+Al	C+Cu	C+Pb
Inelastic cross section, mb	830±50	1260±50	1790±50	3075±50

[1] Kalliopi Kanaki “Study of Λ hyperon production in C+C collisions at 2 AGeV beam energy with the HADES spectrometer”.

[2] H. Angelov et al., P1-80-473, JINR, Dubna.

1
$$\Delta Y_{\Lambda_{sys_signal_var}}^2 = Y_{\Lambda}^2 (\sigma_{N_{recDATA}^{\Lambda}}^2 / \langle N_{recDATA}^{\Lambda} \rangle^2 + \sigma_{N_{recMC}^{\Lambda}}^2 / \langle N_{recMC}^{\Lambda} \rangle^2);$$

from signal variation of the Λ – hyperon(Data/MC)

2
$$\Delta Y_{\Lambda_{sys_cut_var}} = 0.004$$
 – from the variation of the Λ – hyperon selection criteria;

3
$$\Delta Y_{\Lambda_{sys}} = \sqrt{\Delta Y_{\Lambda_{sys_signal_var}}^2 + \Delta Y_{\Lambda_{sys_cut_var}}^2}$$
 – total systematic uncertainty;

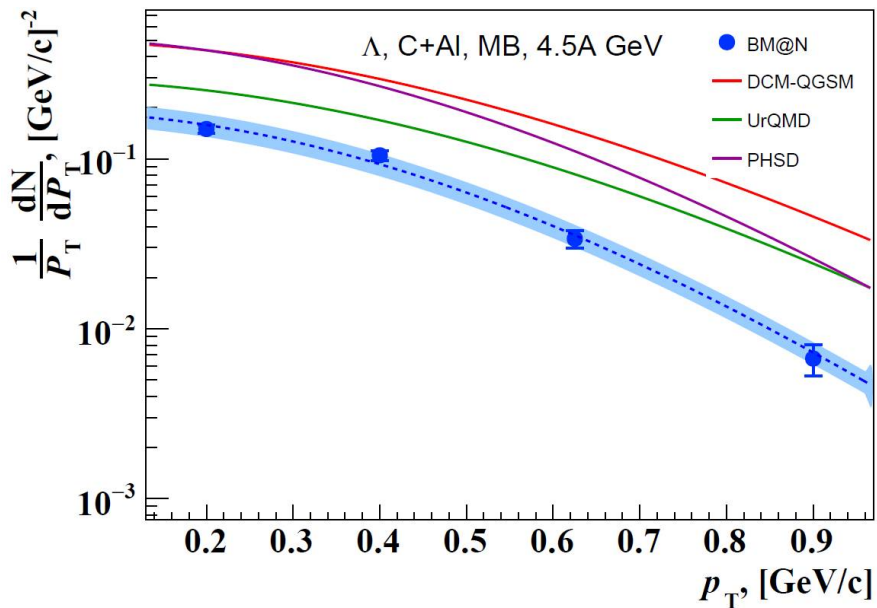
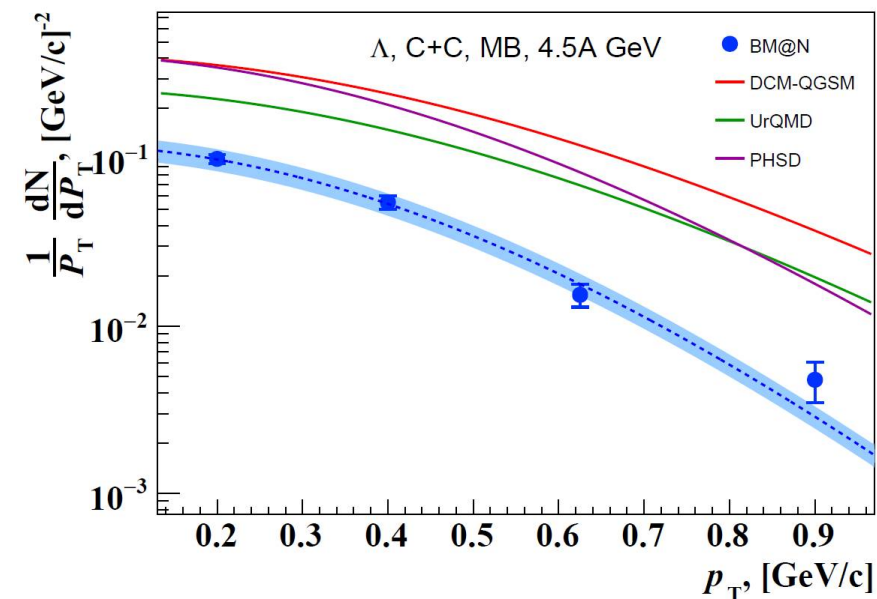
The results (Preliminary) of the integrated yields of the Λ

Systematics from variations of **dca** and **path** parameters $\pm 10\%$ systematics is within $\pm 10\%$;
 Systematics from variations of signals under different approaches to background estimation is $\pm 15\%$;

Full systematics is given in the tables 

Target	Energy, AGeV	$Y_{\Lambda} \pm \Delta Y_{\text{stat}\Lambda} \pm \Delta Y_{\Lambda_{\text{sys}}}$	Energy, AGeV	$Y_{\Lambda} \pm \Delta Y_{\text{stat}\Lambda} \pm \Delta Y_{\Lambda_{\text{sys}}}$
$0.1 < p_T < 1.05$ and $1.2 < y_{\text{lab}} < 2.1$ (Full acceptance)				
C + C	4.0	$0.011 \pm 0.001 \pm 0.004$	4.5	$0.013 \pm 0.002 \pm 0.005$
C + Al		$0.032 \pm 0.004 \pm 0.006$		$0.025 \pm 0.003 \pm 0.005$
C + Cu		$0.030 \pm 0.003 \pm 0.005$		$0.037 \pm 0.004 \pm 0.006$
C + Pb		$0.039 \pm 0.008 \pm 0.009$		$0.033 \pm 0.010 \pm 0.010$

Invariant p_T spectra of Λ hyperons vs models predictions(Preliminary)



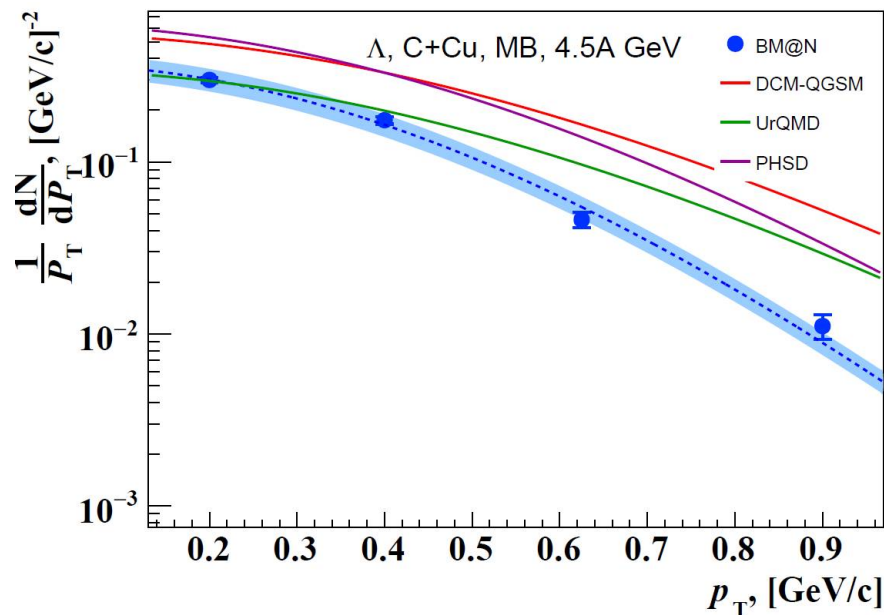
The measured spectra of the Λ yields in p_T are parameterized by the formula:

$$1/p_T d^2N/dp_T dy = N \cdot \exp(-(m_T - m_\Lambda)/T_0)$$

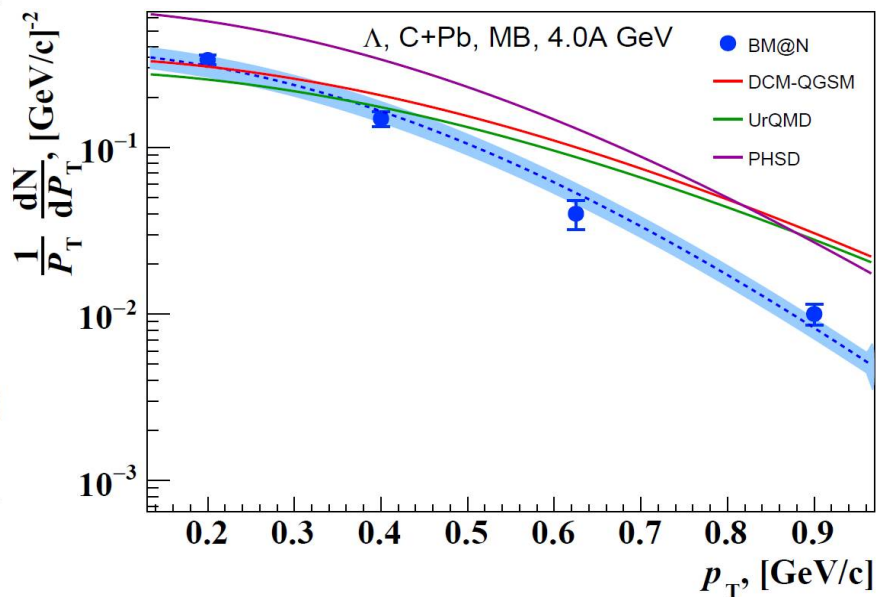
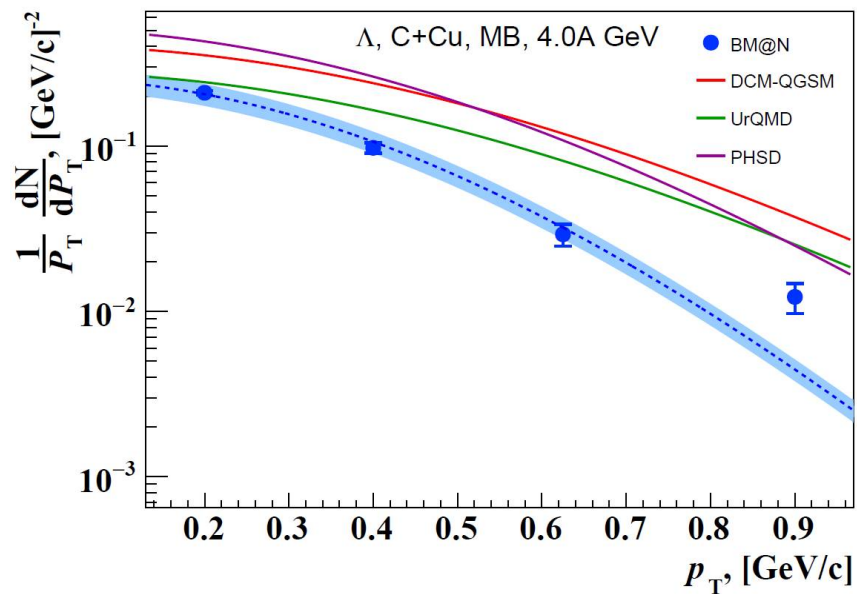
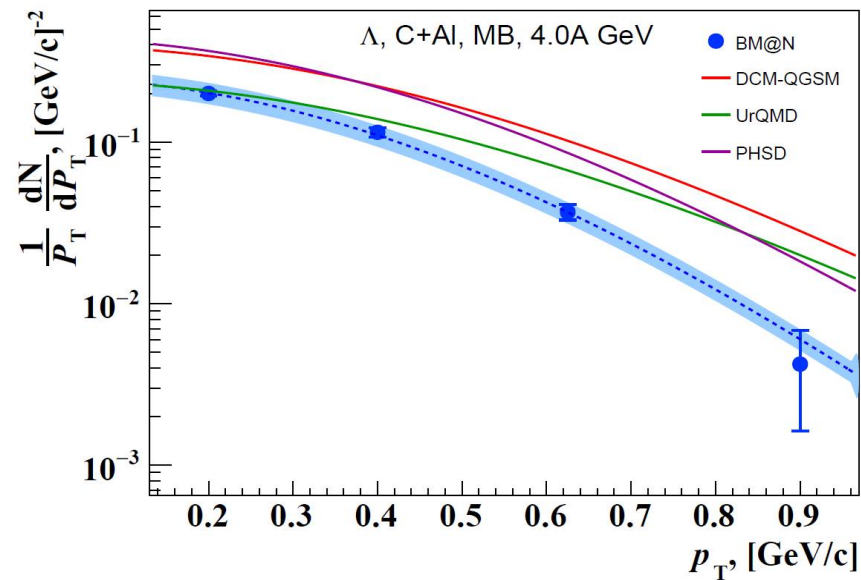
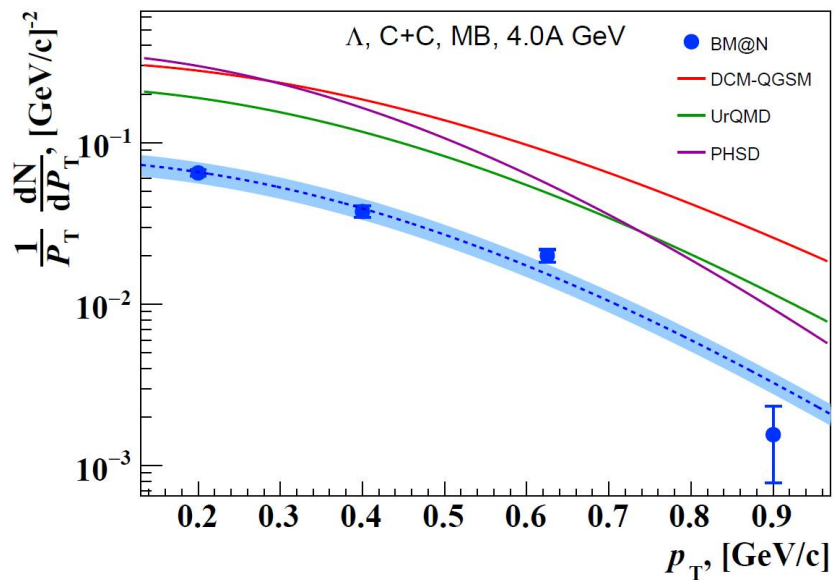
The transverse mass $m_T = \sqrt{m_\Lambda^2 + p_T^2}$,

The N normalization,

The inverse slope parameter T_0 are free parameters of the fit;



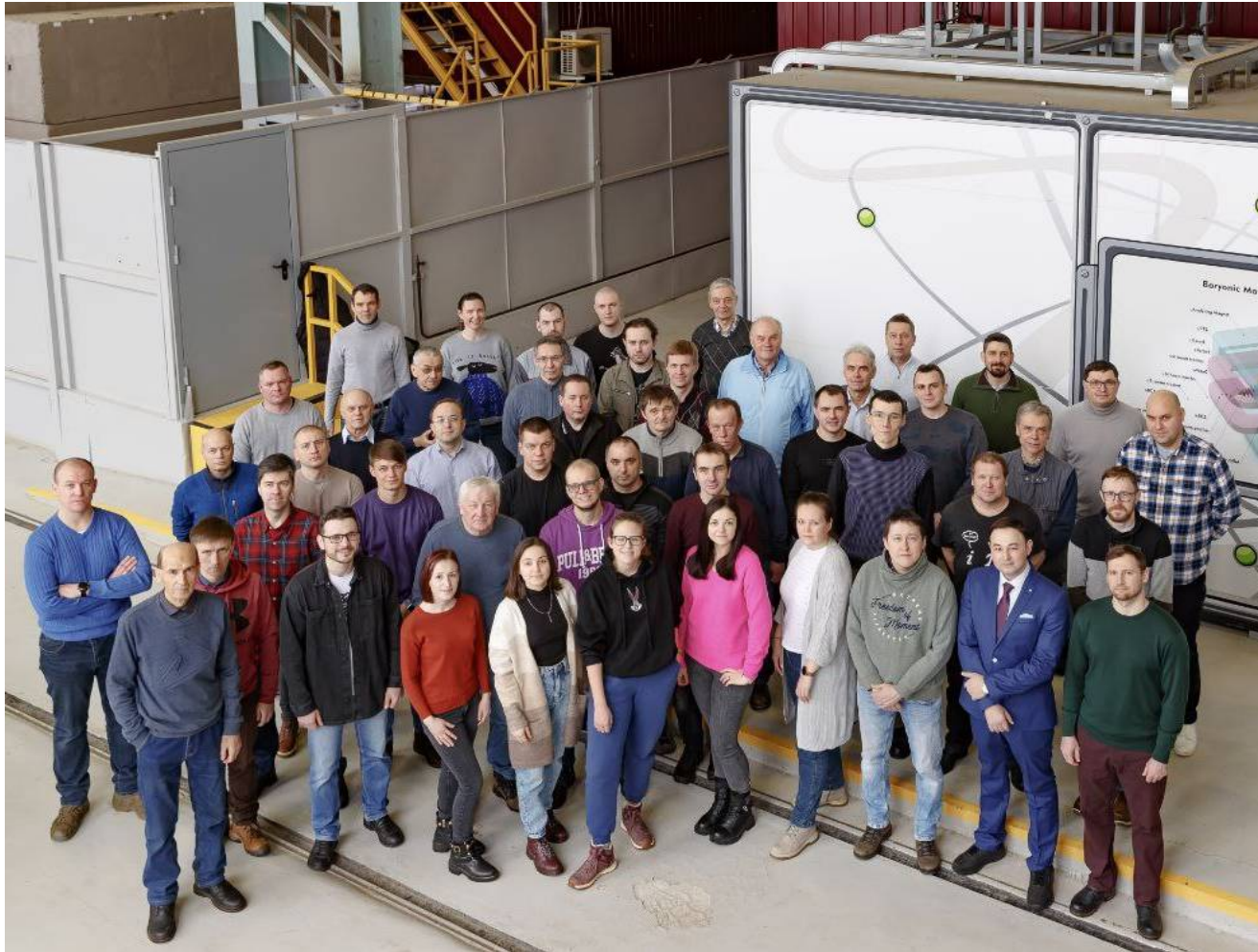
Invariant p_T spectra of Λ hyperons vs models predictions(Preliminary)



SLOPE RESULTS (Preliminary)

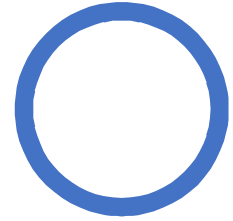
4.0 AGeV	T_0 , MeV, C+C	T_0 , MeV, C+Al	T_0 MeV, C+Cu	T_0 MeV, C+Pb
BM@N	$114 \pm 19 \pm 17$	$108 \pm 16 \pm 16$	$96 \pm 14 \pm 14$	$83 \pm 8 \pm 12$
DCM - QGSM	126	120	133	130
UrQMD	107	128	133	136
PHSD	87	100	105	98

4.5 AGeV	T_0 , MeV, C+C	T_0 , MeV, C+Al	T_0 , MeV, C+Cu	T_0 , MeV, C+Pb
BM@N	$116 \pm 24 \pm 17$	$115 \pm 7 \pm 17$	$101 \pm 3 \pm 15$	Due to low statistics
DCM - QGSM	132	133	135	142
UrQMD	122	128	130	134
PHSD	101	106	109	108

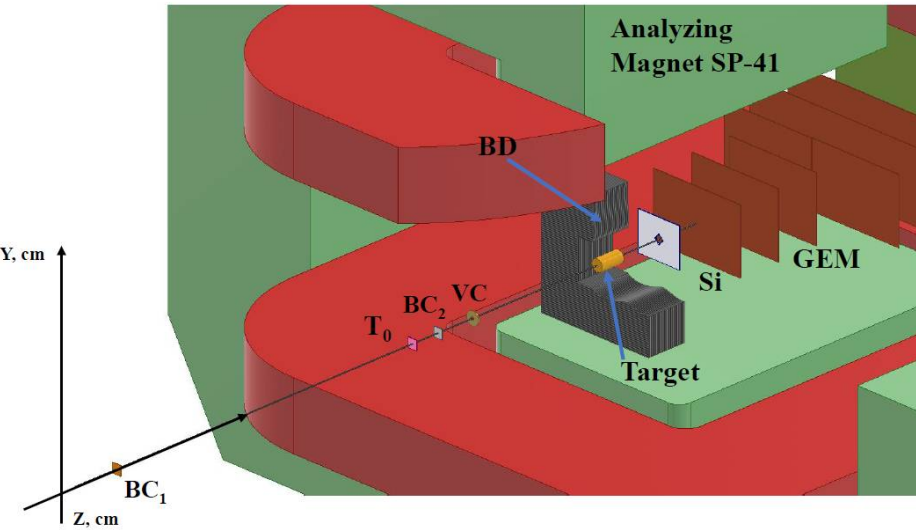


Thank you for your attention

Back up



Event selection criteria



- 1 | Number of tracks in selected events:
positive \geq 1, negative \geq 1
- 2 | Number of signals in the start detector: $T_0=1$
- 3 | Number of signals in the beam counter:
 $BC_2=1$
- 4 | Number of signals in the veto counter around
the beam: Veto=0
- 5 | Trigger condition in the barrel detector: number
of signals $BD\geq 2$ or $BD\geq 3$ (run dependent)

1 | Gem's Efficiency(**next slide**, example C+C);

2 | Track hits residual corrections*;

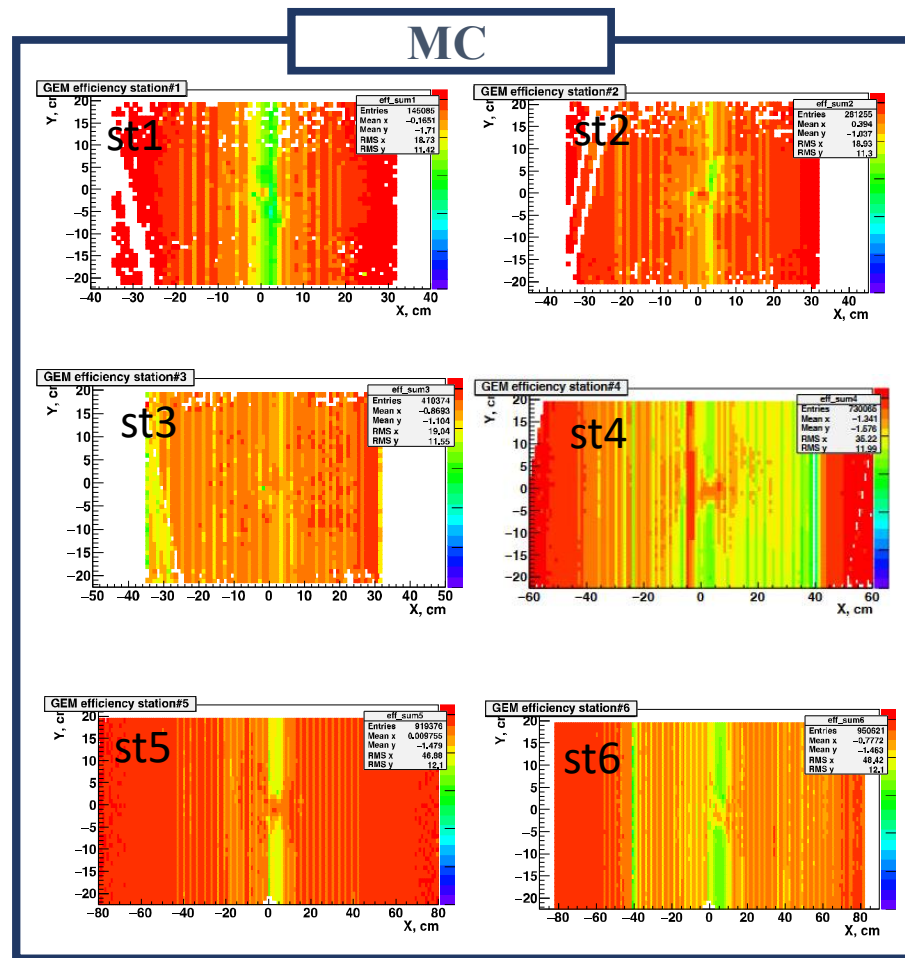
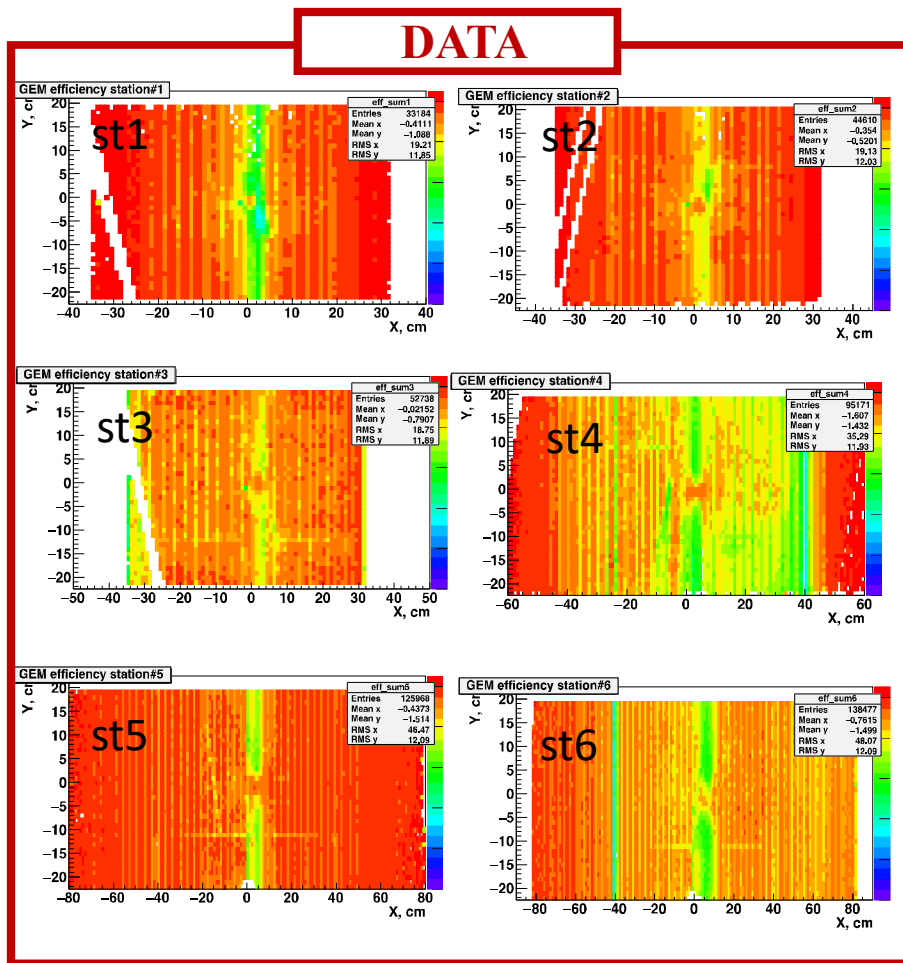
3 | Track hit position error corrections;

4 | Residuals width vs. momentum corrections;

Yury Stepanenko

*K. A. Alishina, Yu. Yu. Stepanenko, A.Y Khukhaeva” Gem residuals corrections in monte-carlo simulation for the run 6 at the BM@N experiment”, PEPAN letters – volume 19, part 5, 2022

GEM efficiencies comparison Data/MC (4.0GeV C+C) after applying effs to MC

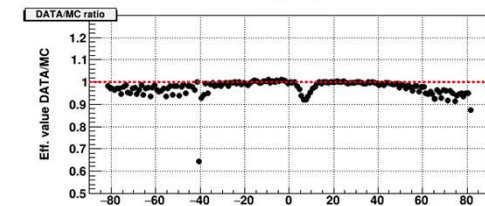
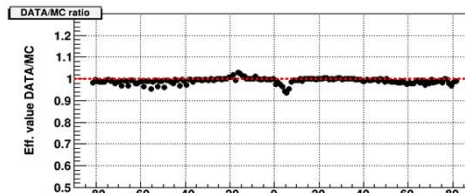
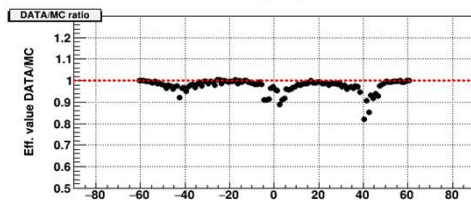
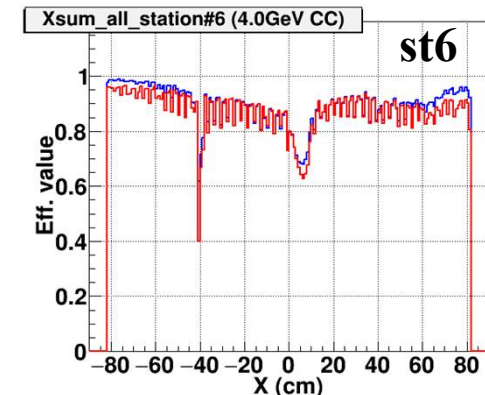
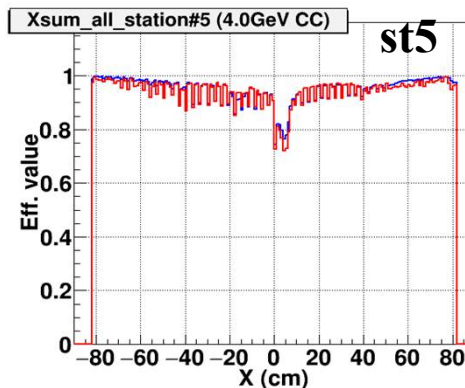
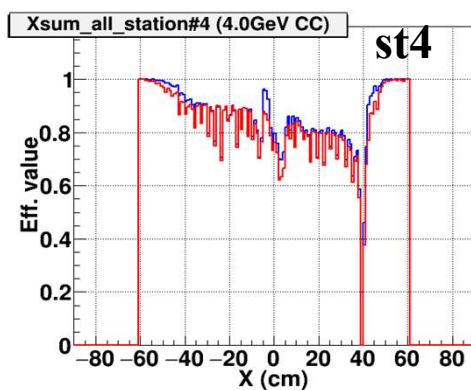
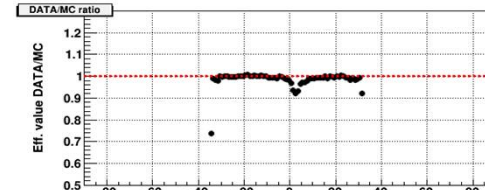
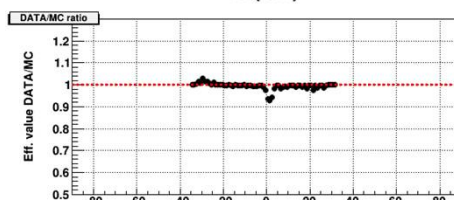
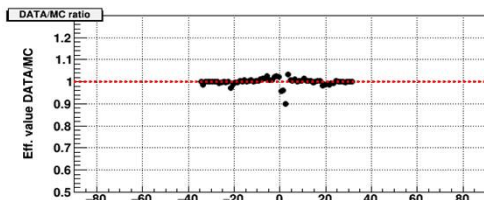
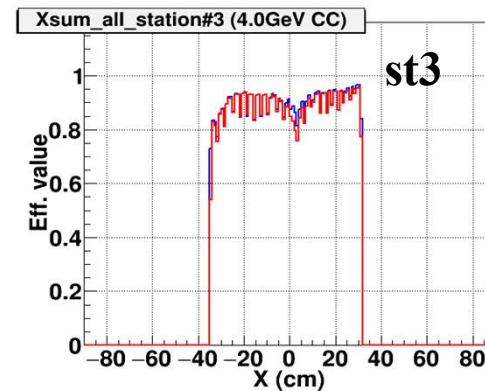
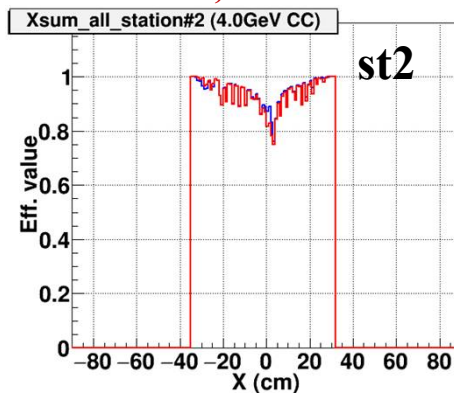
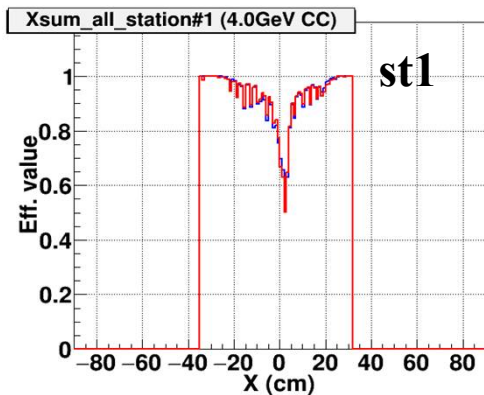


For each GEM station they were estimated using the following approach:

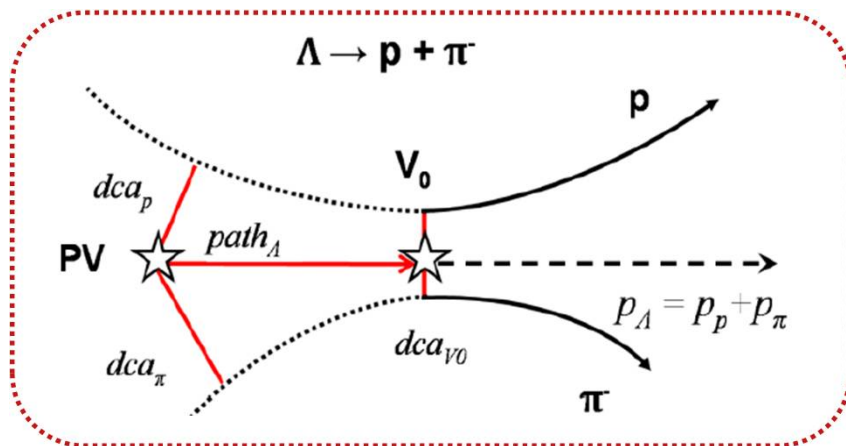
1. Select good quality tracks with the number of hits per track (excluding the station under study) not less than N;
2. Check that track crosses the detector area, if yes, add one track to the denominator;
3. If there is a hit in the detector, which belongs to the track, add one track to the numerator;
4. **GEM** efficiency = sum of tracks in numerator / sum of tracks in denominator.

1D GEM efficiency comparison between the experimental data and MC (4.0GeV C+C)

Data—red line, MC—blue line;



Selection of events with Λ hyperon



Event topology:

PV – primary vertex

V0 – vertex of hyperon decay

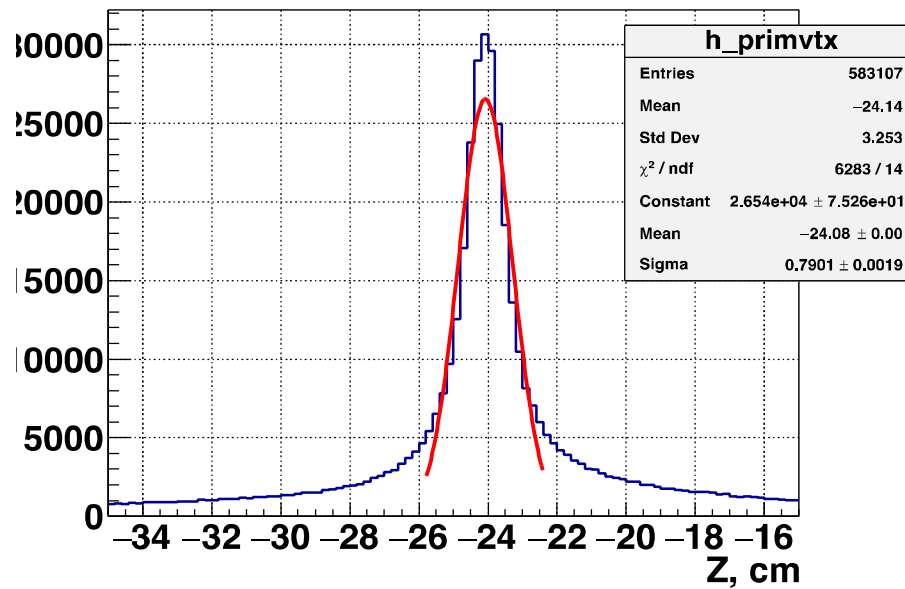
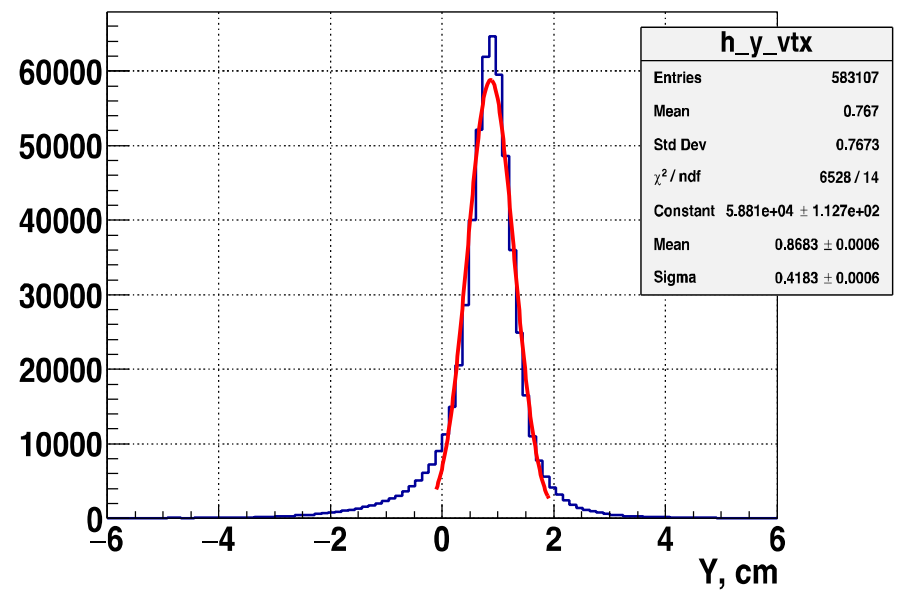
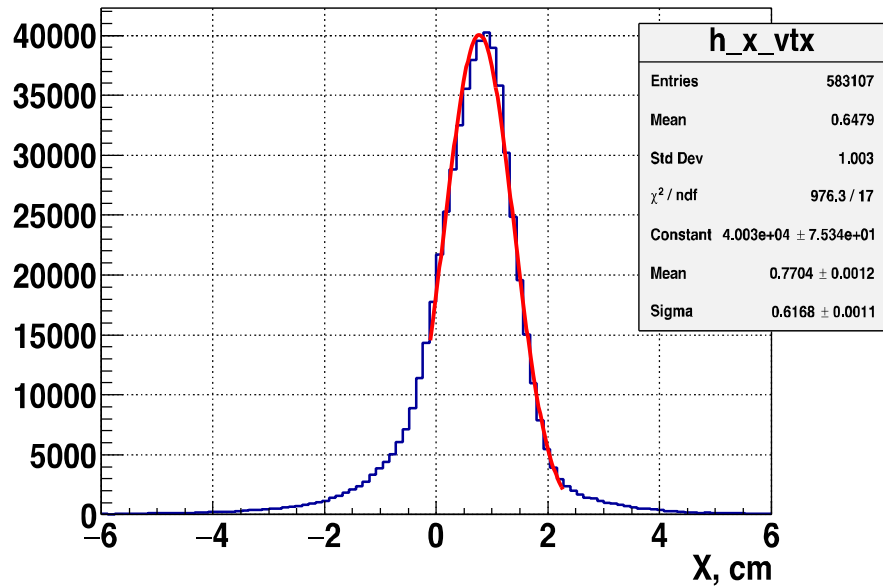
dca – distance of the closest approach

path – decay length

Criteria for the selection of Λ - hyperons :

- 1 Each track has at least 4 of the 6 hits in (Si+GEM);
- 2 $p_{\text{pos}} < 3.9(4.4)$ GeV/c for a beam energy of 4 (4.5) AGeV;
- 3 $p_{\text{neg}} > 0.3$ GeV/c;
- 4 $dca < 1$ cm;
- 5 Distance between the decay vertex V_0 and the primary vertex: $\text{path} > 2.5$ cm;

X, Y, Z distributions of the experimental primary vertex

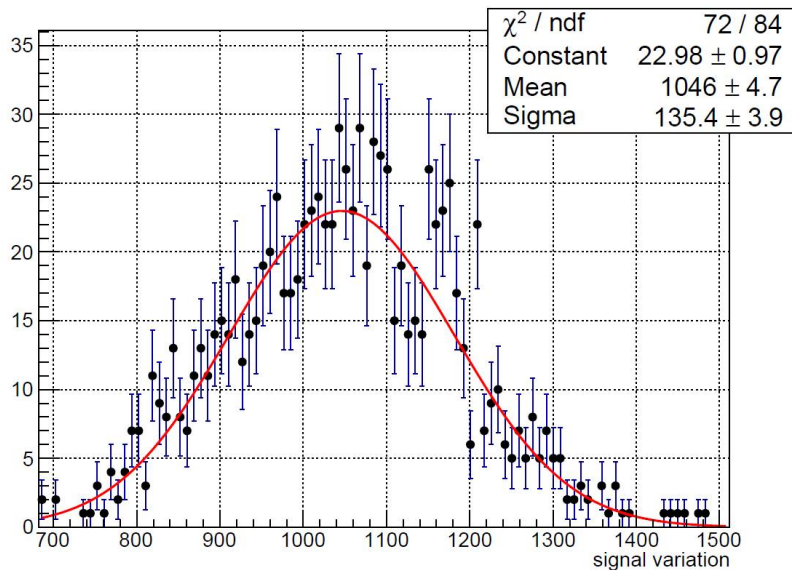


Pseudo-experiment

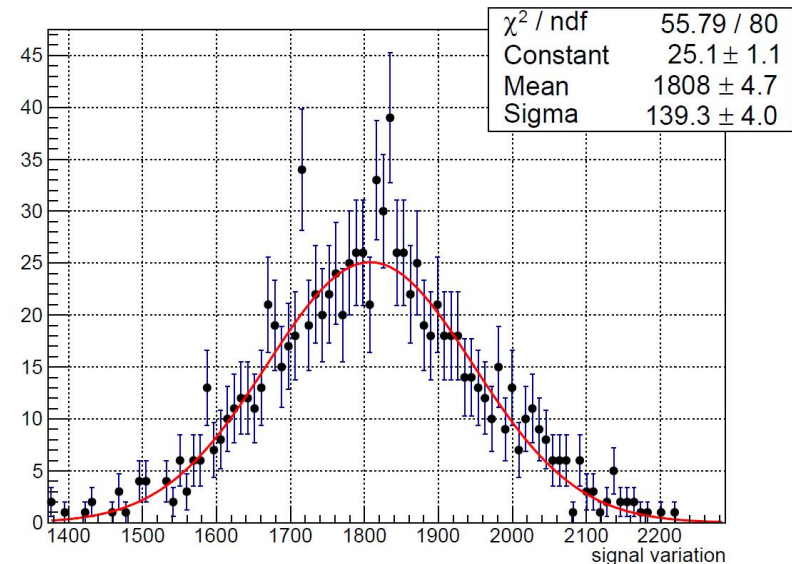
In each bin the bin content was modified by gaussian distribution with the widths equal to the bin error.

The “new” histogram was fit and the new signal was evaluated.

Procedure was repeated 1000 times and the **signal variation** are presented in a **bottom histogram**.



$$1.2 < y_{\text{lab}} < 1.33, 0.1 < p_{\text{T}} < 0.2$$



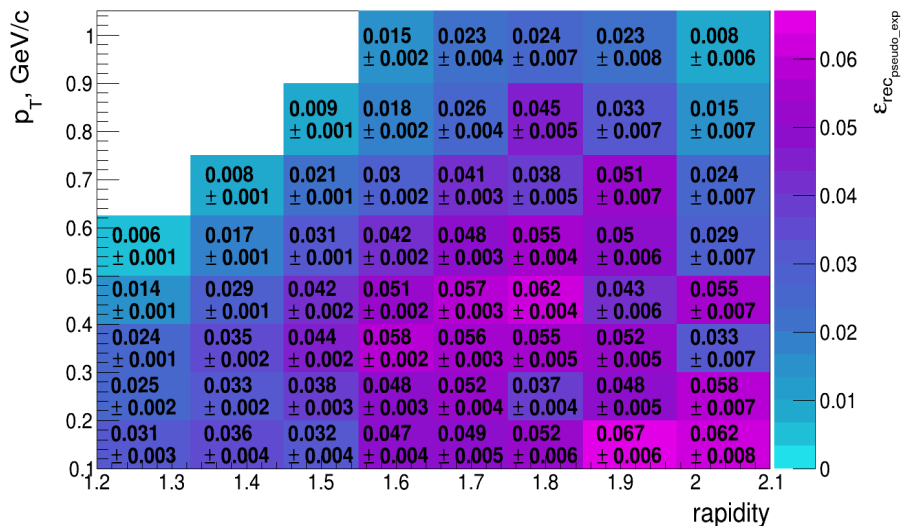
$$1.33 < y_{\text{lab}} < 1.45, 0.2 < p_{\text{T}} < 0.3$$

Red Line – Fit function $\text{Gauss}(\langle N_{\text{recMC}}^\Lambda \rangle, \sigma_{N_{\text{recMC}}^\Lambda})$

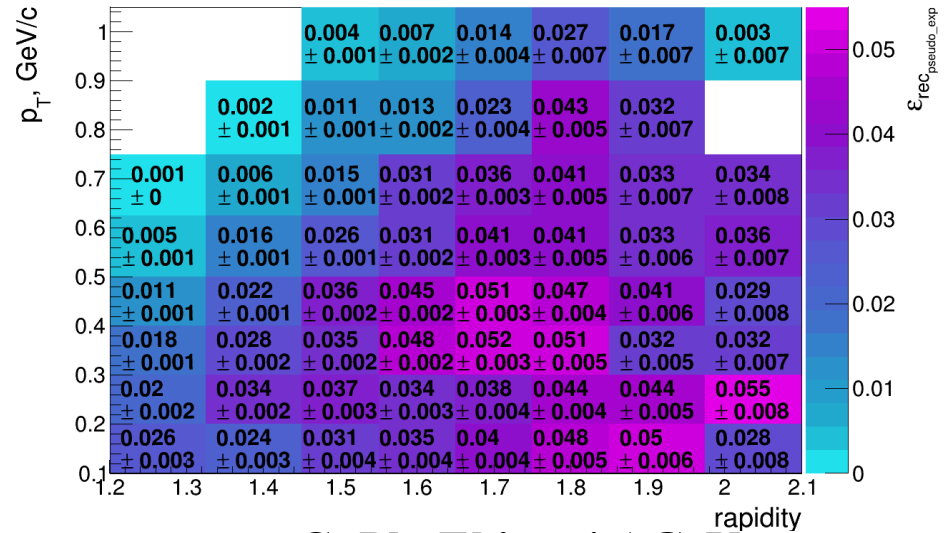
- 4 Each event is weighted with $\varepsilon_i = \langle N_{\text{recMC}}^\Lambda \rangle_i / N_{\text{gen}_i}^\Lambda$ is evaluated number of Λ , $N_{\text{gen}_i}^\Lambda$ is the number of Λ generated; $\Delta\varepsilon_i = \sigma_{N_{\text{recMC}_i}^\Lambda} / N_{\text{gen}_i}^\Lambda$ is evaluated error.

Spectrometer acceptance ($\varepsilon_i \pm \Delta\varepsilon_i$) for Δ in (y, p_T) cells

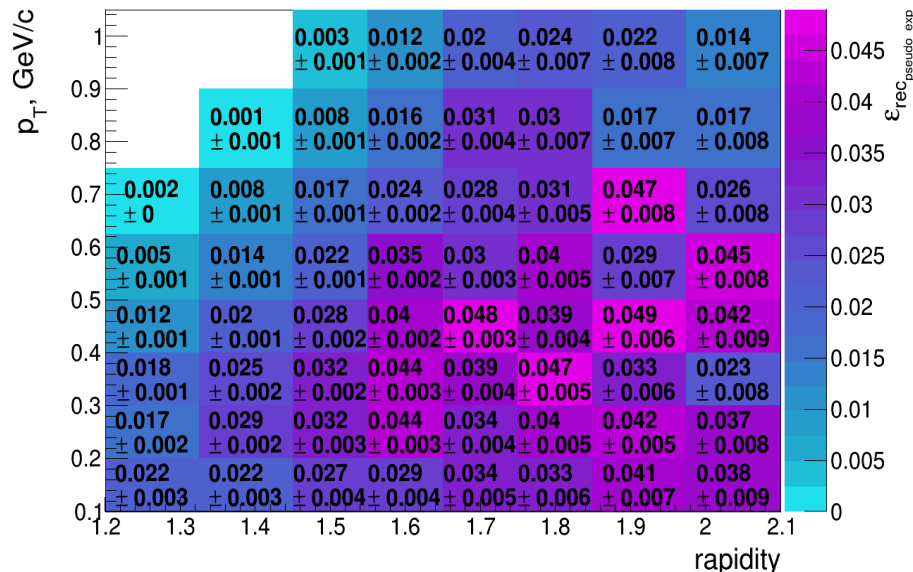
C+C, E_{kin} = 4 AGeV



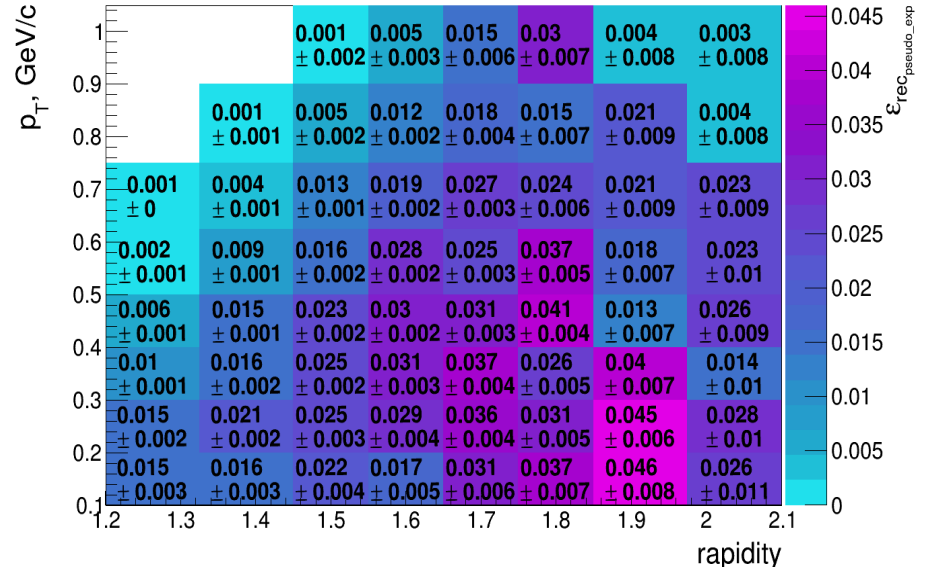
C+Al, E_{kin} = 4 AGeV



C+Cu, E_{kin} = 4 AGeV

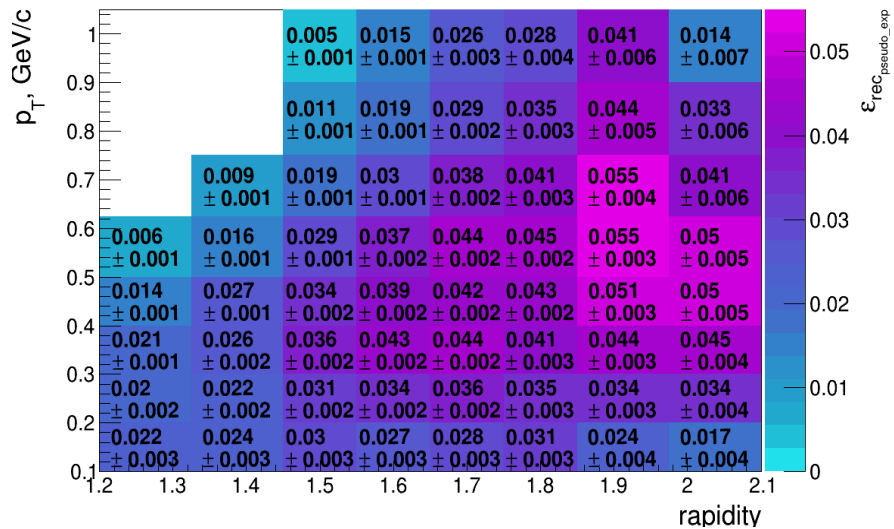


C+Pb, E_{kin} = 4 AGeV

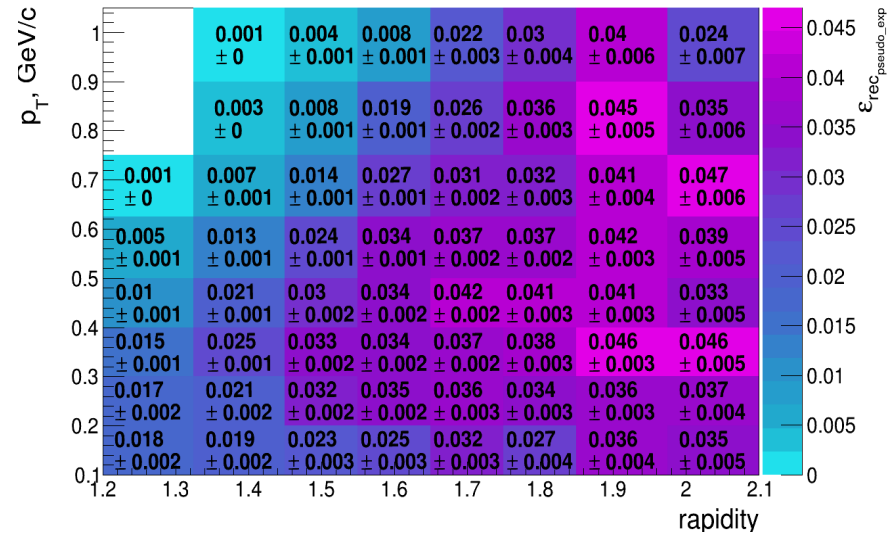


Spectrometer acceptance ($\varepsilon_i \pm \Delta\varepsilon_i$) for Λ in (y, p_T) cells

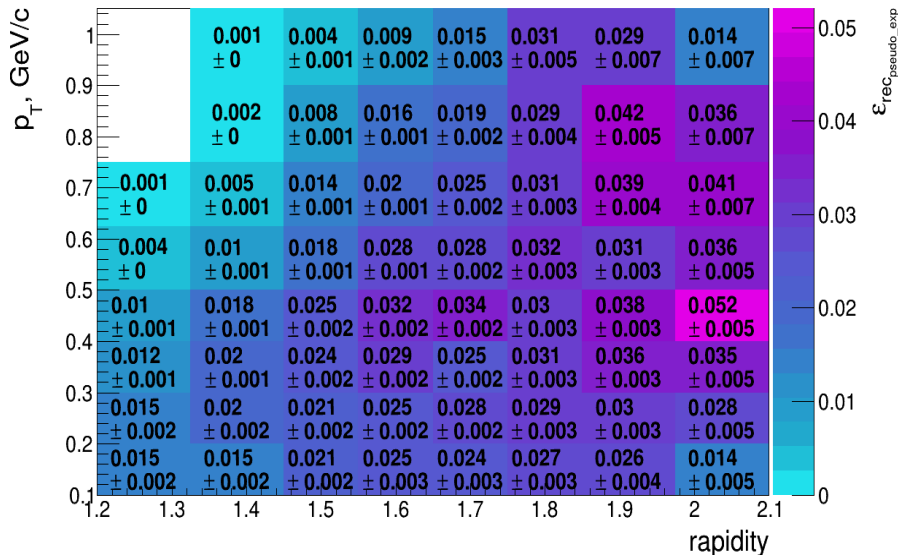
C+C, E_{kin} = 4.5 AGeV



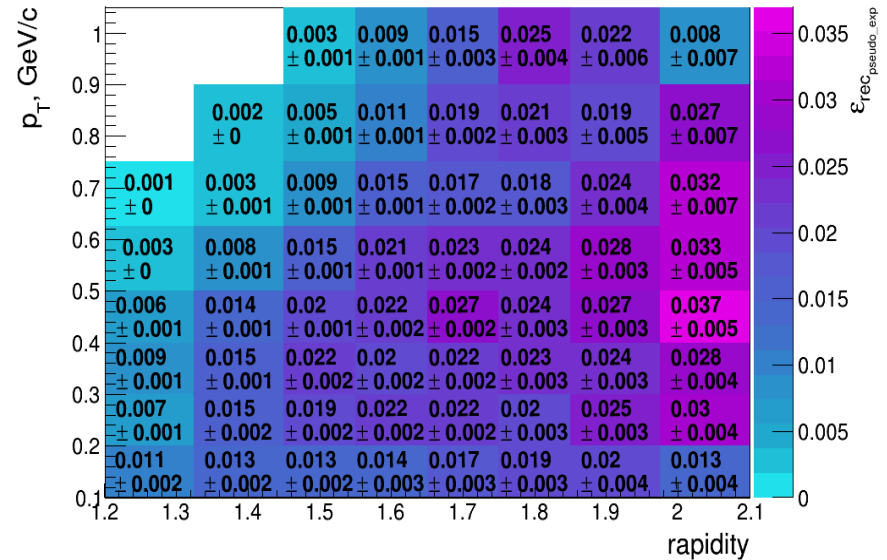
C+Al, E_{kin} = 4.5 AGeV



C+Cu, E_{kin} = 4.5 AGeV



C+Pb, E_{kin} = 4.5 AGeV



1 part

An approach in the estimation of systematic uncertainties related to the variation of selection criteria for events with Λ -hyperons.

The selection criteria considered are **path, dca**.

Nominal Analysis: $dca < 1 \text{ cm}$, $path > 2.5 \text{ cm}$;

Cut variation 1:

$path > 2.25 \text{ cm}$, **fixed:** $dca < 1 \text{ cm}$;

$path > 2.75 \text{ cm}$,

Cut variation 2:

$dca < 0.9 \text{ cm}$,

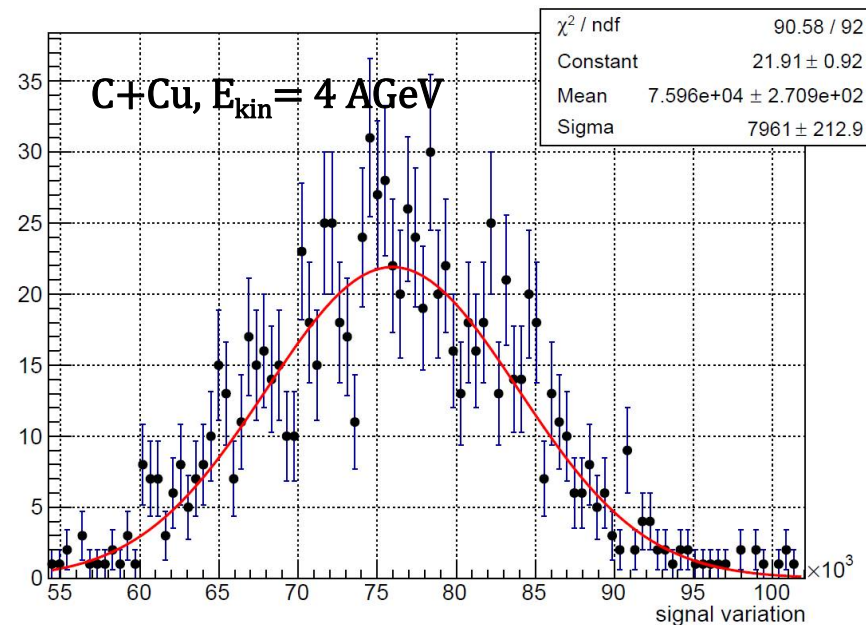
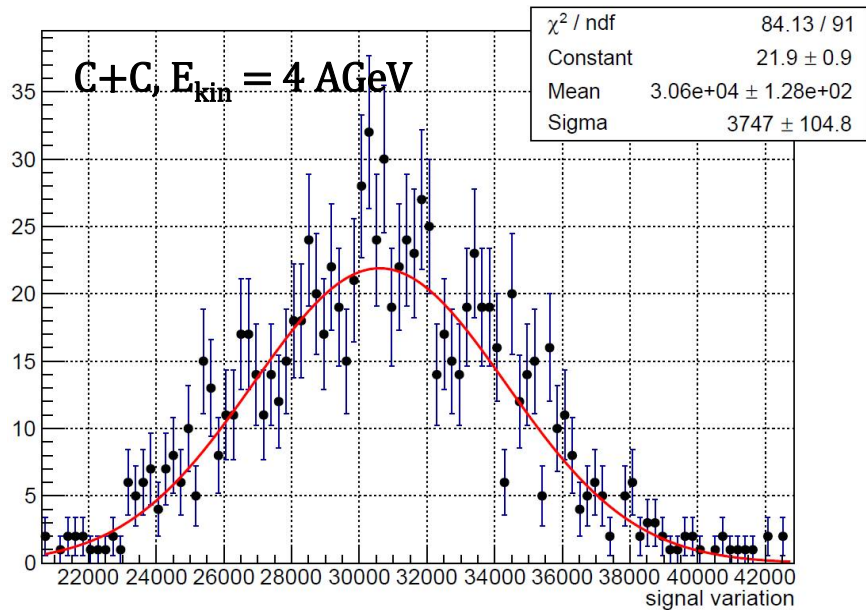
$dca < 1.1 \text{ cm}$, **fixed:** $path > 2.5 \text{ cm}$;

Combined systematic uncertainties

C+Cu, $E_{\text{kin}} = 4.5$ AGeV

dca	path	Yields (with cut variation)	Yields (nominal analysis)
Data statistic – II period			
Fixed: dca <1 cm	Path >2.25	0.043±0.004	0.035±0.009±0.007
	Path >2.75	0.042±0.004	
dca <0.9 cm	Fixed: Path >2.5	0.041±0.004	
dca <1.1 cm		0.042±0.004	
Data statistic – I period			
Fixed: dca <1 cm	Path >2.25	0.037±0.004	0.035±0.011±0.003
	Path >2.75	0.036±0.005	
dca <0.9 cm	Fixed: Path >2.5	0.038±0.004	
dca <1.1 cm		0.039±0.005	
Data statistic – (I + II) periods			
Fixed: dca <1 cm	Path >2.25	0.041±0.003	0.037±0.007±0.004
	Path >2.75	0.041±0.003	
dca <0.9 cm	Fixed: Path >2.5	0.041±0.003	
dca <1.1 cm		0.041±0.003	

Uncertainties from signal variation (BM@N DATA)



2 part

Red Line – Fit function

$$\text{Gauss}(\langle N_{recDATA}^\Lambda \rangle, \sigma_{N_{recDATA}^\Lambda})$$

$$0.1 < p_T < 1.05$$

and

$$1.2 < y_{lab} < 2.1$$

$$\Delta\sigma_\Lambda = \sigma_{N_{recDATA}^\Lambda} / (\varepsilon_{trig} \times \varepsilon_{pileup} \times L)$$

$$\Delta Y_{stat\Lambda} = \Delta\sigma_\Lambda / \sigma_{inel}$$

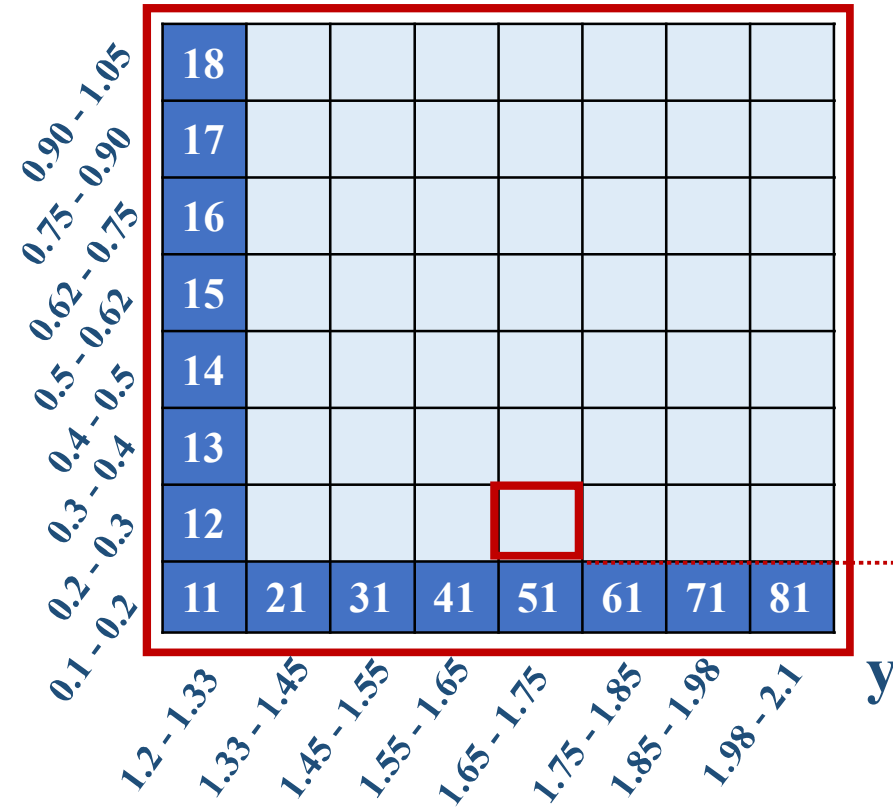
Acceptance evaluation procedure (DCM - QGSM)

Kinematic measuring range (4, 4.5 AGeV):

$$0.1 < p_T < 1.05 \text{ GeV}/c$$

$$1.2 < y_{\text{lab}} < 2.1$$

$p_T, \text{ GeV}/c$



1

Divide the kinematic measuring range by y, p_T into (8×8) cells in the MC simulation.

2

To get the number of events generated by the MC.

3

In each cells the invariant mass distribution fit with

$$f_{bg} = N \cdot (m - M_0)^A \cdot e^{-B \cdot (m - M_0)}$$

N, A, B are free parameters,

$M_0 = 1.078 \text{ GeV}/c^2$ is the threshold limit, m is the mass value.

